

INST2003

F YgYUfWX 'A Yh\cXg']b '\=bhYfbUh]cbU''Gh X]Yg

HYfa 'C bY''##'&\$%

7ci fgY⁻Cj Yfj]Yk

'GhJZZ'7cbhJWh'8YhJ]`g'

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUhjcb	D\cbY
A Uf]`i 'A Y`c	a Uf]`i "a Y`c4 i bgk "YXi "Ui	Ŭ	A cfj Yb [.] 6fck bž fcca '' *%"	-',)`&-+\$

GWXcc``7cbHJWhi±bZcfa Uh]cb

GWkcc`cZ<iaUb]hJYg'UbX'@Ub[iU[Yg

@c\\U||cb. G\\cc``C\\Z|\\\žA\cfj\Yb'6fck\b'6i]\X]b[\z'@\j\Y``&z'&),

CdYb]b['<ci fg. 'A cbXUm'! : f]XUmž - Ua '! ') da

D\cbY.'Ž*%'&'-',)'%*,%

: UI . 'Ž * %'&'-' ,) ', +\$)

9a U]`. '<u>\U`4 i bgk "YXi "Ui</u>

7ci fgY 8YW] g

7 fYX]hDc]bhg * *

Gi a a UfmcZh\Y'7ci fgY

GI VYW15fYU.; TWA Sf[a S^E fgV[We

H\]g'Wei fgY'k]``Yei]d'mci 'k]h\ 'U'gYhcZfYgYUfW\ a Yh\cX'g_]``g"H\Y'Wei fgY'ZcWigYg'cb'hYUW,]b['\ck 'hc i bXYffU_Y'UbX'UbU`mgY'fYgYUfW\ a Yh\cXg'h\fci [\'Yl dYf]Ybf]U``YUfb]b['UbX'h\Y'i gY'cZWcbhYa dcfUfmUbX ZJa]`]Uf'WugY'ghi XmYl Ua d'Yg'cZfYgYUfW\ 'hcd]Wg'fY'Yj Ubhhc']bhYfbUh]cbU`ghi X]Yg"'K Y'k]```[Yhci hcZh\Y WUggfcca 'UbX'dfUW]W'k\Uhk Y'UfY'YUfb]b["'H\Y'Wei fgY'k]``]bhfcXi W'Vch\ 'hfUX]hJcbU`a Yh\cXg'fEcf Yl Ua d'YžX]gWci fgY'UbU`mg]gžgi fj Ymg'UbX']bhYfj]Yk gŁ'Ug'k Y``'Ug']bbcj Uhjj Y'a Yh\cXg'h\UhXfUk 'cb'h\Y UZYWfj Y'h fb'Ug'X][]hU`Yh\bc[fUd\mfZcfYl Ua d'YžYa VcX]YX'cVgYfj Uhjcbžgcb]Wa cj Ya Ybhž'd\chc Y`]WhUh]cb'UbX'[Yc!hU[[]b[Ł"l bXYfd]bb]b['h\]g'h]hjcb'cZfYgYUfW\ a Yh\cXg']g'h\Y'fUh]cbU'Y'Zcf'[YbYfUh]b[XUhU'h\fci [\ 'fYgYUfW\ a Yh\cXg']b'h\Y']bfghd'UWY"''5 ``fYgYUfW\ a Yh\cXg']g'h\Y'fUh]cbU'Y'Zcf'[YbYfUh]b[XUhU'h\fci [\ 'fYgYUfW\ a Yh\cXg']b'h\Y']bfghd'UWY"''5 ``fYgYUfW\ i bXYffU_Yb'k]h\ 'dYcd'Y']b']bhYfbUh]cbU'`UbXgWdYg'k]``]bj c'j Y'fYgYUfW\ a Yh\cXg'hc'i bXYfghUbX'h\Y']bhYfUW]cbgža cV]]hjYgža cX]ZJWUh]cbgž UhhUW\a Ybhg'UbX'ZYY`]b[g'hc'UbX'UVci hih\cgY'`UbXgWdYg"'H\]g'Wci fgY'k]``Yei]d'mci 'k]h\ 'h\Y'g_]``g'hc WcbXi WifYgYUfW\ 'a Yh\cXg'mci fgY'ZVi hi]hk]``'U'gc'XYj Y'cd'mci f'Uk UfYbYgg'cZ\ck 'h\Y'XUhU'mci 'i gY']g [YbYfUhYXž'Ug'k Y``'Ug'dfcj]X]b['h\Y'WcbhYl hi U'`Zci bXUh]cb']b'fYgYUfW\ 'Yh\]Wg'UbX'fYgYUfW\Yf dcg]h]cbU']mm''

.

.

7 ci fgY @YUfb]b['Ci hWca Yg

%" '5dd`m_bck `YX[Y`UbX`g_]``g`cZU`VfcUX`fUb[Y`cZgcWJU``fYgYUfW\ a Yh\cXg`]b`U`ZJY`X`gYHJb[/ &" 8Ya cbgHfUhY`\ck `fYgYUfW\ a Yh\cXg`UfY`X]gW| ggYX`UbX`i Hj`]gYX`]b`fY`UhJcb`hc`WcbhYa dcfUfm XYVUhYg`]b`]bhYfbUhJcbU``ghi X]Yg/

' "FYWc[b]gY`h\Y`Yh\]WU`ž'dc`]h]WU`ž'W`hifU``UbX`gcW]U``]ad`]WUh]cbg`cZWcbXiWf]b[`fYgYUfW\

- ("Gmbh\Yg]gY'_bck `YX[Y'Zfca ``YWf fYg'UbX'k cf_g\cdg'hc'Yl dYf]Ybh]U``_bck `YX[Y'[U]bYX'h\fci[\ZY'Xk cf_
-) " 5 bU`mgYži gY`UbX`YZZYWNjj Y`mWca a i b]WUNY`df]a Ufm'UbX`gYWcbXUfm'gci fWY`XUNU`]b`YggUmgž dfYgYbNUNjcbg`UbX`fYgYUfW\`fYdcfhg
- *" =XYbhjZmh\Y`ghfYb[h\g`UbX`k YU_bYggYg`cZX]ZZYfYbhfYgYUfW\`a Yh\cXc`c[]Yg`UbX`X]ghjb[i]g\`h\Y a cghW`hifU``mžgcWjU``mUbX`dc`]hjWU``mUdd`]WUV`Y`fYgYUfW\`a Yh\cX

HYUW]b['GhfUhY[]Yg'

H\Y`hYUW\]b[`ghfUhY[mWcadf]gYg`cbY`&`\cif`cZ`YWhfY`UbX`cbY`&`\cif`aYh\cX`kcf_g\cdžhc[Yh\Yf`k]h\`UjUf]YX`UgqYqqaYbh`qhfUhY[m'

H\Y"YWfi fYg'k]`"VY'dfYgYbhYX"]b'Zcfa U`ghmY'VI hei Ygh]cbg'UbX'XYVUhY'k]`"VY'YbWci fU[YX'UbX']bXYYX

Vi]`h`]bhc`h\Y``YWhi fY`ghfi Whi fY"`H\Y``YWhi fYg`k]```]bhfcXi WY`h\Y`k YY_`ma Yh\cX`ZcWig`h\fci [\`h\Y`i gY`cZU WUgY`ghi XmUddfcUW\`gi W\`h\UhU`fYU`! k cf`X`YI Ua d`Y`cZU`fYgYUfW\`ei Ygh]cb`k]```VY`dfcj]XYX`UbX`h\Y a Yh\cX`Zcf`YI Ua]b]b[`h\]g`fYgYUfW\`ei Ygh]cb`k]```VY`X]gWiggYX"

 $\label{thm:linear} H\Y'''kk\ c!\ci f'k\ cf_g\cd'k]```VY']bhY[fU''hc'h\Y'dYXU[c[mcZhYUW]b['h\Y'fYgYUfW\'a\ Yh\cXg'''H\Y k\ cf_g\cd'ghfi\ Wi\ fY']g'dfYX]WbhYX'cb'?\ c`V'g'Y!\ dYf]Ybh]U''`YUfb]b['WhWY'k\YfY'fibck\`YX[Y']g'WfYUhYX h\fci [\'h\Y'hfUbgZcfa\ Uh]cb'cZY!\ dYf]YbWfifk\YU'mUbX'>Yb_]bgž&$$$,%\) <math>E'''H\Y''k\ cf_g\cd'k\]```VY'XYg][bYX k\]h\'h\Y'Y!\ d`]WhZcW'g'cZYb[U[]b['ghi\ XYbhg']b'h\Y'dfUW]WY''cZWcbXi\ W]b['fYgYUfW\'a\ Yh\cXg'UbX\ UbU'mg]b['XUhU'[YbYfUhYX'Zfca\ 'h\]g'dfUW]W'''$

#Jih Yiz Ifghi ci ficzy UW. ik cf_g \cdžih Yi]bglfi Wtcfik]``YI d`U]b ih Yia Yh cxi Ubxih YidfuWjWi Hug_žubxik]` h Yb [i] XY ghi XYbhgfidfuWjWi czh]gia Yh cxi'' H \Yik cf_g \cdgik]``fYei] fYidfYdufuhcfmfYuX]b[iczh Yaa Yh cxi']biei Yghjcb Ubxih YiWcbhYI h'' i #Jih Yigy Wcbxi \ci ficzh Yik cf_g \cdih YiWuggik]``X]gWiggik \]``X]gWiggik \] i``X]gWiggiy ggik \Uhhcxi' k]h ih Yixuhu [YbYfuh Xžih YiWu U`Yb[YgicZxuhu Wc`YWjcbžYh]Wb`]ggi Ygžubxidfc Wiggy gicZubu mg]g'' 8 YdYbX]b[icbih Yia Yh cxih YaYžih]gigy Wcbxi \ci ficZubu mg]g'k]``Y]h YfivYiWcbxi Whxi g]b[ixuhu Ubu mg]gidfc[fuagicbih YiuviWcadi hYfgicfik]```VYiX]gWiggy XiUbxi \ubxik f]hhyb'''

5ggYgga Ybh

5ggYgga Ybh'HUg_g

5ggYgga Ybh'hUg_	K Y][\h	8i Y [.] 8UhY	Gh XYbh@YUfb]b[Ci hWca Yg 5ggYggYX

5 h Yb X Ub WY F Yei] f Ya Yb hg

5 hh/b X U b W/ c Z @ Y Wi f Y g 'U b X 'Hi hc f] U 'g '] g 'a U b X U hc fm] b 'h\] g 'W c i f g Y " I b Y I W g Y X 'U V g Y b W/ Z f ca 'a c f Y 'h\ U b & 1 c Z `Y Wi f Y g 'U b X 'hi hc f] U 'g 'k] `` f Y g i `h] b 'h\ Y 'U k U f X c Z U 'Z U] ` [f U X Y "

 $\\ \pm 0.74 \text{Win fYg'UbX'hin hcf]U'g'mci'k] \\ \text{```UWhj Y'mYb[U[Y'k]h\'WcfY'WcinfgY'WcbhYbhž'YbUV']b['mci'hc'UhhU]b'7@C'&" }$

7ci fgY GWX YXi `Y

J]Yk 'WUgg'h]a YhUV'Y

H]a YHJV`Y

8UhY	HmdY	7 cbhYbh
K YY_'%'% ': YVfi Ufm!'&(: YVfi Ufm	@YWhi fY	±blfcXiWh]cb#9d]ghYac`c[mUbXCbhc`c[m# ±bhYfbUh]cbU`GhX]Yg`UbXFYgYUfWXAYh\cXg`
K_YY'&_'&) ': YVfi Ufm!'' A_UfWX	@YWhifY	F YgYUfWX '9h\]Wg
K YY_" ."("A UfVX"! "%\$ A UfVX	@YWn fY	F YgYUfW\ '8Yg][b '
K YY_"(."%%"A UfWX"!"%+ A UfWX	@YWhifY	±ohYfj]Yk]b['#CVgYfjUh]cb'
K YY_")."% "A UfWX"!"&(A UfWX	@YWhifY	Gi fj Ymg [·] #A Ud¢l]b[

FYgci fWfg

DfYgWf]VYX F Ygci fWYg

₺Zcfa Uh]cb 'Uj U]`UV`Y 'cb 'A ccX`Y

FYWca a YbXYX FYgci fWYg

±bZcfa Uh]cbʻUj U]`UV`YʻcbʻA ccX`Yʻ

7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

7 ci fgYgʻUfYʻdYf]cX]WU``mfYj]Yk YX`UbX`ghi XYbhg' ZYYXVUW_`]gʻi gYX`hc`]a dfcj Y`h\Ya "`

 $: YYXVUW_^{\cdot}]g^{\cdot}[Uh_{\cdot}YfYX^{\cdot}Z^{\cdot}]ca ^{\cdot}ghi XYbhg^{\cdot}i g]b[^{\cdot}a m9l dYf]YbW'^{\cdot}=h^{\cdot}]g^{\cdot}YbWc^{\cdot}i fU[^{\cdot}YX^{\cdot}ghi XYbhg^{\cdot}Wc^{\cdot}a d^{\cdot}YhY^{\cdot}h_{\cdot}Y]f$ gi fj Ymg^VmUWWgg]b[^{\cdot}h_{\cdot}Y^{\cdot}dYfgcbU^{\cdot}]gYX^{\cdot}k YV^{\cdot}]b_{-}^{\cdot}j]U^{\cdot}h_{\cdot}Y^{\cdot}A ccX^{\cdot}Y^{\cdot}Wc^{\cdot}i fgY^{\cdot}g]hY^{\cdot}

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

#mci YbWci bhYf'U'dfcV'Ya 'k \Yb'UthYa dr]b['rc'gi Va]hmci f'Ugg][ba Ybht\fci [\'Hi fb]r]bž'd'YUgY
hY'Yd\cbY'9I hYfbU''Gi ddcfhcb'-',) '''' %cf'Ya U]''h\Ya 'cb'YI hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft\"'=\maintention
UfY'i bUV'Y 'rc'gi Va]hmci f'Ugg][ba YbhXi Y 'rc'U'\ZUi 'hk]h\'Hi fb]r]b'mci 'a Um'Udd'm\Zcf'Ub'YI hYbg]cb\ZVi hmci
a i ghfYhU]b'mci f'r]\W_Yhbi a VYf\Zfca '9I hYfbU''Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY'Yj UbhXcW a Ybfg\L'rc
]bWi XY'Ug'Yj]XYbWY 'rc'gi ddcfhmci f'YI hYbg]cb'Udd']\WUh]cb'''=\maintention
UfY'' bUYY''mfYWY']j Y'U'r]\W_Yhbi a VYf\ZVi h']Zmci 'hY'Yd\cbY'mci 'k]'''bYYX'rc'gdYW]\Z\WU'`mUg_'\Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'gfUh' g'cb'Hk]hYf"

; YbYfU``mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\W)``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh'' =b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]``'VY'gHJhYX'cb'mci f'\\ci fgY'g'A ccX`Y'g]hY'k]h\ U`hYfbUh]j Y'gi Va]gg]cb'XYhJ]`g''

cfi]bZcfa Uh]cbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbh'i bgk "YXi "Ui #\ck! qi Va]hUgq][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"'=hWUb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UWW]XYbhU``mWcdm]b['Zfca `U`gci fW'k]h\ci hUW_bck `YX[Ya Ybh'

 $I BGK `[fci dg'd`U[]Uf]ga `]bhc'h\Y'Zc``ck]b[`WUhY[cf]Yg.$

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$

- i bXYfgHUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbhUhI BGK
 VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hz'I BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5VWWdhUV`Y'I gY'cZ IBGK =7 HF Ygci fWrg Dc`]Wh