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7\]bYgY`W\UfUWfYfg"`GfUffjb[`Zfca 'D]bmjbž'h\Y`cZZ]WJU``d\cbYh]WgmghYa 'cZGfUbXUfX`7\]bYgYž'h\Y`Wci fgY\Y`dg`mci 'YghUV`]g\`U`gmghYa UhJW`YUfb]b[`dUffYfb`UbX`XYjY`cdg`mci f`Zci f``Ub[i U[Y'g_]``g`f]"Y"``]ghYb]b[ž gdYU_]b[žfYUX]b[`UbX`kf]hjb[£']b`Ub`]bhY[fUhYX`a UbbYf"'#i]bffcXi WYg`mci 'Uddfcl]a UhY`m'%)\$'j cWUVi `Ufmk cfXgž'U`cb[`k]h\ h\Y`UggcWjUhYX`gcWjcW`hi fU``UbX``]b[i]ghJWUk UfYbYgg`]b`XUmhc!XUmhcd]Wgžgi W\`Ug [fYYh]b[gž]bffcXi WJb[`cbYgY`Zza U_]b[`Ub`Uddc]bha YbhUbX`hU`_]b[`UVci hi b]j Yfg]fm`]ZY"

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- %" I bXYfghUbX UbX i gY Uddfcl]a UhY`m%) \$ YggYbh]U`ij cWUVi `Ufm]hYa g"
- &" 5ddmih\Y`Zci f``Ub[i U[Y`g_]``g`]b`7\]bYgY`f]"Y"``]ghYb]b[ž`gdYU_]b[ž`fYUX]b[`UbX`k f]h]b[Ł'Uh]bhfcXi Wfcfm`Yj Y`ž'hU_]b[`]bhc`UVW£i bhqh XYbhqf\Yf]hU[Y`VUW_[fci bX"
- ' " 7 ca a i b]WUHY YZZYWNj Y`m`]b`7 \]bYgY`cb`hcd]Wg`gi W.`Ug`]bHcXi Wjb[`cbYgY`Zzʿa U_]b[`Ub Uddc]bha Ybh'UbX`HU`_]b[`UVci hi b]j Yfg]hm`]ZYž`]b`Vch\`cfU``UbX`k f]HHYb`Zcfa gž`]b`U``]b[i]gH]WU``mUbX qcW[cW\`hi fU``mUddfcdf]UHY`a UbbYf"
- ("5dd`m]bXYdYbXYbh`YUfb]b['glfUhY[]Yg'lc']bWfYUgY'7\]bYgY'dfcZ[W]YbWhiVYmcbX'h\Y'WUggfcca"

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H\]g``Ub[i U[Y'Wci fgY'fYei]fYg'ghi XYbhg'hc'UhhYbX``YWhi fYg'UbX'hi hcf]U`g"'H\Y'`YWhi fYg'Wcj Yf'bYk j cWUVi `Ufmž'[fUa a Uh]WU``ghfi Whi fYž``Yggcb'hYl h'UbX'W `hi fU``UbX``]hYfUfmUk UfYbYgg"'H\Y'hi hcf]U`g'ZcW g'cb `]ghYb]b['UbX'gdYU_]b['Yl YfW]gYg'Ug'k Y```Ug'fYUX]b['UbX'k f]h]b['HUg_g"'6Yg]XYg'h\Y'WUggYgž'U`a]b]a i a 'cZ ('\ci fg'cZk YY_`mghi Xm]b['h]a Y'ci hg]XY'h\Y'WUggfcca ']g'fYei]fYX']b'cfXYf'hc'cVhU]b'U'gUhJgZUWhcfm `YUfb]b['fYgi `h'Ghi XYbhg'UfY'Yl dYWhYX'hc'fYj]Yk 'YUW\'`Yggcb'UbX'Z]b]g\'U``k cf_Vcc_'Yl YfW]gYg'Ug'gccb UZhYf'h\Y'k YY_`mWUggYg'Ug'dcgg]V`Y''';]j Yb'h\UhYUW\'bYk '`Yggcb']g'VUgYX'cb'U``'WcbhYbh'Wcj YfYX dfYj]ci g`mž'ghi XYbhg'g\ci `X'bchdcghdcbY'h\Y]f'ghi X]Yg"

5g·Zcf·dfuWijwu``hYuw\]b[žvch\`ghfi Wifu``a Yh\cX`UbX`wca a i b]wuhj Y`a Yh\cX`k]```VY`Udd`]YX`]b`h\Y wci fgY"' ⊕ Yuw\``Yggcb`ghi XYbhg`k]```VY[]b`k]h\j cwuvi `UfmUbX`ghfi Wifu``dfuWijwžZc``ck YX`VmHug_!VugYX uwhj]h]Yg"`7 cbg]XYf]b['h\Uhih\Y`ghi XYbhg`UfY`Vuw_[fci bX``YUfbYfgžU`gi VghUbh]U``Ua ci bhcZwugg`k]```VY wcbXi WhYX`]b`7 \]bYgY"'H\Y`hYuw\]b['ghuZk]```UX^ ghh\Y`Ua ci bhcZ9b[`]g\`UbX`7\]bYgY'i gYX`UwwcfX]b[hc`ghi XYbhg''ZYYXVuw_UbX`bYYXg"

GYY XYHJ]`g`]b`h\Y`UggYgga YbhVf]YZ]b`A ccX`Y`

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5XX]h]cbU`XYhU]`g.

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\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
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a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hy'Yd\cby'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cby''
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; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

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