

EDST5303

@YUfb]b[ž'DfcV`Ya 'Gc`j]b[ž'UbX'h\Y'8Yj Y`cda YbhcZ 9I dYfh]gY

GYa YghYf'Hk c''#'&\$%

7ci fgY'Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g`

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUh]cb	D\cbY
G`Uj U'? U`mi [U	5 - : 5		>c\b'; ccXgY``ž F cca '%)	-',) '%-,)

GWkcc`7cbhJWh =bZcfa Uhlcb

GW.cc``cZ9Xi WUhjcb 5fhg`UbX`GcWjU``GWjYbWYg

@Y|Y`'%z'>c\b'; ccXgY``'6i]`X]b['fl &\$Ł

H. 'Ž * %'f&Ł'-',) '%-++

9. YXi WUhjcb4 i bgk "YXi "Ui

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5 h Y b X U b W F Y e i] f Y a Y b h g

5XX]h]cbU`GWXcc`cZ'9Xi WUh]cb'UhhYbXUbWY'fYei]fYa Ybhq

#i]gYl dYWYX'h\UhUbmghi XYbhYbfc``YX']b'Ub'98GH'Wci fgY'k]h\Y'GW\cc``cZ9Xi WUhjcb'k]``a U_Y'U Wca a]ha Ybhhc'h\Y]f``YUfb]b['UbX'UhYbX'U```WUggYg']b'Z ```k\YfY'WcbhYbh]g'XY`]j YfYX']b'U'ZJWY!hc!ZJWY a cXY'Yl WYdh]b'WjfW a ghUbWYg'k\YfY'UVgYbW']g'Xi Y'hc']``bYggža]gUXj Ybhi fY'cf'i bZcfYgYYb WjfW a ghUbWYg'VYmcbX'h\Y'ghi XYbhg'Wcbhfc`'''5'a]b]a i a 'UhhYbXUbWY'fYei]fYa YbhcZ, \$i ']g'fYei]fYX'Zcf YUW\'Wci fgY'''-\D'WftU]b'WjfW a ghUbWYgž'U'ghi XYbha Uma]gg'i d'hc'&\$i 'cZU'Wci fgY'k]h\ci h\Zcfa U` U'Udd']WUhjcb'UbX'i d'hc'' 'i 'cZU'Wci fgY'k]h\'Zcfa U``XcW a YbhUhjcb'fgYbhj]U'Ya U]`'hc 'Wci fgY'Wcbj Ybcfb'dfcj]X]b['U``h\Y'fYei]fYa Ybhg'XYhU]YX'VY`ck 'UfY'a Yh'''Ghi XYbhg'bcha YYhjb['h\Y'UhhYbXUbW'fYei]fYa Ybhg'ci h]bYX'UVcj Y'k]```VY'Uk UfXYX'Ub'I bgUhjgZUWcfm: U]`'fl : b'Zcf'h\UhWci fgY'fY[UfX`Ygg'cZ h\Y]f'dYfZcfa UbW']b'h\Y'UggYgga YbhhUg_g'cf'ch\Yf'fYei]fYa Ybhg'Zcf'h\Y'Wci fgY''

: cfiZ fh\Yfi]bZcfa Uhjcbicbi9Xi WUhjcbiWci fgYiUhhYbXUbWYifYei]fYa YbhgžidiYUgYifYZYfihcih\YifYgdYWhji Y 98GHiA ccXiYia cXi `Yfgt"

5 WUXYa 1W = DZcfa Uhlcb.

cf'YggYbhjU`ghi XYbhjbzcfa Uhjcb'fY`Uhjb['hc.'fYei Yghg'zcf'Yl hYbg]cb/fYj]Yk 'cZa Uf_g/cWW dUhjcbU``\YU`h\ UbX'gUZYhm'Yl Ua]bUhjcb'dfcWYXi fYg/gdYWjU``Wcbg]XYfUhjcb']b'h\Y'Yj YbhcZ]``bYgg'cf'a]gUXj Ybhi fY/ghi XYbhYei]hmUbX'X]gUV]`]hm'UbX'ch\Yf'YggYbhjU``UWUXYa]W]bZcfa Uhjcbž aYY`\hdg.##k k k "Ufha"i bak "YXi "Ui #W ffYbhahi XYbha#JWUXYa]W]bZcfa Uhjcb#dfchcWc`a![i]XY`]bYa#

7ci fgY 8YHJ] g

7 fYX]hDc]bhg**

K cf_`cUX

%) \$`\ci fg`]bWi X]b[`WUgg`WcbHJWi\ci fgž`fYUX]b[gž`WUgg`dfYdUfUh]cbž`UggYgga Ybhž`Zc``ck`i d`UWhj]hjYgž YHVI

Gi a a UfmcZh\Y 7ci fgY

H\Y'a U'cf'ZcW g'cZh\]g'Wci fgY']g'hc'Yl Ua]bY'\ck '\i a Ub'Wc[b]h]j Y'ghfi Wh fYg'UfY'cf[Ub]gYX']bhc'U Wc\YfYbh'UfW\]hYWh fY'YbUV']b['mci 'hc''YUfbž'h\]b ž'fYUgcb'UbX'gc'j Y'dfcV'Ya g'''H\Y'WbhfU''fc'Y'd'UmYX'Vm UWhj Y''YUfb]b[']b'h\]a'UfW\]hYWh fY']g'Ya d\Ua]gYX'''H\Y'Wci fgY'Yl Ua]bYg'\ck 'Yl dYfh]aY'XYj Y'cdg'UbX

5i ghfu`]Ub DfcZYgg]cbU`; fUXi UhY HYUWX]b[GhUbXUfXg

GhubXUfX	8 Y g Wf] d h] c b
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%"&"'	9IdUbX`ibXYfgHJbX]b[`cZ\ck`ghXYbhg``YUfb`ig]b[`fYgYUfW\`UbX`kcf_d`UWf_bck`YX[Y"
%") "&	8 Yj Y`cd'HYUW.]b['UWHjj]HjYg'H\Uh]bWcfdcfUHY'X]ZZYfYbHjUHYX'gHfUHY[]Yg'Hc'a YYhH\Y gdYWJZJW`YUfb]b['bYYXg'cZgH XYbHg'UWfcgg'H\Y'Z ```fUb[Y'cZUV]`]HjYg"

5ggYgga Ybh

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5ggYgga Ybh'hUg_	K Y][\h	GH XYbh@YUfb]b[CihWcaYg 5ggYggYX	5 ≠IG@`DfcZYgg]cbU`; fUXi UHY HYUWX]b['GHJbXUfXg'5ggYggYX	8iY 8UhY
A U⁄cfYggUmi) \$1	&Ž Ž(Ž)	%") "&	&* #%\$#& \$% \$) .\$\$ DA
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 $\label{eq:continuity} D`YUgY`fYZYf`hc`3gefcS`fS`BcaXWee[a`S^EfS`VSdVeXadFWSUZWce'cb'h\Y'dfYj]cig'dU[Y]$

5ggYgga Ybh'8YhJ]`g

5ggYgga Ybh% A U⁄cfYggUm

GhUfhXUhY. Bch5dd`]WUVY

 $\textbf{8YHJ} \texttt{`g.'K} \texttt{ f]} \texttt{h'.'Ub.'YggUmVUgYX.'cb.'h.Y.'a} \texttt{ UhYf]} \texttt{U`.'Wcj. YfYX.']} \texttt{b'.'h.Y.'Wci} \texttt{ fgY'.Zc.W'} \texttt{ g]} \texttt{b['.cb.']} \texttt{hg.'Udd.']} \texttt{wUhJcb.'hc} \texttt{b'.'h.Y.'wci} \texttt{ fgY'.Zc.W'} \texttt{ g]} \texttt{b['.cb.']} \texttt{hg.'Udd.']} \texttt{wUhJcb.'hc} \texttt{b'.'h.Y.'wci} \texttt{ fgY'.Zc.W'} \texttt{ g]} \texttt{b['.cb.']} \texttt{hg.'Udd.']} \texttt{wUhJcb.'hc} \texttt{b'.'h.Y.'wci} \texttt{ fgY'.Zc.W'} \texttt{ g]} \texttt{b['.cb.']} \texttt{hg.'Udd.']} \texttt{wUhJcb.'hc} \texttt{b'.'hc} \texttt{ fgY'.Zc.W'} \texttt{ g}} \texttt{ fg.'hc} \texttt{ fg.$

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GhUfh XUhY.

8 YHJ]`g. '5 '&\$`]hYa 'a i `h]d`Y`W\c]\W'`hYghcb`\i a Ub`\\c[b]h]j Y`Uf\W\]hY\\n fY"H]a Y. '&\$`a]bi hYgGhi XYbhg`k]`` fY\\n"]j Y`ZYYXVU_`k]h\ '\%`Vi g]bYgg`XUmg`cZgi Va]gg]cb"

5XX]h]cbU`XYhJ]`g.

`=b!WUgg'a i `hjd`Y!VXc]WY`hYghf&\$`]hYa gŁ`cb`a U'cf`Wca dcbYbhg`UbX`dfcWYggYg`cZ\i a Ub`Wc[b]hjj Y

GdYWJZJW7 f]hYf]U	"f!Ł	– 2fŽŁ

@YWhifYf

"B6. h\]g'h\\g']b'h\Y'j Uf]ci g'Vcl Yg'UbX'XYg][bYX'bc'dfcj]XY'ZYYXVUW_bc'gh XYbhg/h\Ym'UfY'bch[]j Yb Yei U``k Y][\h']b'XYhYfa]b]b['h\Y'fYWca a YbXYX'[fUXY"8YdYbX]b['cb'h\Y'bUh fY'cZ'h\Y'UggYgga Ybh'H\g_ž YWh fYfg'a Um'U`gc'WcbhYl hi U`]nY'UbX#cf'Ua YbX'h\YgY'gdYWJZWWf]hYf]U""H\Y'fYWca a YbXYX'[fUXY']g hYbh'hhj Y'cb`mžgi Va YWh'bc'gh'bXUfX]gUhjcb'dfcWYggYg'UbX'Uddfcj U``Vmh\Y'GW\cc``cZ'9Xi WUhjcb@YUfb]b['UbX'HYUW\]b['7ca a]hhYY"

I BGK 'G7<CC@'C: '98I 75H€B'FI 6F = 7 # 998657? 'G<99H' 98GH)' \$'

5ggYgga YbhHUg_. 7`Ugg dfYgYbhUh]cb

GdYWJZJW7 f]HYf]U	···flŁ	 2fŽŁ
I bXYfgHUbX`cZ`h\Y`ei Ygh]cb`cf`]ggi Y`UbX`h\Y`_YmWcbWYdhg]bj c`j YX		
8Ydh\cZUbUmg]g`UbX#cf`Wf]heiY`]b`fYgdcbgY`hc`h\Y`hUg_		
: Ua]`]Uf]hmk]h\ 'UbX`fY`Yj bWY`cZ'dfcZYgg]cbU``UbX#cf`fYgYUfVX `]hYfUh fY`i gYX`hc`gi ddcfhfYgdcbgY		
GHfi Whi fY'UbX'cf[Ub]nUh]cb'cZfYgdcb		
DfYgYbHJhjcb`cZfYg <mark>gc</mark> bgy www.fxjb[`hc`Uddfcdf]UhY`UWUXYa]WUbX `]b[i]ghjWWcbjYBhjobg		
; YbYfU``Wcaa Ybhg#YWcaa YbXUh]cbgʻZcfʻbYl h'h]a Y.ʻ		

@YWhi fYf

FYWcaa YbXYX. '''#&\$'f!@'DG'7F'8B'<8E' k Y][\h]b['.'&\$i

"B6. h\]g'h\Wg']b'h\Y'j Uf]ci g'Vcl Yg'UbX'XYg][bYX'hc'dfcj]XY'ZYYXVUW_hc'ghi XYbhg/h\YmUfY'bch[]j Yb
Yei U`k Y][\h]b'XYhYfa]b]b['h\Y'fYWca a YbXYX'[fUXY"8YdYbX]b['cb'h\Y'bUhi fY'cZh\Y'UggYgga YbhHUg_ž
'YWhi fYfg'a Um'U`gc'WcbhYl hi U`]nY'UbX#cf'Ua YbX'h\YgY'gdYV]ZJWWf]hYf]U"''H\Y'fYWca a YbXYX'[fUXY']g
hYbhUh]j Y'cb`mžgi Va 'YWh'nc'ghUbXUfX]gUh]cb'dfcWyggYg'UbX'Uddfcj U`'Vmh\Y'GW\cc`'cZ'9Xi WUh]cb
@YUfb]b['UbX'HYUW\]b['7ca a]hhYY"

I BGK 'G7<CC@'C: '98I 75H€B'FI 6F = 7 # 998657? 'G<99H' 98GH)' \$'

5ggYgga Ybh'HUg_. '7`Ugg'hYgh

¨flŁ—	 	 2fŽŁ

@YWhi fYf

F YWca a YbXYX. ' '''#&\$'fl @'DG'7F'8B'<8Ł' k Y][\h]b['.'&\$i

"B6. h\]g'h\Wg']b'h\Y'j Uf]ci g'Vcl Yg'UbX'XYg][bYX'hc'dfcj]XY'ZYYXVUW_hc'ghi XYbhg/h\YmUfY'bch[]j Yb
Yei U`k Y][\h]b'XYhYfa]b]b['h\Y'fYWca a YbXYX'[fUXY"8YdYbX]b['cb'h\Y'bUhi fY'cZh\Y'UggYgga YbhHUg_ž
'YWhi fYfg'a Um'U`gc'WcbhYl hi U`]nY'UbX#cf'Ua YbX'h\YgY'gdYV]ZJWWf]hYf]U"''H\Y'fYWca a YbXYX'[fUXY']g
hYbhUh]j Y'cb`mžgi Va 'YWh'nc'ghUbXUfX]gUh]cb'dfcWyggYg'UbX'Uddfcj U`'Vmh\Y'GW\cc`'cZ'9Xi WUh]cb
@YUfb]b['UbX'HYUW\]b['7ca a]hhYY"

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

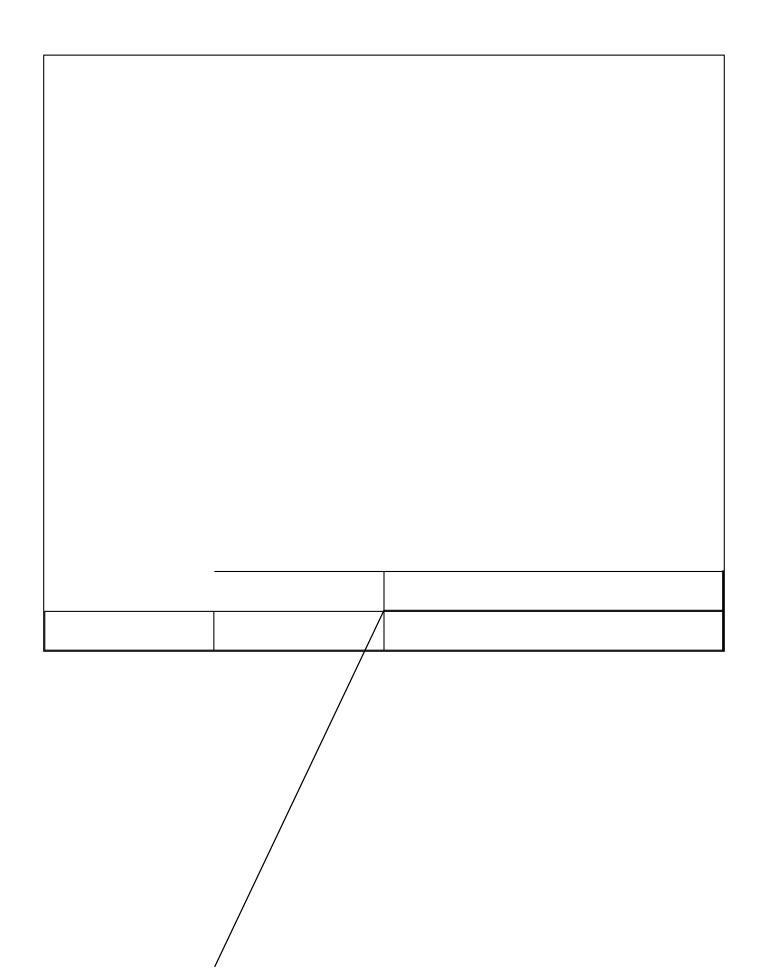
 $Gh\ XYbhg\ 'UfY\ 'YI\ dYWhYX\ 'hc\ 'di\ hh\ Y]f\ 'bUa\ Yg\ 'UbX\ 'gh\ XYbhbi\ a\ VYfg\ 'cb\ 'Yj\ YfmdU[\ Y\ 'cZh\ Y]f\ 'Ugg][\ ba\ Ybhg\ ''$

Hi fb]h]b Gi Va]gg]cb

 $\bullet \ \ \, \text{K cf_'gi Va]} \\ \text{lh} \\ \text{X '\%' hc '\% 'XUmg 'UZhYf' h\ Y 'gh]} \\ \text{di ``UhYX 'XYUX`]} \\ \text{bY } \\$

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWfg'cZ9@ ${\mathfrak G}$ 9'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "f\hd.#gi V\YWfi \\X\yg''\YfUfm'i bgk\\"YXi\\"Ui\#\`\]qY\#JVci \\Y\\]qY\\



FYgci fW/g

DfYgWf]VYX F Ygci fWYg

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HYI Wcc_`XYHJ]`g. `H\YfY`UfY`bc`gYhHYI Wcc_g`Zcf`t\]g`Wci fgYž'U`t\ci [\`t\Y`Zc``ck]b[`k]```VY`ZfYei Ybhm fYZYffYX`tc.

7`Uf_žF"B[i mYbž "ž'/ 'Gk Y``Yfž'>" 'f&\$\$*\L''`7 X\[U[W Uk [` >WSd [` Y\z'GUb': fUb\W]g\Wc.'>c\b'K]`Ym'/ 'Gcbg\z' \\
\(\daggreen \)

 $A \ UmYf \ Z^F \ "^9" f \& \$\$, \ L''> W \ L'' > W \ L'$

GkY`Yfž'>"ž'5mfYgž'D"/ '?U`mi [Už'G"'f&\$%%£"'5aY` [f[hW^aSV fZWack"'BYk 'Mcf_, 'Gdf]b[Yf"

FYWca a YbXYX FYgci fWyg

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