

ARTS3574

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- '" 8]gWi gg`h\Y`X]ZYfYbWi'g`VYhk YYb`h\Y`bYk `hfYbXg`]b`@Uh]b`5a Yf]WUb`W]bYa U`UbX`h\Y`UYgh\Yh]Wg UbX`dc`]h]Wg`cZh\Y`@Uh]b`5a Yf]WUb`BYk `7]bYa U#H\]fX`7]bYa U:cZ% *\$g!%, \$g
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H\Y'H\YUW\]b['d\]`cgcd\mcZh\]g'Wci fgY']g']bZcfa YX'Vmh\Y'I BGK'; i]XY`]bYg'cb'@YUfb]b['z'UbX'WUb'VY gi a a Uf]nYX'Ug'9b['U['Ya Ybhz'7cbhYl hi U']nUh]cb'UbX'\dwi g]j YbYgg'fgYY'\
\(\frac{k k k "[i]XY`]bYgcb`YUfb]b['"i bgk "YXi "Ui \\\"'\\Y'`YWh fYf']b'W\Uf['Y'gYY_g'hc'dfcj]XY'U'j Ybi Y'Zcf'h\cgY'h\fYY_Ymdc]bhgz'UbX'h\YfYZcfY'Ya d\Ug]nYg'h\Uh'h\Y'`Uf['Yf'cVYW]j Y']g'hc'hYUW\'gh XYbhg'\ck 'hc'VYWca Y'Wf]h\W\'YUfbYfg"

 $\label{eq:hamiltonian} $$H^{g''U'V'YbXYX'UddfcUWX'cZ@YWiffYg''UbX'Hifcf]U'gz'cf[Ub]nYX'UfcibX'_YmfYUX]b[g'UgWcbfU]bYX']b'hX'7cifgY'FYUXYf''$$

5 "YWM fY YUW\ k YY_k |` "UXXfYgg hcd |WfgLUXXfYggYX |b h\ Y Z|a J |Yk |b[; i |XYg UbX F YUX|b[g" A U cf|lm |

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 $H\g^{2}UVYbXYX`YUfb]b[`WcifgYz`UWij Y`X]gW gg]cb`UbX`dUffjWjdUfjcb`UfY`fYei]fYX''`5Wij Y`dUffjWjdUfjcb]b`h\]g`WcifgY`a YUbg`h\Uhmci`\Uj Y`a UXY`U`Wcbglfi Wij Yž]bZcfa YX`Wcblf]Vifjcb`hc`WUgg`X]gW gg]cbg'' D`YUgY`Wca Y`hc`WUgg`dfYdUfYX''`H\]g`a YUbg. `gYY`h\Y`k YY_`m`Z]`a g`UbX`fYUX`h\Y`dYffjbYbh'UffjWYg`Zcf`h\Y dUffjW`Uf`k YY_`gc`mci`UfY`dfYdUfYX`Zcf`WUgg''$

5ggYgga Ybh'HUg_g'

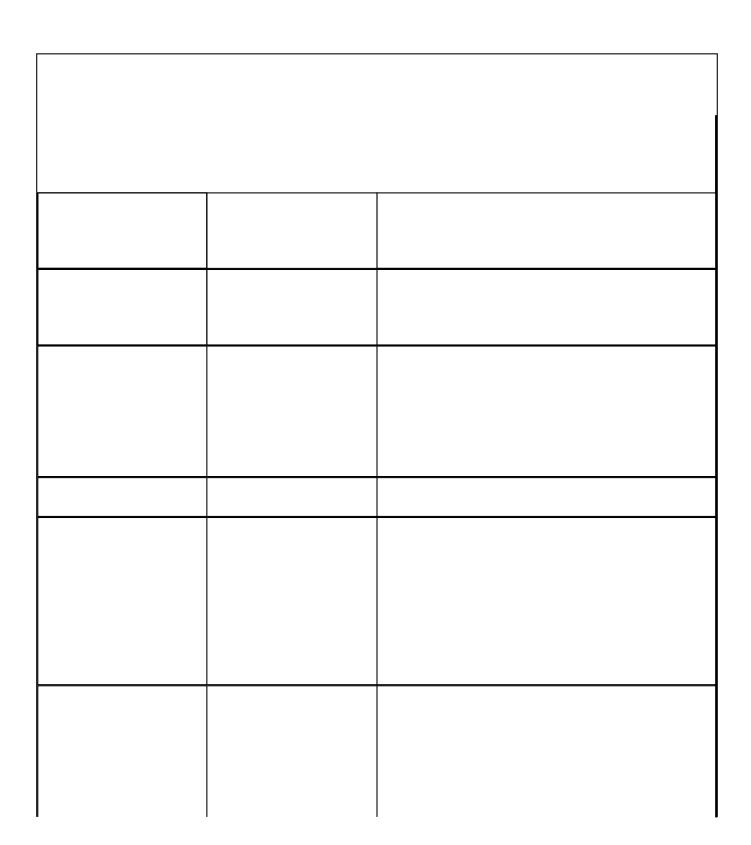
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hc 'h/b 'a]bi h/g 'cZWUgg 'X]gW gg]cb " 'Mci 'k] ``'hU`_ž'B C H 'F 958 " $^{\circ}$

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5ggYgga Ybh'8YgWf]dh]cb. `Gh XYbhg bYYX'hc `fYgYUfW `U'hcd]WfY`Yj Ubhhc `@Uh]b '5a Yf]WUb '7]bYa U'Vi h X]ZYfYbh'Zca 'h\Y'cbY'WkcgYb 'Zcf'h\Y'[fci d'dfYgYbhUf]cb" '9UWk 'gh XYbhbYYXg'hc 'k f]hY U'' \$\$\$!k cfX`YggUmUbX`]bWi XY'U'V]V`]c[fUd\mcZ'Uh`YUgh'hYb 'UWUXYa]Wgci fWYg'Wcbgi `hYX`]b



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a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgthc
]bWi XY'Ug'Yj]XYbW' hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']\WJh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]\WJ'`mfYW']j Y'U'h]\W_Yhbi a VYfz'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdY\WZ]\WJ'`mUg_'Zcf'cbY''
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; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

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- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
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Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

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