

MUSC1604

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D\cbY.'f\$&E'-',)'(,)*

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K YVg]hY. k k k "Ufhg"i bgk "YXi "Ui #gUa

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck``YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubgž h\Y'6YXY[U'`fPYbg]b[tcb'WJadigŁZ'; UX][U'`fP]tmUbX'5fthZ''8Yg][b'7UadigYgŁUbX't\Y'B[ibbUkU`dYcd'Y'fbighfU`]Ub'8YZYbW': cfWY'5WJXYam]b'7UbVYffUŁ'cZh\Y'`UbXg'k\YfY'YUW\'WJadig'cZIBGK']g`cWJhYX''$

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7 fYX]h'Dc]bhg'*

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Gi VYWh5fYU. ? ge[U

H\]g`Wci fgY`dfcj]XYg`Ub`cj Yfj]Yk `cZh\Y`\]ghcfmž`[YbfYgž`UbX`_YmUfr]gh]WUbX`]bhY``YWi U``h\Ya Yg`]b K YghYfb`WUgg]WU``a i g]WZfca `h\Y`F YbU]ggUbW'`h\fci [\`hc`h\Y`dfYgYbhXUm'`H\fci [\`X]gW gg]cb`cZ g][b]Z]WUbhWca dcg]h]cbg`Zfca `X]ZZYfYbh\]ghcf]WU``dYf]cXgž`mci `k]```XYj Y`cd`Ub`cj Yfj]Yk `cZh\Y XYj Y`cda YbhcZa i g]WU``ghm`Yg`UbX`[YbfYg"`H\YgY`XYj Y`cda Ybhg`k]```VY`fY`UhYX`hc`_Ymi]XYc`c[]Yg`UbX d`UWYX`]b`\]ghcf]WU``UbX`gcW]U``WcbhYl hg"`6mh\Y`YbX`cZh\]g`Wci fgYž`mci `k]```VY`Yei]ddYX`hc`i bXYffU_Y XYhJ]YX`ghi Xm]b`gdYW]ZWUfYUg`cZWf]h]WU``Ybei]fm"

7 ci fgY @YUfb]b['Ci hWca Yg

- $% = XYbh]ZmUbX:XYgWf]VY:h,Y:\]ghcf]WU:Z:Ufh]gh]WUbX:gcW]U:WcbhYI:hg:cZ_Ymk:cf_g:cZK:YghYfb:WUgg]WU:a:i:g]W$
- &" 9 I d`U]b`UbX`X]gWi gg`h\Y`]bhYffY`Uh]cbg\]d`cZa i g]WUbX`_Ymih\Ya Yg`]b`9i fcdYUb`h\ci [\h'\' "FYgYUfW\ž`Wf]h]ei Y`UbX`X]gWi gg`K YghYfb`WUgg]WU`a i g]WžUVWi fUhY`mi g]b[`X]gW]d`]bY`gdYW]Z]W `Ub[i U[Y"

HYUWX]b['GhfUhY[]Yq'

H\Y'Wci fgY'k]``VY'HUI [\h']b``YWfi fYg'h\Uhi gY'U'k]XY'fUb[Y'cZUi X]c'UbX'j]gi U``fYgci fWrg'hc'Yl Ua]bY\]ghcf]WJ'ž'Ufh]gh]WUbX'gcW]U``WcbhYl hg'cZ_Ymk cf_g'cZK YghYfb'WUgg]WJ'`a i g]W''8]gW fg]j Y'gYgg]cbg'k]`` Z fh\Yf'XYj Y'cd'ghi XYbhi bXYfghUbX]b['cZh\Y']bhYffY`Uh]cbg\]d'cZa i g]WUbX'_Ymh\Ya Yg']b'9i fcdYUbh\ci [\h''Hi hcf]U`g'ZcW ggYX'cb``]ghYb]b['UbX'gWcfY'fYUX]b['k]``fYZ]bY'ghi XYbhUV]`]mhc'Wf]h]WJ\``mX]gW gg a i g]Wi g]b['X]gW]d')bY'gdYW]ZJWhYfa]bc`c[m'H\Y'XYj Y`cda YbhcZ]bhYfUWf]j Y'dfc'YWg'XfUk]b['h\YgY

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D`YUgY`gYY`AccX`Y`Zcf`XYHJ]`YX`]bZcfaUh]cb`UVcih'h\]g`WcifgY"

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5ggYgga Ybh'% 'DfYgYbhJh]cb 'UbX'dUfh]W]dUh]cb

GhUfhXUhY. Bch5dd`]WUV`Y

8 YHJ]`g.

%) \$\$ 'k cfXg" ``

Gh XYbhg fYWY]j Y k f]hhYb ZYYXVUW_UbX U bi a Yf]WU`a Uf_"

5XX]h]cbU`XYhJ]`g.

 $\label{thm:local_def} \begin{tabular}{ll} Hi hcf]U``UggYgga YbhhUg_g`k]```VY`dYfZcfa YX`h\fci [\ci hhi hcf]U```WUggYg"``5XX]h]cbU``]bZcfa Uh]cb`k]```VY dfcj]XYX`cb`A ccX`Y`UbX`]b``WUgg" \\ \end{tabular}$

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GhUfhXUhY. Bch5dd`]WUV`Y

8 YHJ] g.

*\$ Ei Yghcbg

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5XX]h]cbU`XYhJ]`g.

@]ghYb]b['HYghg'k]``'VY'\Y'X'Xi f]b['`YWh fYg'cf'h hcf]U'g'cf'gdYW]U``m'UffUb[YX'h]a Yg'Ug']bX]WUhYX']b'h\YWti fgY'gW\XXi 'Y'h]a YhUV'Y"

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GHJfhXUhY. Bch5dd`]WUV`Y

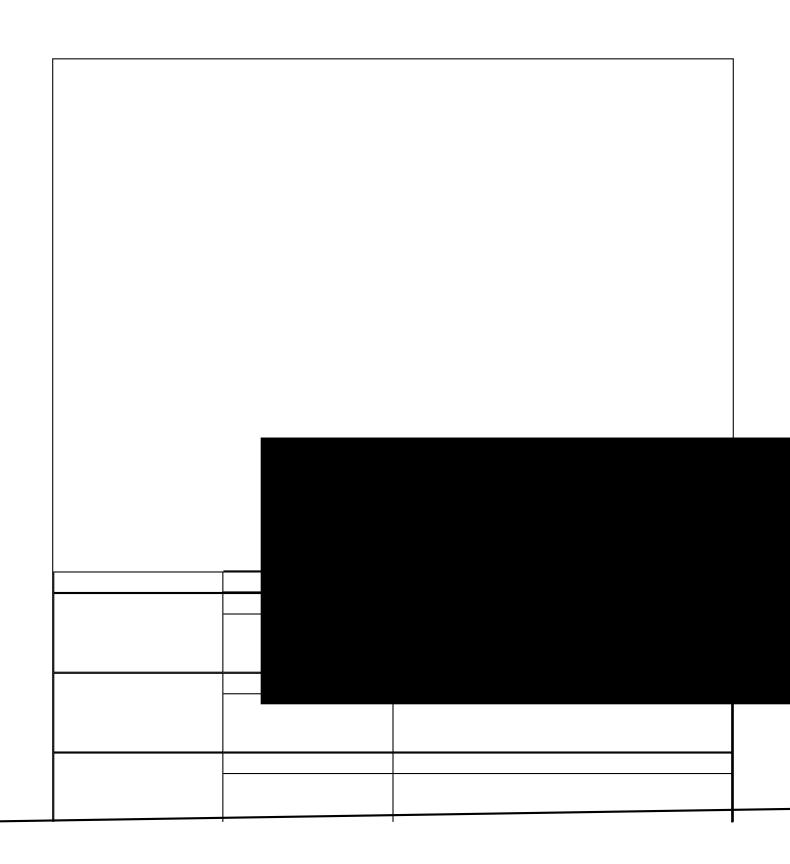
8YHJ]`g.

GY`YWfjcb`Zfca 'Uddfcl "'' \$']hYa g"

Gh XYbhg fYVV] j Y 'U 'bi a Yf]WJ `a Uf_ 'UbX Z ```gc `i h]cbg 'UbX 'U 'dfYdUfUhcfmih/gh'

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@ghYb]b['HYghg'k]``VY'\Y`X'Xi f]b['`YWh fYg'cf'h hcf]U`g'cf'gdYW]U``mUffUb[YX'h]a Yg'Ug']bX]WUhYX']b'h\YWci fgY'gW\YXi 'Y'h]a YhUV'Y"



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K YY_"%%"%\$"5i[igh!"%\$	5ggYgga Ybh	7cbhYbhf&)ı ŁUbX@]ghYb]b[f&)ı ŁhYghg&cZ&"
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FYWca a YbXYX FYgci fW/g

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Ghi XYbhgʻUfYʻYbWci fU[YX`hcʻdfcj]XYʻZYXVUW_`hcʻ]a dfcj Yʻh\YʻWci fgYʻcfʻVYhhYfa YYhh\YjfʻYl dYWhlhjcbg YUf'm]bʻh\YʻhYfa žʻgcʻh\Uhih\YfYʻ]gʻha Yʻhcʻ]a dʻYa YbhW\Ub[Ygʻk \YfYʻdcgg]V`Y"`Ga U```W\Ub[Ygʻ]bʻh\Y Wci fgYʻa UhYf]U``\UgʻVYYbʻa UXY`]bʻh\YʻdUghVUgYX`cbʻfY`Yj UbhžʻgdYWJU``]bhYfYghgʻfYdcfhYX`Vmghi XYbhg" Gi Va]gg]cb cZ5ggYgga YbhHUg_g Hi fb]h]b Gi Va]gg]cb

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"`±hWJb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UWW]XYbhJ``mWcdm]b['Zfca `U`gci fWY`k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
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Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci žch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWhg'cZ9@&9'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi V'YWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

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