

ARTS1030

: cfa gʻcZK f]h]b[.'@]hYfUh fYž; YbfYž7i `h fY

HYfa 'C bY''##'&\$&\$

7ci fgY'Cj Yfj]Yk

Ghuzz 7 cbhuWh8 Yhu]`g

'7cbj Ybcfg'

BUa Y	9a U]`	5j U]`UV]`] m	@cWJhjcb	D\cbY
G][] [·] >ch <u>U</u> bXh	g"^chh_UbXh4 i bgk "YXi "Ui	Vm'Uddc]bha Ybh	K YVghYf" %%>	l)*,%

GWXcc`7cbHJWh =bZcfa Uhlcb

Fcca " %&ž~Yj Y~" FcVYfhK YVghYf~6i]X]b[

D\cbY.'f\$&Ł'-',)'(,)*

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.##gUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck``YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubgž h\Y'6YXY[U'`fPYbg]b[tcb'WJadigŁZ'; UX][U'`fP]tmUbX'5fti/'8Yg][b'7UadigYgŁUbX't\Y'B[ibbUkU`dYcd'Y'fbighfU`]Ub'8YZYbW': cfW'5WJXYam]b'7UbVYffUŁ'cZh\Y'`UbXg'k\YfY'YUW\'WJadig'cZIBGK']g`cWJhYX''$

7ci fgY 8YHJ] g

7 fYX]hDc]bhg * *

Gi a a UfmcZh\Y'7ci fgY

H\]g`Wci fgY`]bhfcXi WYg`mci `hc`9b[`]g\`h\fci [\`h\Y`ghi XmcZ`]hYfUfmZcfa "`: cW g]b[`cb`h\Y`a U'cf``]hYfUfm [YbfYg`cZdcYhfmždfcgY`UbX`XfUa Užh\Y`Wci fgY`k]``Yl Ua]bY`k Umg`cZk f]h]b[`]b`9b[`]g\`Zfca `U`fUb[Y`cZdYf]cXg`UbX`W`hi fU``hfUX]h]cbg`]bWi X]b[`bcb!6f]h]g\`UbX`dfY!Hk Ybh]Yh\`WYbhi fm''±ik]```U`gc`]bhfcXi WYmci `hc`h\Y`gdYW]U`]gYX`j cWUVi `UfmcZ`]hYfUfmUbX`hYl hi U``UbU`mg]g"

7 ci fgY @YUfb]b[Ci hWca Yg

&" 7 f]h]WU``mUbU`mgY``]hYfUfmihYI hg`]b'hYfa g'cZei Ygh]cbg'cZ`]hYfUfmiZcfa

' " 7 cbXi WhVUg]WfYgYUfWX cb``]MYfUfmiNYI hgži g]b['Uddfcdf]UNY gWXc`Uf`mifYgci fWYg

("5fi)W`UhY`UbX`WcbhYI hi U`]qY`mci f`ck b`Wf]h]WU``dcq]h]cb

) " 7 cbg/fi Whubx uff/W `uh/ `urWf/hWU` uff i a Ybhcfu``mubx]b k f]h]b[

*" I gY 'Uddfcdf]UhY 'Zcfa Uhg ']bWi X]b['WcffYWhfYZYfYbW]b['hc 'dfYgYbhmci f'k cf_

HYUW]b[GhfUhY[]Ya

H\Y`Wci fgY`]g`HJi [\hih\fci [\``YWfi fYg`UbX`hi hcf]U`g`UbX`cbY`\ci f`cZghfi Wfi fYX`cb`]bY``YUfb]b[`'UWhji]hm'

@YWhi fYq.

H\Y^YWi fYg'UfY`XYg][bYX hc']blfcXi WYghi XYbhg hc'h\Y']ggi Yg'UbX'hYl hg'cZh\Y'Wci fgY'Vmdfcj]X]b[
WcbhYl hi U`]bZcfa Uh]cbz'ci h]bYg'cZWf]h]WU`fYgdcbgYg'hc'h\Y'hYl hg'UbX'gca Y'WcgY'X]gW gg]cb"'@YWi fYg
U'gc'a cXY`Zcf'ghi XYbhg'h\Y'k Umg']bZcfa Uh]cb']g'cf[Ub]nYX'UbX'dfYgYbhYX']b'h\Y'X]gW]d`]bY'cZ9b[`]g\"
H\YfY'k]``'VY'cddcfhi b]h]Yg']b'Yj Yfm`YWi fY'Zcf'ei Ygh]cbg'UbX'[YbYfU'X]gW gg]cb"'7 YfhU]b'gWXYXi `YX

'YWi fYg'UXXfYgg'h\Y'gdYW]Z]Wg'cZUbU'mg]gz'Uf[i a YbhUh]cb'UbX'k f]h]b[']b'Vch\'YggUmg'UbX'Yl Ua g"'H\Y

'YWi fY'Zcfa Uh]g']a dcfhUbh]b'h\Uh]hXYa cbghfUhYg'Zcfa U`a cXYg'cZdfYgYbh]b['U'ghfi Wi fYX'Uf[i a Ybhz'UbX

Zcf'h\]g'fYUgcb 'YWi fY'UhhYbXUbW']g'Wca di 'gcfm''9UW\'YWi fY'k]``']bWi XY'U'g\cfhcb']bY'ei]n'k \]W\'a i gh

VY'Wca d'YhYX'Xi f]b['U'gdYW]Z]YX'h]a Y'Xi f]b['h\Y'`YWi fY"'H\YgY'ei]n'fYgdcbgYg'k]``'dfcj]XY'U'ghUfh]b[

dc]bhZcf'X]gW gg]cb']b'hi hcf]U'g"'H]a YhUV'Y WUg\Yg'a i ghVY']bX]j [Xi U`mUddfcj YX'Vmh\Y'Wci fgY

Wcbj Ybcfz'UbX'UfY'XYdYbXYbhcb'WffU]b'_Ymi bXYffU_]b[g'Vmghi XYbhg"'9Wxc'' *\$ 'gi ddcfhUbX

Dck YfDc]bhbchYg'UfY'Xfdcj]XYX'j]U'@A G'hc'gi ddcfhih\Y''YWi fYg'UbX'Zcf'fYj]g]cbz'bchUg'U'gi Vgh]hi hY'Zcf

'YWi fY'UhhYbXUbW'''

Hi hcf]U`g.

 $H\Y'h hcf]U'g'fYei]fY'gh XYbhg'hc'Yb[U[Y'UWhjY'mk]h h\Y'YWh fY'UbX'fYUX]b['a UhYf]U'`UbX'XYj Y`cd'h\Y]f ckb'Wf]h]WU''fYgdcbgYg''$

 $H\setminus g^*k$]``c\\\\\\fci[\.

- ````k YY_`mdfYdUfUhjcbž']bWi X]b[`XYj]g]b[`X]gWi gg]cb'ei Yghjcbg'Zcf'h\Y'[fci d'UbX#cf'fYgdcbgYg'hc ``YWi fY ei]nnYg
- · · · · · ghfi Whi fYX · UbX ·]bZcfa U · · WUgg · X]gW gg]cb
- ""Wc"UVcfUhjj Y'k cf_']b 'ga U`"[fci dg"

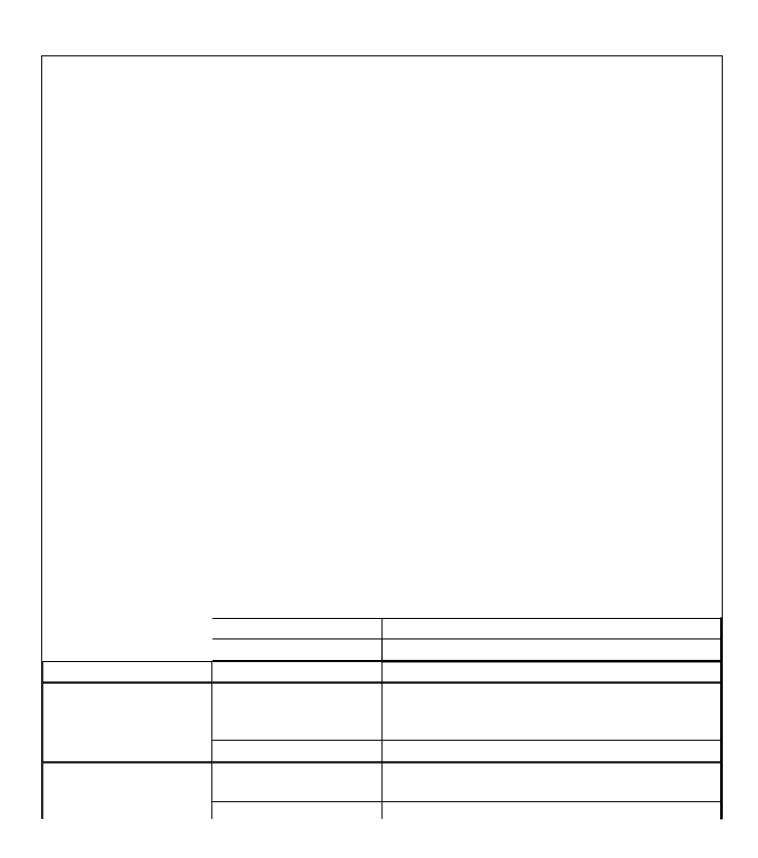
Cb`]bY'@YUfb]b['5Wh]j]hm

5 hih. Y 'VY[]bb]b['cZh\Y 'Wci fgY 'ghi XYbhg'k]``'Wca d`YhY 'U'cbY '\ci f'a UbXUhcfmcb`]bY 'WcgY 'fYUX]b[YI YfW]gY"'H\]g 'YI YfW]gY']g 'Vch\ 'X]U[bcgh]WUbX 'Zcfa Uh]j Yž 'UbX 'dfcj]XYg'h\Y 'cddcfhi b]hm'Zcf 'YUf'm'ZYYXVUW_Zfca 'hi hcfg"'H\Y 'UWfj]]hm]g 'bchdUfhcZh\Y 'UggYgga Ybh'Zcf'h\]g 'Wci fgY"

5ggYgga Ybh

5ggYgga YbhHUg_g

5 gg)Yggga YKbbHlbg_	K Y][\h	8i Y [.] 8UhY	Gh XYbh@YUfb]b[Ci hWca Y)



Hi hcf]U`	6ccW.Ub]ž@a 8dW V 4gffZW? ag`fS[e UbX'HU_Y
	< ca Y '91 Ua 'DfYdUfUh]cb

Fygci fWyg

DfYgWf]VYX`F Ygci fWYg`

8 fUa U. K]``]Ua G\U_YgdYUfYž=[Y >W\$d

G9H'H9LHG'!'Mci 'g\ci 'X'Ybgi fY'mci '\Uj Y'Wcd]Yg'cZh\Y'Zc'`ck]b[.

DcYlfm'dcYa g'gYh'Zcf'ghi Xmk]``'VY'Uj U]`UV'Y'j]U'h\Y'Wci fgY'A ccX'Y'g]hY

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

_Zmci YbWci bhYf'U'dfcV`Ya 'k \Yb'UhYa dhJb['hc'gi Va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]hJbž'd`YUgY
hY`Yd\cbY'9| hYfbU``Gi ddcfhcb'-',) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU`hY`hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft'' =Zmci
UfY'i bUV`Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZUi 'hk]h\'Hi fb]hJb'mci 'a Um'Udd'mZcf'Ub'Y! hYbg]cbžVi hmci
a i ghfYhU]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU``Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY`Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd`]WUhJcb'' =Zmci 'Ya U]`'9! hYfbU``Gi ddcfhmci 'k]``

5 WUXYa | W < cbYghmUbX D`U[| Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b['U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b['h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k]h\ci hUW_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci hWfYX]hUbX'hc d]YW]b['hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b["

7 c``i g]cb. 'k cf_]b['k]th 'cth Yfg'Vi hidUgg]b['cZZth Y 'k cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7 c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfglUbX`mci f`f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'Uhi BGK
- VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hzil BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5WWdhUV`Y'I gY'cZ I BGK '= H'F Ygci fWfg'Dc`]Wh
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWhYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wcaaib]hm
- `cWUHY 'gYfj]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm