

# **ARTS3455**

7 cbhYa dcfUfm7 \]bYgY @]hYfUhi fY

HYfa 'C bY''##'&\$%

# 7ci fgY<sup>·</sup>Cj Yfj ]Yk

# ·GHUZZ:7cbHUWh:8YHJ]`g

'7cbj Ybcfg'

BUa Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWUh]cb	
_				

a

**%** 

7 ci fgY 8 YHJ]`g 7 fYX]hDc]bhg \*\* Gi a a UfmcZh\Y 7 ci fgY

Gi VYWh5fYU.

## 5ggYgga Ybh

#### 5ggYgga YbhHUg\_g

5ggYgga Ybh'hJg_	K Y][\h	8i Y'8UHY	Gh XYbh@YUfb]b[ Ci hWca Yg 5ggYggYX
A U'cf'9ggUm	) \$1	&(#\$(#&\$%-`%%\$\$`DA	%ž&Ž Ž(
±bX]j ]Xi U``dfYgYbfUf]cb`]b h\Ya YX`[ fci d`gYff]b[ `	' \$1	: fca 'k YY_'' 'hc'k YY_',	%ž&Ž Ž(
±b!WUgg"hYgh"	&\$ı	&(#\$(#&\$%-'%&.&\$`DA	%ž&Ž

#### 5ggYgga Ybh'8YhJ]`g

5ggYgga Ybh% A U'cf 9ggUm

GhUfhXUhY. Bch5dd`]WUV`Y

**8YHJ]`g**. `Ghi XYbhg`k f]hY`Ub`YggUmf\\\\\J"` ž) \$\$!(\$\$\$`k cfXg\!\VUgYX`cb`]bXYdYbXYbhifYgYUf\\\\\": YYXVU\\\\_`j ]U\\]bX]j ]Xi U``\\cappa a Ybhg`UbX`fi Vf]\\\\\]g`]g`h\Y`Z]bU``UggYgga YbhZcf`UhY\bXUb\\\'di fdcgYg''

 $\label{eq:higher} \textbf{Hi fb]hjb'gYhjb[.'H\]g'Ugg][ba Ybh']g'gi Va ]hhYX'h\fci [\''Hi fb]hjb'UbX'ghi XYbhg'WUb'gYY'Hi fb]hjb'g]a ]`Uf]hm fYdcfhg''$ 

5ggYgga Ybh& ±bX]j ]Xi U dfYgYbhUh]cb ]b h\Ya YX [fci d gYhh]b[

GhUfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g. `Ghi XYbhg`dfYgYbhifUbX`UfY`a Uf\_YXŁ`]bX]j ]Xi U``mifl%\$`a ]bi hYg`YUWXŁcb`U`WkcgYb`hcd]Wk ]h\]b`h\Y ZfUa Yk cf\_cZ`U`h\Ya YX`[ fci d"`H\Y`hcd]Wg`UfY`VUgYX`cb`Ugg][ bYX`fYUX]b[ g"`Ghi XYbhg`UfY`cf[ Ub]nYX`]bhc [ fci dg`k ]h\`U`g\UfYX`h\Ya Yž'h\Y]f`]bX]j ]Xi U``dfYgYbhUf]cbg`XYU``k ]h\`U`X]ZZYfYbhUgdYWicZh\Y`h\Ya Y" : YYXVUW\_j ]U`]bX]j ]Xi U``Wca a Ybhg"

Hi fb]hjb gYhjb[. H\]g ]g bchU Hi fb]hjb Ugg][ ba Ybh

5ggYgga Ybh' ±b!WUgg hYgh

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\. '&'\ci fq

**8YHJ]`g.** `Ghi XYbhg`Wca d`YhY`U`hYghifWJ"`&`\ci fgŁ`]bWi X]b[ `a i `h]d`Y!W.c]WYžh\Yb`g\cfh`UbX``cb[ Yf!Ubgk Yf ei Ygh]cbg'`Ghi XYbhg`fYWY]j Y`U`a Uf\_'UbX`WJb`Wcbgi `hh\Y``YWhi fYf`Zcf`Zi fh\Yf`ZYXXVUW\_"

Hi fb]hjb gYhjb[. H\]g ]g bchU Hi fb]hjb Ugg][ ba Ybh

## 5 http://bxubww.F.Yei ]fYa Ybhg

5 hh/bXUbW/cZ@YWh fYg#Hi hcf]U`g`]g`a UbXUhcfmi]b`h\]g`Wci fgY"'I bYI W gYX`UVgYbW/Zfca `a cfY`h\Ub`&\$i cZ@YWh fYg#Hi hcf]U`g`k]``fYgi `h]b`h\Y`Uk UfX`U`ZU]``[ fUXY"

 $\\ \pm \text{``YWhi fY'UbX'hi hcf]U'g'mci'k ]```UWh]j Y'mYb[U[Y'k]h\'WcfY'Wci fgY'WcbhYbhz'YbUV']b['mci'hc'UhhU]b'7@C'\% UbX'7@C'&"$ 

# 7ci fgY GWX YXi `Y

#### J]Yk 'WUgg'ha YhUV'Y

#### H]a YtUV`Y

8 UhY	HmdY	7 cbhYbh
K YY_'%'% ': YVfi Ufm!'&( : YVfi Ufm	@YWhi fY	⇒blfcXi Wfjcb:!!'FZW5a`UWbfS`V: [efack aX? aVWd 5Z[`WeW>[fWdSfgdW
K YY_`&.`&) ': YVfi Ufm!'' A UfVX	@YWhi fY	= Wk 8[YgdNe S`V;eegWe aXS 5 Z[`WeW>[fWdSdk ? aVWd [fk, >g J g`- DWSV[`Ye, /: S`Vagfefž
	Hi hcf]U`	GYa]bUf. @ 'Lib'UbX'acXYfb'7\]bYgY'Z Wf]cb
K YY_" ."("A UfWX"!"%\$ A UfWX	@YWn fY	= Wk 8[YgdWe S`V;eegWe aXS 5Z[`WeW>[fWdSdk ? aVWd [fk, @W BaWfdkž DWSV[`Ye, 'fk UbXci hgŁ"
	Hi lcf]U`	EW_[Sd`W baWfok S`V_aVWd 5Z[S-efgVWfbdWeWfSf[a`e
K YY_'(.'%%'A UfWX'!'%+ A UfWX	@YWn fY	= Wk 8[YgdNe S`V;eegWe. LZS`Y 3[1] YžFYUX]b[g. fk UbXci fgŁ
	Hi hcf]U`	EW_ [ Sda` LZS`Y 3 [{ Y S`V _ aVWd 5 Z [ WeW XUf[a` - efgVW f bdWeW fSf[a` e
K YY_`).`% `A UfVX`!`&( A UfVX	@YWn fY	= Wk 8[YgdNe S`V;eegWe, G\Yb'7cb[kYb"FYUX]b[g. fk UbXci hgŁ
	Hi hcf]U`	GYa ]bUf`cb`G\Yb`7cb[kYb/ghXYbhdfYgYbhUh]cbg
K YY_'*.`&) `A UfVX`!`' % A UfVX	@YWhi fY	7 Sak S`V >SfWE a U[S1ef > [fWaSfgaW K Ub[ 'M Ub1]Ub/ K Ub[ 'A Yb[ "'F YUX]b[ g. 'E fgVk = [f, ' " "
	Hi lcf]U`	gYa]bUf'cb'9Uf'mUbX'@UHY'GcWJU']gh'@HYfUhifY/ ghiXYbhidfYgYbHUhJcbg
K YY_'+.'%'5df]`'!'+'5df]`	@YWhi fY	A fZWdi Ske aXi d[f[`Y 5 Z[`WeW_aVWd [fk S`V Z[efack, 6U]`L]Ubmcb[/7\Yb`M]bn\Yb"`F YUX]b[ g. E fgVk = [f, `"
	Hi lcf]U`	GYa ]bUf`cb`6U]`UbX`7\Yb/a cXYfb`7\]bYgY`\]ghcfmefgVW f bdWeW fSf[a`e
K_YY_', .', '5df]`!'%( '5df]`	@YWn fY	BaefŽeaU[S´[ef´[fWdSfgdW 4S[6SaWfS^ŽŽBaWfdkž DWSV[Ye, EfgVk=[f,
	Hi hcf]U`	GYa ]bUf`cb`dcghgcWJU`]gh7\]bYgY``]hYfUhi fYž'dcYhfmghi XYbhdfYgYbhUh]cbg

K_YY_''%)		BaefŽeaU[S´[ef´[fWdSfgdW A c´MUb´!!´:]Wf]cb" FYUX]b[g.' fk UbXci hgt"
		GYa ]bUf`cb`dcgHgcWjU`]gh7 \ ]bYgY``]hYfUh fYžZJWjcb/gh XYbhdfYgYbhUhjcbg"
K_YY_'%\$.`&&'5df]`'!`&, 5df]`	@YWhifY	±b WUggʻhYgh

# FYgci fW/g

### DfYgWf]VYX F Ygci fWYg

### HYI Mcc\_'8YM]`q

5FHG'()) '5a` fW\_ bacSck 5Z[` WeW>[fWcSfgdWEfgVk = [fl`Uj U]`UV`Y`Zfca 'I BGK '6cc\_'GhcfY/\
\UbXci hg`UbX`A ccX`Y`i d`cUXg

### FYWca a YbXYX FYgci fWyg

#### K YVg]hYg

: cf'h\Y'`]VfUfm'\hd.#k k k "`]VfUfm'i bgk "YXi "Ui #

: cf'h\Y'l BGK '@YUfb]b[ 'UbX'HYUW\]b[ 'l b]h '\htd.#k k k "`h "i bgk "YXi "Ui

Ufj UfX F YZYfYbW]b[ "GmgHYa . \\ \hdg. #ghi XYbh'i bgk "YXi "Ui #\Ufj UfX!fYZYfYbW]b[

### 7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

 $\label{eq:continuity} Gh XYbhZYXVUW\_g`UfY`HU\_Yb`]bhc`Wcbg]XYfUh]cb`]b`Wci fgYž`UggYgga Ybhg`UbX`XY`]j Yf]b[ `a Yh\cXgfYj ]g]cbg''$ 

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

Hi fb]h]b Gi Va ]gg]cb

Image: Ybwci bhYf'U'dfcV'Ya k \Yb'UhYa dhJb[ 'hc'gi Va ]hmci f'Ugg][ ba Ybht\fci [ \ 'Hi fb]hJbž'd'YUgY

HY'Yd\cbY'9| hYfbU''Gi ddcfhcb'-', ) '' ' ' %cf'Ya U] 'h\Ya 'cb'Y! hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'\\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-') .\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUfŁ" Image:

UfY'i bUV'Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\ 'Hi fb]hJb'mci 'a UmUdd'mZcf'Ub'Y! hYbg]cbž'Vi hmci
a i ghfYhJ]b'mci f'hJW\_Yhbi a VYf'Zfca '9! hYfbU''Gi ddcfhfU'cb[ 'k ]h\ 'Ubmch\Yf'fY'Yj UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj ]XYbW' 'hc'gi ddcfhmci f'Y! hYbg]cb'Udd']WUh]cb" Image: Ya U]''9! hYfbU''Gi ddcfhmci 'k ]''

Ui hca UhJWJ''mfYW'] Y'U'hJW\_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k ]'''bYYX'hc'gdYWJZWJ''mUg\_'Zcf'cbY"

Hi fb]hJb'U'gc'dfcj ]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk ]hYf"

; YbYfU``mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\W)``mj ]U'Y]h\Yf'Hi fb]hjb'cf'U'A ccX`Y Ugg][ ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]``'VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k ]h\ U`hYfbUhj Y'gi Va ]gg]cb'XYHJ]`g''

cfi]bZcfa Uh]cbicbi\ckihcigi Va ]hUgg][ ba Ybhgicbi]bYij ]UiA ccXiY.i\hdg.#gh XYbh'i bgk "YXi "Ui #\ck! qi Va ]hUgq][ ba Ybha ccXiY

#### 5 WUXYa | W < cbYghmUbX D`U[ | Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU\_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUiqci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b[ 'WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW\_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf\_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b[ 'U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b[ 'h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k ]h\ci hUW\_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k ]h\ci hWfYX]hUbX'hc d]YW]b[ 'hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b[ "

7 c``i g]cb. 'k cf\_]b[ 'k ]th 'cth Yfg'Vi hidUgg]b[ 'cZZth Y 'k cf\_'Ug'U'dYfgcb'g']bX]j ]Xi U``k cf\_"'7 c``i g]cb'U`gc ]bWi XYg'dfcj ]X]b[ 'mci f'k cf\_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUHYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfglUbX`mci f`f][\hg`UbX`fYgdcbg]V]`]h]Yg`Ug`U`gh XYbh'Uhi BGK
- VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hzil BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5WWdhUV`Y'I gY'cZ I BGK '= H'F Ygci fWfg'Dc`]Wh
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWhYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wcaaib]hm
- `cWUHY 'gYfj ]WYg'UbX `]bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

# 5 WUXYa ]W = DZcfa Uhjcb

: cf`YggYbhJU``gh XYbh]bZcfa UhJcb`fY`UhJb[ 'hc.

fYei YghgʻZcfʻYl hYbg]cb/ `UhYʻgi Va ]gg]cbgʻ[ i ]XY`]bYg/ fYj ]Yk ʻcZa Uf\_g/ I BGK ʻ< YUʻh\ 'UbXʻGUZYhmdc`]WJYg/