

# **ARTS2455**

;  $YbXYf^{\cdot}]b^{\cdot}7 \setminus ]bU$ 

HYfa 'H\fYY''##'&\$&\$

# 7ci fgY<sup>·</sup>Cj Yfj ]Yk

## GhJZZ 7 cbhJWh 8 YhJ] `g

## 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWJh]cb	D\cbY
DUb'K Ub[	DUb"k Ub[4 i bgk "YXi "Ui			
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	_		<u> </u>	

## 7ci fgY 8YW] g

7 fYX]hDc]bhg\*\*

Gi a a UfmcZh\Y'7ci fgY

H\]g'Wci fgY YI d'cfYg'h\Y XfUa UhJWW.Ub[Yg'hc'[YbXYf'UbX'gYI i U']lmibcfa g'YI dYf]YbWX.VmdYcd'Y '`]j ]b[]b'7\]bU'cf'cdYfUhJb[']b'h\Y'G]bcd\cbY'k cfX"'H\Y'Wci fgY YI Ua ]bYg'h\Y'hfUbgZcfa UhJcb']b'h\YgY'fYU'a g Zfca ']a dYf]U''hJa Yg'h\fci [\'hc'h\Y'W ffYbhYfU"'±ig\ck g'h\Y'cb[c]b['hYbg]cb'VYk YYb'dcdi 'Uf']XYUg'UVci h fffUX]hJcbfiUbX'fa cXYfb]mfiUg'[YbXYf'UbX'gYI i U']lmibcfa g'UbX'dfUWJWg'\Uj Y'W\Ub[YX'cj Yf'hJa Y"'±h YI Ua ]bYg']bhYfj YbhJcbg'Vm7\]bUfg'j Uf]ci g'[cj Yfba Ybhg'UbX'`Y[U'''gmghYa g'UbX'WJa dU][bg'VmUWJj]]ghg UbX'fYZcfa Yfg'hc'W\Ub[Y'h\Y'ghUhi g'ei c'Ug'k Y'''Ug'h\Y'i gY'cZgYI 'UbX'[YbXYf'VmWfYUhJj Y'Uff]ghgž'k f]hYfg UbX'UXj YfhJgYfg"'Nci 'k]'''YUfb'Uvci hd\Ybca YbU'gi W\ 'Ug. 'dfc[fYgg'hck UfXg'gYI 'Yei U']lmž'hYbg]cbg VYfk YYb']bX]j ]Xi U''XYg]fYg'UbX'ZYa ]b]b]hJYg']b''cWJ''UbX'[`cvU''WcbhYI hgž'X]j Yfg]hm]b'[YbXYf'UbX gYI i U']lmbcfa g'Ua cb['7\]bUfg'bcb!<Ub'Yh\b)MJhJYg'UbX'X]ZYfYbhigcWJU''WUggYgž'W ffYbhW\U''Yb[Yg']b [YbXYf'UbX'gYI i U']lmbcfa g']b'fY'UhJcb'hc'd\Ybca Ybcb'']\_YZJa ]'mZcfa UhJcbžYa d'cma Ybhz'dc']hJWJ'

### 5ggYgga Ybh

8YHJ]YX`]bghfi Whjcbg`Zcf`YUW\`UggYgga YbhHJg\_'k]``VY`i d`cUXYX`hc`A ccX`Y"`FYZYf`hc`UggYgga YbhVf]YZ'`

#### 5ggYgga Ybh'HUg\_g

5ggYgga Ybh'hUg_	K Y][ \h	8iY'8UHY	Gh XYbh@YUfb]b[ Ci hWca Ygʻ5ggYggYX
DfYgYbhUhjcb <sup>*</sup> Ž <sup>*</sup> HfUbgWf]dh	' \$1	(da ˈcbˈdfYgYblIJljcbːXUm	%ž&Ž ž( ž)
DYfgcbU`*\DHYfdfYfUfJcb'	&\$I	(da 'Hi YgXUm']b'K YY_'+	%ž&Ž Ž( ž)
K f]hb[ 'HJg_'	) \$1	( da ': f]XUm']b'k YY_'%\$	%ž&Ž Ž( ž)

#### 5ggYgga Ybh'8YHJ]`g

5ggYgga Ybh% DfYgYbhJh]cb Ž HfUbgWf]dh

GhUfhXUhY. K YY\_&

8YHJ]`g.

Gh XYbhg k ]```dfYgYbhh\Y]f'i bXYfgHUbX]b[ 'UVci hU'gY`ZgY`YVMYX`WJgY'fY`UhYX`hc 'h\Y`k YY\_fg``X]gW gg]cb hcd]W'`H\Ymk ]```VY`Ug\_YX`hc 'dfca dhX]gW gg]cb 'Zcf'h\Y]f'dYYfg"'H\Y`ZYYXVUW\_k ]```VY`dfcj ]XYX'j ]U'U'F i Vf]W Zcf'DfYgYbhUh]cbg`W ffYbhm]b'i gY`]b'5g]Ub'Gh X]Yg'Wci fgYg"

@Yb[h\.') hc \% a ]bi hYg

CfU`ZYYXVUW ..

Gi Va ]gg]cb`bchYg.Mci `WJb`YX]hmci f`dfYgYbhUh]cb`UbX`h\Y`hfUbgWf]dh]b`DDH`UbX`gUj Y`]hUg`U`D8: `Z]`Y`Zcf Z|bU``gi Va ]gg]cb"

 $\label{thm:continuous} \begin{tabular}{ll} Hi & fb & fb & gYM &$ 

5ggYgga Ybh& DYfgcbU` ⇒hYfdfYhJh]cb

GHJfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g.

Ghi XYbhgʻk ]```gi Va ]hiU'dYfgcbU`]nYX'UggYgga Ybhhcʻg\ck WJgY'h\Y]fʻi bXYfghJbX]b[ 'UVci h[ YbXYfʻ]bʻ7 \]bU" H\]g'UggYgga YbhiWJb'VY`]bʻh\Y`Zcfa 'cZg\cfhiYggUmžj ]XYcžXcW a YbhJfmž'dcghYfž'dcXWJghžYh\bc[ fUd\]W ]bhYfj ]Yk žk YVg]hY'cf`Ubmch\Yf`Zcfa Uhg"'Ghi XYbhgʻg\U```X]gW ggʻh\Y]f'dfcdcgU`gʻk ]h\'h\Y``YWhi fYf'UbX cVhJ]b'dYfa ]gg]cb'VYZcfY'gi Va ]hh]b[ 'h\Y`UggYgga Ybh'

C fu`ZYYXVUW"

 $\begin{tabular}{ll} Gi Va ] $gg]$cb`bch'g. D`YUgY`WcbhUWh\Y`hYUW\]b[ `ghUZ]Zmci `UfY`i bUV`Y`hc`gi Va ]hh\Y`W\cgYb`Zcfa Uhhc h\Y`Ugg][ ba YbhVcl `]b`A ccX`Y \\ \end{tabular}$ 

Hi fb]hjb gYhjb[. H\]g ]g bchU Hi fb]hjb Ugg][ ba Ybh

5ggYgga Ybh' . K f]h]b[ HJg\_

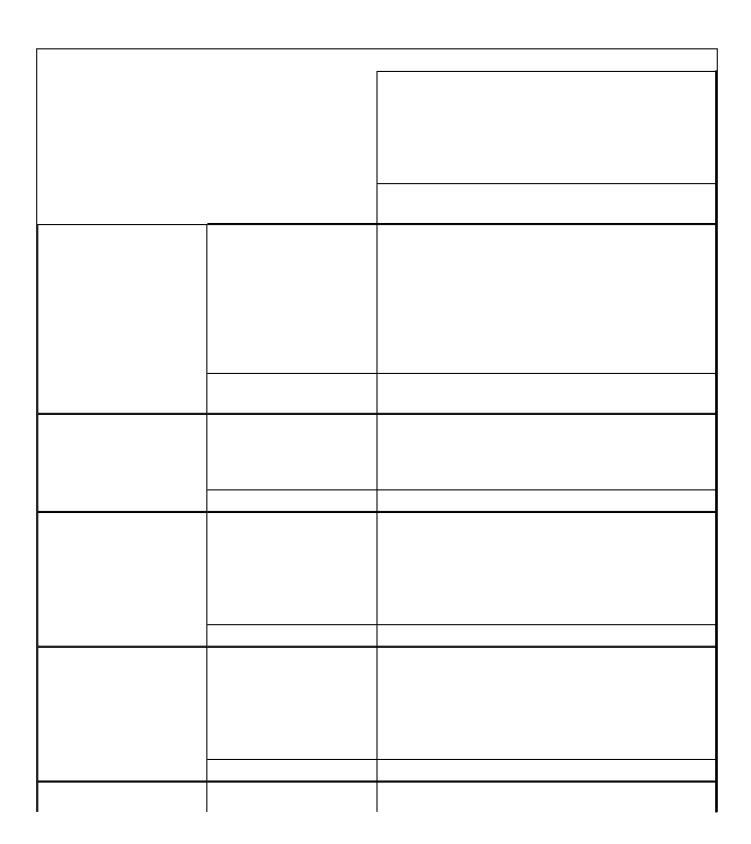
GhufhXuhY. Bch5dd`]WUV`Y

8 YW] g.

Ghi XYbhgik ]```\Uj Yihk cicdhjcbgiZcfih\YihUg\_"'Cdhjcbi%]giU'WU"'&ž(\$\$!kcfXifYgYUfW. YggUm'iGhi XYbhgik]``VYUg\_YXihcigY`YWhiUifYgYUfW. iei YghjcbiZca iU'bca ]bUhYX``]ghi'H\Y]fihUg\_i]gihci[Uh\YfifYgYUfW. iei YghjcbiZca iU'bca ]bUhYX``]ghi'H\Y]fihUg\_i]gihci[Uh\YfifYgYUfW. iei Yhhk]h\Yj ]XYbWfiUbX``c[]\Wi`U'WYUfi iei YbhiUfci bXih\YifYgYUfW. iei YghjcbiZvi hffYggih\]giUf[iei Ybhik]h\Yj ]XYbWfiUbX``wca e iei]\WhYi]biU'WYUfikf]hhYbiZJg\]cb"'H\YiYj ]XYbWfik]``VY'dfYgYbhYX`]biZcfe U''UWUXYe]\WebiUhJcb'''CdhJcbi&i]giU'Wf]hJWU``fYZYWhJcbiCZh\YiWci fgY"'H\]giHUg\_i]giYei]j U'Ybhhcih\YfYgYUfW. YggUm]bihYfe gicZkcfXiYb[ih\"iGhi XYbhgik]``kf]hYiY][\hi'\$\$!kcfX'Wf]hJWU``fYZYWhJcbgiVmh\YiYbXcZh\YihYfe ibcXYeeoffUhYih\Y]fii bXYfgHUbX]b[iUVci hh\YikYy\_`mhcd]\WUbXifYUX]b[g"'H\Yikf]hjb[iHUg\_i]gh\YiZfUUy\XifYUX]b[g"'H\Yikf]hbXUbWfidi fdcgYg"

K f]hhyb ZYYXVUW "

 $\label{thm:continuous} \begin{tabular}{ll} Hi fb]h]b"gYh]b[."H\]g"Ugg][ba Ybh]g"gi Va]hhYX"h\fci [\Thi fb]h]b"UbX"gh XYbhg"WUb"gYY"Hi fb]h]b"g]a]"Uf]hm fYdcfhg" \end{tabular}$ 



### FYgci fW/g

#### DfYgWf]VYX F Ygci fWYg

FYZYf'hc'k YY\_`mfYZYfYbWYg'UbX'@Y[Ubhc'fYUX]b['`]ghi]b'AccX`Y'

#### FYWca a YbXYX FYgci fWYg

9Xk UfXgž@"&\$\$, ž9W VWd Ba $^{f}$ f[Ueł S`V 6 W\_ a UdSUk, I a\_ W e E g XdSYW[ 5 Z [ SžGHJb ZcfXž7 5 žGHJb ZcfX I b]į Yfq]hm DfYqq"

9j Ubgž'< "'% - +ž'l a\_ W S` V eWj gS'{fk [` 5Z[` S, Va\_ [` S` f V[eUagdeWe a X X W\_ S WeWj gS'{fk S` V Y W V W de[` UW#+&+ž' 7 Ua Vf]X[Y. 'Dc`]miDfYgg"

A Ubbž@"G'&\$%%39W VWdS`V EWjgS1fk [ ? aVWd 5Z[ WeW: [efack37Ua Vf]X[Y:7Ua Vf]X[Y'I b]j Yfg]lm DfYgg"

Gcb['; Yb['UbX'<]fXž'8"'&\$%( ž'? W S` V ? SeUg f [f[We [ 5a`fW\_ bac6ck 5Z[ Sž'@Y]XYbž'BYh\Yf'UbXg. '6f]`"

K Ub[ DUb &\$%) zzahWS V? Sch[SYW] 9 aTS1 Y 5 Z Sz 5 V b Xcbz C I cb / BYk Mcf\_ : F ci hYX Y "

NUb['L]UckY]'UbX'N\Uc'L]Uc'@''fYXgŁ'&\$% ž: S`VTaa] a` fZW8S\_['k S`V ? Scb[SYW[' 5 Z[' Sž'9Xk UfX 9'[ Uf"

#### 7ci fgY'9j U'i Uhcb'UbX'8Yj Y'cda Ybh

H\]gʻWci fgYʻk]``VYʻYj U`i UhYXʻj ]Uʻh\Yʻa m9l dYf]YbWYʻgi fj YmgʻUhih\YʻYbXʻcZh\YʻhYfa "ʻ⊋mci ʻ\Uj Y gi [[Ygh]cbgʻcbʻk Umgʻhcʻ]a dfcj Yʻh\YʻWci fgYʻXi f]b['h\YʻhYfa ž'd`YUgYʻZYY``ZfYYʻhcʻWca YʻUbXʻhU`\_ihcʻi g"ʻK Y k Y`Wca Y`mci fʻZYYXVUW"

### Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

### Hi fb]h]b Gi Va ]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb[ 'hc'gi va ]hmci f'Ugg][ ba Ybhh\fci [ \ 'Hi fb]h]bz'd'YUgY

Hy'Yd\cby'9| hy'fbu''Gi ddcfhcb'-', ) '' ' ' %cf'Ya U]''h\Ya 'cb'Y! hy'fbu'hy'hgi ddcfh4 i bgk "YXi "Ui "''Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUft'''=Z'mci
UfY'i bUV'Y'hc'gi va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\ 'Hi fb]h]b'mci 'a Um'Udd'mZcf'Ub'Y! hy'bg]cbz'Vi hmci
a i ghfYhJ]b'mci f'h]W\_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb[ 'k ]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj ]XYbW' hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k ]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W\_Yhbi a VYfz'Vi h]Zmci 'hY'Yd\cbY'mci 'k ]``bYYX'hc'gdYW]Z]WJ'`mUg\_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj ]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug\_g'a i ghVY'gi Va ]hhYX'Y`YVWfcb]\WJ``mij ]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k ]h\U`hYfbUh]j Y'gi Va ]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va ]hUgg][ ba Ybhgicbi]bYij ]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va ]hUgg][ ba Ybha ccXiY

## 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU\_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW\_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga ]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj ]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U\_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

## 5WUXYa]W±bZcfaUhjcb

: cf'YggYbhJU`ghi XYbh]bZcfa UhJcb'fY`UhJb['hc.

• fYei Yghg Zcf Yl hYbg]cb/