

ARTS2040

; `cVU``@|hYfUhi fYg. '5Xj Ybhi fYg'k]h\`h\Y'"7cbhYa dcfUfm 7`Ugg]W

HYfa 'C bY''# '&\$&\$

7ci fgY'Cj Yfj]Yk

Ghuzz 7 cbhuWh8 Yhu]`g

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUhjcb	D\cbY
:]cbU^A cff]gcb	Za cff]gcb4 i bgk "YXi "Ui	K YX '%4 %	K YVghYf'&\$-	-',))&+)

GWXcc~7cbhJWh~abZcfa Uhlcb

Fcca " %&ž~Yj Y~" FcVYfhK YVghYf~6i]`X]b[

D\cbY.'f\$&Ł'-',)'(,)*

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.##gUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[tcb'WJadig\cong \cong mV][U'`fP]thubX'5fti/'8Yg][b'7UadigYg\cong \cong tUbX't\Y'B[ibbUkU`dYcd'Y'fbighfU`]Ub'8YZYbW': cf\W'5\WXYam]b'7UbVYffU\cozh\Y'`UbXg'k\YfY'YUW\`WJadig'cZl\BGK']g`c\WJhYX''$

7ci fgY 8YHJ] g

7 fYX]hDc]bhg**

Gi a a UfmcZh\Y 7ci fgY

 $K \ Y \ fY UX \ WcbhYa \ dcfUfm`]hYfUhi fY \ Z \ K \ Y \ bck \ k \ Uhi]g'j \ U`i \ UV`Y \ Z \ [ccX`cf``Ugh]b \ 3``8c'k Y \]a \ a \ YX]UhY`mfY \ b \ [b]gY`U````WUgg]W```k \ cf_'Vm]hg`gWcdY \ Z \ d`YI \]mUbX`W, U``Yb \ Y \ cf']hg`XUf]b \ Z \ YVUi \ hmcf \ X]gg]XYbW 3``<ck \ UbX`k \ mXcYg`h\Y```WUgg]W```HYI hYa \ Yf[Y`]b`h\Y`dfYgYbh3``H\ci [\````WcbhYa \ dcfUfm \ WUgg]W```gci \ bXg``]_Y`U`d]hW \ i \ gYX`Vmdi \ V`]g\Yfgz`]g`h\]g`U`hYfa \ h\Uha \][\ hYbUV`Y`X]gW \ gg]cb`cZf]W\`UbX \ Wca \ dY``]b[\ ``]hYfUfmk \ cf_g`\Zca \ h\Y``Ughh\]fhmmYUfg3$

7 ci fgY @YUfb]b[Ci hWca Yg

- % 9 I d`U]b`U`bi a VYf`cZh\YcfYhJWJ`]ggi Yg`]b`[`cVU``UbX`hfUbgbUhJcbU``k f]hJb[``UbX`UbU`mgY``]hYfUfm'UbX`Zja `hYI hg`hc``cWJhY`h\Y`q][b]ZJWJbWY`UbX`cdYfUhJcb`cZh\YqY`]gqi Yg
- &" 5bU`mgY`U`fUb[Y`cZk Umg`]b`k\]W\`h\Y`ei Ygh]cb`cZ`]hYfUfmj U`i Y`UbX``]hYfUfmZcfa 'Ya Yf[Yg`]b`h\Y WcbhYl hcZ[`cVU```]hYfUhi fYg`UWfcqg`U`fUb[Y`cZ[YbfYg"
- ' " 9a d`cmU`Wf]h]WU``UbX`h\YcfYh]WU``m]bZcfa YX`UddfcUW\`hc`hYI hg`i bXYf`X]gW gg]cbžUddfcdf]UhY`m gi ddcfhYX`VmigW\c`Uf`mfYgci f\Wg"
- (" 7 cbg/fi Wh`i WJX`k f]hhYb`Uf[i a Ybhg`VUgYX`i dcb`WcgY`UbU`mg]g`cZ`]hYfUfmi`Ub[i U[YžYh\]WU``i gY`cZ gW\c`Uf`mfYgci fWYgžUbX`h\Y`_Ymh\YcfYh]WU``WcbWYdhg`ghfi Wh f]b[`h\Y`Wci fqY"

HYUWX]b[GhfUhY[]Yg

H\]g`Wci fgY`k]```]blfcXi WY`ghi XYbhg`hc`h\Y`Z]Y`X`cZ[`cVU``UbX`k cf`X``]hYfUfmghi X]Yg`UhgYWcbX!nYUf``Yj Y`" H\Y`Wci fgY`k]```VY`cf[Ub]gYX`W\fcbc`c[]WU``mz`gc`h\Uhghi XYbhg`WUb`]XYbhJZmUbX`X]gWi gg`h\Y`W\Ub[]b[`]XYUUbX`]a dcfhUbWi`cZX]ZZYfYbh_]bXg`cZ`]hYfUfmj U`i Y`dYfWY]j YX`]b`X]ZZYfYbh`]hYfUfmhYI hg`cj Yf`hJa Y"

5ggYgga Ybh

=\Uj Y`gYhik c`UggYgga Ybhg"'H\Y``c[`UggYgga Ybhk]```gi ddcfhgca Y`fYUX]b[`]b`h\Ycf]Yg`cZk cf`X`]hYfUh fYž`UbX`Zcfa `U`gWUZZc`X`Zcf`h\Y`a U'cf`YggUmXi Y`Uh'h\Y`VY[]bb]b[`cZK YY_'%''

5ggYgga Ybh'HUg_g'

5ggYgga Ybh'hJg_	K Y][\h	8i Y'8UHY	Gh XYbh@YUfb]b[Ci hWca Ygʻ5ggYggYX
FYUX]b['UbX'FYgYUfWX'@c['	(\$1	%%#\$'#&\$&\$`\$\$\$`5A	%ž&Ž
A Uʻcfʻ9ggUmi	*\$1	&+#\$(#&\$&\$`\$).\$\$`DA	&ž ž(

5ggYgga Ybh8YhJ]`g

5ggYgga Ybh% FYUX]b[UbX FYgYUfWX @c[

GhUfh'XUhY.

@Yb[h\.'%) \$\$

5XX]h]cbU`XYhU]`g.

H\Y`fYUX]b[``c[`gi Va]gg]cb`k]```Wca df]gY`f\Y`' ``c[g`fcZ)\$\$`k cfXg`YUW\E'f\UhUfY`Xi Y`UhK YXbYgXUm - Ua `cZk YY_g`&Z` 'UbX`("`H\Y`K YY_'(`gi Va]gg]cb`k]```VY`U`XcW a Ybhf\UhWca V]bYg`U```f\fYY``c[g`Zcf k f]ftYb`ZYYXVUW_"`H\Y``c[g`Zcf`k YY_g`&`UbX`' `f\UhUfY`Xi Y`Uh- Ua `cb`K YXbYgXUmcZf\Y]f`fYgdYWf]j Y k YY_g`k]```cb`mfYWY]j Y`U``]fhY`ZYYXVUW_"`Hc `fYdYUh! `f\Y`Z]bU```c[`]b`k YY_'(`k]```VY`UXXYX`fc``c[g`%UbX`& fc`a U Y`cbY`XcWa YbhcZ%)\$\$`k cfXg`UbX`f\]g`k]```fYWY]j Y`gi gfU]bYX`ZYYXVUW"`

5ggYgga Ybh& A U/cf 9ggUm

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. &\$\$\$!&)\$\$

8 YHJ]`q. '&ž) \$\$ 'k cfXq" 'K f]HYb 'ZYYXVUW_ 'UbX 'bi a Yf]WJ``[fUXY 'j]U '@A G"

FYgci fWYg

DfYgWf]VYX`F Ygci fWYg`

 $6 \texttt{cc_g'WUb''VY'Zci} \ b \texttt{X']b''h} \texttt{Y'I} \ B \ G \ K \ "Vcc_g \texttt{Cd''UbX'Zfca} \ "fYdi \ h'UV'Y' fYh'U]'Yfg$

 $A \; cc \; X \; Y \; `Ub \; X \; @ Y [\; Ub \; hc \; `k \;] \; ``` dfcj \;] X \; Y \; `ch \; Y \; f \; f \; Y \; gci \; f \; W \; g \; \\$

FYWca a YbXYX FYgci fWYg

BchUj U]`UV`Y

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'=hWUb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UWW]XYbhU``mWcdm]b['Zfca `U`gci fW'k]h\ci hUW_bck `YX[Ya Ybh'

 $I BGK `[fci dg'd`U[]Uf]ga `]bhc'h\Y'Zc``ck]b[`WUhY[cf]Yg.$

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

5 WUXYa]W±bZcfa Uhjcb

: cf'YggYbhJU`gh XYbh]bZcfa UhJcb'fY`UhJb['hc.