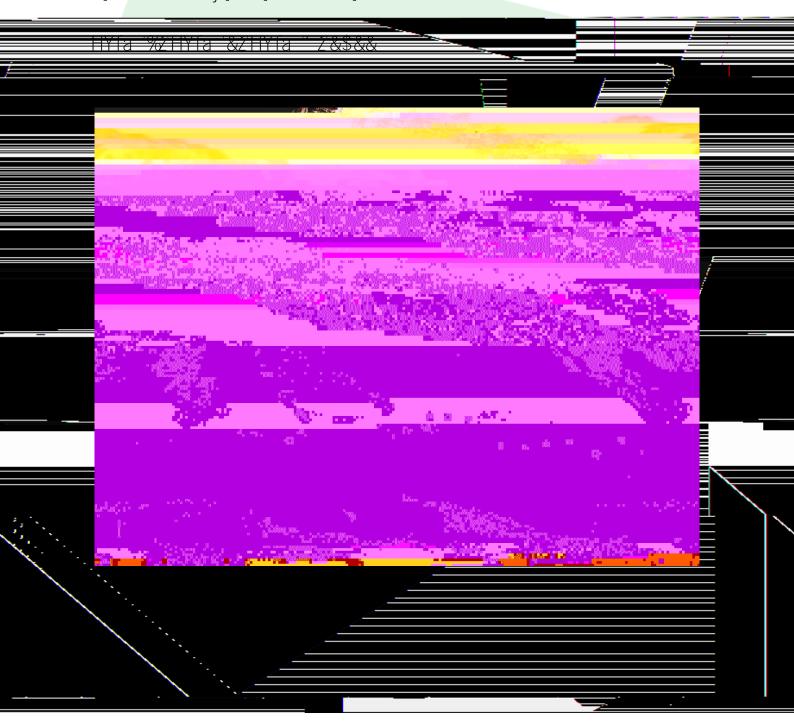


EDST5457

@]hYfUh fY`FYj]Yk`]b`9XiWUh]cb



7ci fgY⁻Cj Yfj]Yk

GHJZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]m	@cWUh]cb	D\cbY
F]WXUfX ⁻ B]YgWXY	f"b]YgWXY4 i bgk "YXi "Ui	9a U]`Zcf'Ub Uddc]bha Ybh	; %* A cfj Yb 6fck b	f\$&Ł'-\$*) %*&&

GWXcc``7cbHJWh'±bZcfa Uh]cb

GW.cc`cZ9Xi WJhcb

 $5 fhg \dot{z} 8 Yg][b Ub X 5 fW]h W f fY$

; fci bX': `ccfž'A cfj Yb '6fck b '6i]`X]b['fi &\$Ł

H. $^{'}$ Ž * % $^{'}$ f&Ł $^{'}$ - $^{'}$,) $^{'}$ % ++

9. YXi WUhcb4 i bgk "YXi "Ui

K. `\hdg.#kkk"Ufhg"i bgk"YXi "Ui #YXi WUhjcb

5W_bck `YX[Ya YbhcZ7ci bhfm

 $\label{eq:localized-loca$

7ci fgY 8YHJ] g

I b]hg cZ7fYX]h * *

K cf_`cUX

%) \$`\ci fg`]bWi X]b[`WUgg`WcbHUWh\ci fgž`fYUX]b[gž`WUgg`dfYdUfUh]cbž'UggYgga Ybhž'Zc``ck 'i d`UWh]j]h]Ygž YhW

Gi a a UfmcZh\Y 7ci fgY

H\]g`WcifgY`dfcj]XYg`mci k]h\`Ub`cddcfhib]mhc`WcbXi WhUb`]b!XYdh\`fYj]Yk`cZh\Y``]hYfUhifY`cb`U`hcd]WcZ]bhYfYghz`cf`]ggiY`fY`UhYX`hc`YXi WUh]cb"'=hk]```YbUV`Y`mci hc`XYjY`cd`U`XYYdYf`fYZYWhjY`UddfcUW\`hc YXi WUh]cb`UbX`dfcj]XY`U`Zci bXUh]cb`]b`k cf_]b[`Ui hcbca ci g`mk]h\`[i]XUbW\`Zfca `Ub`U\WXYa]W gi dYfj]gcf"

7ci fgY @YUfb]b[Ci hWca Yg

- %" 7 f]h]WU``mYb[U[Y`]b`U`gWkc`Uf`m]bei]fmicZfY`Yj UbhhkYcfmiUbX`fYgYUfWk``]hYfUhi fY`fY`UhYX`hc`U`hcd]W cZ]bhYfYghžcf`]ggi Y`]b`YXi WUh]cb"
- &" @cWUHY`UbX`Wf]h]WU``mfYj]Yk 'H\YcfmUbX`fYgYUfW\`]b'H\Y``]HYfUHi fY`fY`UHYX`hc`U`hcd]WcZ]bHYfYgHz`cf |aqi Y`]b`YXi WUHcb"
- '" I gY 'Uddfcdf]UhY 'ghfi Whi fYž'cf[Ub]gUh]cb 'UbX'k f]h]b['ghm`Y 'Zcf'U``]hYfUhi fY 'fYj]Yk 'cb 'U'hcd]WcZ]bhYfYghž'cf']ggi Y`]b 'YXi WUh]cb"

HYUWX]b[GhfUhY[]Yg

FUNcbU'Y.

H\]g`Wci fgY`]g`VY]b[`cZYfYX`hc`dfcj]XY`ghi XYbhg`k]h\`Ub`cddcfhi b]hmhc`i bXYffU_Y``]hYfUhi fY`fYj]Yk`]b`U gdYW]ZWUfYU`cZYXi WUh]cb`cZh\Y]f`W\c]WY"'H\Y`Wci fgY`k]``U`gc`YbUV`Y`ghi XYbhg`hc`XYj Y`cd`U`XYYdYf fYZYWfj Y`UddfcUW\`hc`YXi WUh]cb`UbX`[]j Y`h\Ya`U`Zci bXUh]cb`]b`k cf_]b[`Ui hcbca ci g`mk]h\`[i]XUbWY Zfca `Ub`UWUXYa]Wgi dYfj]qcf"

HYUW]b[Ghfuh / [] Yg.

 $\label{thm:continuous} $$H\Y'Wci fgY'k]^{``jb]hJU`mi gY'Yl d`]Whjbghfi Whjcb`XYg][bYX'hc'ghja i `UhY'ghi XYbhh\h]b_]b['VYWUi gY'h\YfY'UfY'Ubi a VYf`cZ]ggi Yg'h\Uhghi XYbhg'k]``bYYX'hc'UXXfYgg'gc'h\Uhh\Y'fYj]Yk 'cZ`]hYfUhi fY'WUb'VYWca Y dfUWhJWUV'Y'UbX'ZYUg]V`Y'UbX'U`gcž'[fci d`X]gWi gg]cb'UbX'UWhjj]hJYg'XYg][bYX'hc']bWfYUgY'h\Y'WUdUW]hm'UbX WUdUV]`]hmcZghi XYbhg'Zcf'WcbXi Whjb['U``]hYfUhi fY'fYj]Yk'''$

5ggYgga Ybh

5ggYgga Ybh'tUg_	K Y][\h	8iY'8UHY	7 ci fgY @YUfb]b[Ci hWca Yg 5ggYggYX
%"`@]hYfUhifY`fYj]Yk	%\$\$ı	Bch5dd`]WUV`Y	%ž`&ž`'

5ggYgga Ybh% @]hYfUh fY fYj]Yk

HUg_'%

DUfhi5" DfcdcgU`

@Yb[h\.'%\$\$\$'k cfXg

 $H\g^dUfhcZhY'hUg_']g'U'YfdU]V'fYei]fYaYbh'$

: cfa Uhji Y ZYYXVUW_dfcj]XYX cb`]bY h\fci [\AccX`Y cb h\Y Wci fgY k YVg]hY k]h\]b '% XUmg cZgi Va]gg]cb"

DUfhi6. @hYfUhi fY fYj]Yk

@Yb[h\.') \$\$\$'k cfXg

 $\label{eq:continuity} Ei U`]hUh]j Y`UbX`ei Ubh]hUh]j Y`ZYYXVUW_`dfcj]XYX`cb`]bY`h\fci [\ \ A ccX`Y`cb`h\Y`Wci fgY`k YVg]hY`k]h\]b`%$ XUmg`cZgi Va gg]cb"$

5XX]h]cbU`XYhU]`g

DUfh'5. DfcdcgU`

Mci f'HJg_']g'hc'k f]hY'U'%\$\$\$!k cfX``]hYfUh fY'fYj]Yk 'dfcdcgU`"

 $HY'dfcdcgU''g\ci `X']bWi XY'h\Y'Zc``ck]b[.$

%" 5b'Uddfcdf]UhY'h|hY"

&" ⇒XYbhjZjWUhjcb cZh\Y hcd]W"

 $' "9ghUV]g\h Y]a dcfhUbW cZhcd]W$

("8YZbY'_Ym'hYfag"

) " 8 YgWf]VY ``]hYfUhi fY 'gYUfW\ 'ghfUhY[]Yg"

*"8YgWf]VY:YI hYbhUbX:bUh fY:cZh\Y:`]hYfUh fYfW\:ghfUhY[]Yg"

%" 5b`Uddfcdf]UhY`h]hY`—`a UhWkYg`k \Uhimci f``]hYfUhi fY`fYj]Yk `]g`UVci h'
&" ±bhfcXi Wh]cb`—`gYhg`WcbhYl hžYl d`U]bg`k \Uhik]```VY`fYj]Yk YX`UbX`k \m]hik]```VY`fYj]Yk YX"
' " 6cXm—`Wf]h]WU``X]gW gg]cb`cZ_YmfYgYUfWk`UbX`Z]bX]b[g`UbX`]XYbh]Z]WUh]cb`cZ[Udg`]b`h\Y``]hYfUhi fY"
(" 7 cbWi g]cbgžX]fYWh]cbg`Zcf`fYgYUfWkž]a d`]WUh]cbg`Zcf`dfUWh]VW"
) " 5D5`ghmY`Zcf`W]hUh]cb`UbX`fYZYfYbW]b["

FI 6F = 7 # 998657? G < 99H 98GH)()+ @ + 19F5HIF9F9J = 9K = 18 98 I 75H € B IBGK G7 < CC@C: 98 I 75H € B

5ggYgga Ybh'HUg_'% @jhYfUhi fY'fYj]Yk

GdYW] ZJW7 f]HYf]U	··f	flŁ———	2	2fŽŁ

5 hhyb XUb WY F Yei]fYa Ybhg

GWki]]XUbWYFYei]fYa Ybhg

FYgci fWYg

DfYgWf]VYX F Ygci fWYg

 $\label{eq:constraint} D`YUgY`gYY`th\Y`Wci fgY`A ccX`Y`g]tY`Zcf`Ugg][bYX`fYUX]b[`a UtYf]U`"$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwci bhYf'U'dfcV'Ya k \Yb'UhYa dhJb['hc'gi Va]hmci f'Ugg][ba Ybht\fci [\'Hi fb]hJbž'd'YUgY

HY'Yd\cbY'9| hYfbU'`Gi ddcfhcb'-',) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUfŁ"'=Imci
UfY'i bUV'Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\'Hi fb]hJb'mci 'a UmUdd'mZcf'Ub'Y! hYbg]cbž'Vi hmci
a i ghfYhJ]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU'`Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY'Yj UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd']WUhJcb"'=Imci 'Ya U]`'9! hYfbU'`Gi ddcfhmci 'k]``
Ui hca UhJWJ'`mfYWY]j Y'U'hJW_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYWJZJWJ'`mUg_'Zcf'cbY"
Hi fb]hJb'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hYf"

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

: cf']b \mathbb{Z} cfa Uh]cb'cb'\ck 'hc'gi Va]h'Ugg][ba Ybhg'cb`]bY'j]U'A ccX`Y. `\hhdg.##gh XYbh'i bgk "YXi "Ui \mathbb{A} ck! qi Va]h'Ugq][ba Ybha ccX`Y

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"`=hWJb`hJ_Y`a Ubm Zcfa gžZca `XY`]VYfUhY`W\YUh]b['hc`UVW]XYbhJ``mWcdm]b['Zfca `U`gci fWY`k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidgdu[]Uf]ga]bhch\YZc``ck]b[WUhY[cf]Yg.

 $\begin{tabular}{ll} \hline \textbf{7.cdm}b[...] g]b[...] MY cf'j Yfmg]a] ``Uf'k cfXg'hc'h\Y'cf][] bU``HYI hcf']XYU'k]h\ci h`U\W_bck ``YX[]b[...] b[...] MY cf'i g]b[...] bU``HYI hcf']XYU'k]h\ci h`U\W_bck ``YX[]b[...] b[...] MY cf'i g]b[...] a UhYf]U`gž']XYUg'cf'WcbW'dhg'\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]WY\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '`U'Vcc_\bar{Z}Ufh]\bar{Z}ca '``U'Vcc_\bar{Z}Ufh]\bar{Z}ca '``U'Vcc_\bar{Z}Ufh]\bar{Z}ca '``U'Vcc_\bar{Z}Ufh]\bar{Z}Ufh]\bar{Z}Ufh]\bar{Z}ca '``U'Vcc_\bar{Z}Ufh]\bar{Z}U$

5 WUXYa]W = b Zcfa Uh cb

8 i Y'hc'Yj c'j]b['UXj]WY'VmBGK '<YU'h\ž'ghi XYbhg'a i gh\W\Y_'Zcf'i dXUh\Y\']bZcfa Uh]cb'fY[UfX]b['cb`]bY 'YUfb]b['Zcf'U``'5fhgž'8Yg][b'UbX'5f\W]h\Y\Mi fY'\\chi fgYg'h\]g'h\fa 'fJ]U'A ccX'Y'cf'\\chi fgY']bZcfa Uh]cb dfcj]XYX"Ł

: cf'YggYbh]U`gh XYbh]bZcfa Uh]cb fY`Uh]b[hc.

- fYei Yghg 'Zcf'Yl hYbg]cb/
- `UhY`gi Va]gg]cbg`[i]XY`]bYg/
- fYj]Yk 'cZa Uf_g/
- I BGK '< YU`h\ 'UbX'GUZYhm'dc`]\\\Yg/
- YI Ua]bUhcb dfcWXi fYg/
- gdYWJU``Wcbg]XYfUhJcb']b'h\Y'Yj YbhcZ]``bYgg'cf'a]gUXj Ybh fY/
- gh XYbhYei]mUbX X]gUV]`]m/
- UbX'ch\Yf'YggYbhJU`'UWUXYa]W]bZcfa UhJcbž'gYY

 $\label{thm:continuous} $$ \hdg.\#k\ k\ ''i\ bgk\ ''YXi\ ''Ui\ \#Uffg!XYg][\ b!\ UffW.\]hYWi\ fY\#gh\ XYbh`]ZY\#Ygci\ fWYg!gi\ ddcfh\#dfchcWc`g![\ i\]XY`]bYg $$ $$ \hdg.\#k\ k\ k\ ''i\ bgk\ ''YXi\ ''Ui\ \#Uffg!XYg][\ b!\ UffW.\]hYWi\ fY\#gh\ XYbh`]ZY\#fYgci\ fWYg!gi\ ddcfh\#dfchcWc`g![\ i\]XY`]bYg $$ \hdg.\#k\ k\ k\ ''i\ bgk\ ''YXi\ ''Ui\ #Uffg!XYg][\ b!\ UffW.\]hYWi\ fY\#gh\ XYbh`]ZY\#fYgci\ fWYg!gi\ ddcfh#dfchcWc`g![\ i\]XY`]bYg $$ \hdg.\]$

.

a U[Y'7fYX]h

GmbYf[]Yg^]b^GcibX^&\$%*

7F = 7CG