

ARTS2270

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7ci fgY⁻Cj Yfj]Yk

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7cbj Ybcfg

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7 cblfcj Yfg]YgʻfY[i `Uf'mYfi dh]bʻ5i glfU`]Uʻcj Yfʻ]ggi Ygʻk \YfY`]XYbh]miUbXʻf`gh]Wf`]bhYfgYWhʻk \cʻg\ci `XʻVY [fUbhYXʻUgmì a 3`\ck `WJbʻh\Yʻf][\hgʻcZ\DX][Ybci gʻdYcd`YgʻVYʻZ ``mfYgdYWhX3`\ck `g\ci `Xʻ5i glfU`]U fY`UhYʻhcʻ5g]U3ʻ\David fgYʻmci `k]``YI dʻcfY`\ck 'h\YgY`]ggi Ygʻk YfYʻZcghYfYXʻVmh\Yʻa Uʻcfʻh\Ya YgʻcZ 5i glfU`]Uʻgʻ% h\`Wfbh fm\]ghcfmʻh\YʻgYhiYfʻfYj cʻi h]cbžʻ\DX][Ybci gʻX]gdcggYgg]cbʻUbXʻfYg]ghUbWfž'UbXʻh\Y f]gYʻcZgWJYbhJZWfUWJga `cbʻh\YʻcbY`\UbX/a cj Ya Ybhgʻhck UfXgʻXYa cWfUWhži b]j YfgU``YXi WUhjcbʻUbX`VYHYf`]j]b[ʻghUbXUfXgʻcbʻh\Yʻch\Yf''HYbg]cbgʻUf]g]b[ʻZfca 'h\YgYʻh\Ya YgʻUfYʻWca a cbʻhcʻU```gYhhYfʻgcWJYhJYgʻVi h 5i glfU`]UʻgʻcWUhjcbʻUhhXyʻYX[YʻcZ5g]Uʻa YUbgʻh\Ymk YfYʻd`UmYXʻci h\YfYʻk]h\`U`X]ghJbWhj YʻgYbgYʻcZ i f[YbWmk\cgYʻfYj YfVYfUhjcbgʻdYfg]gh'

7 ci fgY @YUfb]b[Ci hMca Yg

%" 5bU`mgY ']a dcfhUbhYj Ybhgž]XYUg`UbX`h\Ya Yg`fY`Yj Ubhhc`% h\`W\bhi fm5i ghfU`]U"
&" \$bh\fdfYhžYj U`i Uh\'UbX`Wcbh\I i U`]gY`fY`Yj Ubhdf]a Ufmgci f\\g"
' " 9j U`i Uh\'g\\c`Uf`mUf[i a Ybhg`UbX`XYVUh\'g`cb`_Ymh\Ya Yg"
(" A U_Y`Yj]XYb\\Y!VUgYX`Uf[i a Ybhg`i g]b[`]bXYdYbXYbhm`c\\Uh\'X`gci f\\g"

HYUWX]b['GhfUhY[]Yq'

H\Y'Wti fgY']g'XYg][bYX'hc'XYj Y`cd'mci f'_bck `YX[Y'UbX'i bXYfghUbX]b['cZ_Ymh\Ya Ygž'Yj Ybrg'UbX XYVUhYg']b'5i ghfU`]U'g'% h\ 'Wbhi fm\]ghcfmž'hc']a dfcj Y'mci f'g_]``g'UhWf]hjei]b['gW.c`Uf`mUbX'dcdi `Uf k f]hjb[gž'UbX'hc'\Y'd'mci 'Wtbghfi Whimci f'ck b'Uf[i a Ybhg'VUgYX'cb'Yj]XYbW\"'H\Y'`YWhi fYg'dfcj]XY'U VfcUX'dYfgdYWf]j Y'cb'a U'cf'hcd]Wg'UbX'YbUV'Y'mci 'hc'WtbhYl i U`]gY'UbX']bhYfdfYhh\Y'hi hcf]U``fYUX]b[g" H\YgY'Wtbg]ghcZVch\ 'df]a UfmUbX'gYWtbXUfmgci f\Wg'UbX'k]```VY'UbU`mgYX'UbX']bhYfdfYhYX']b 'ga U```UbX`Uf[Y'[fci d'X]gW gg]cb"'H\Y'fYgYUfW\'YggUmYbUV'Yg'mci 'hc'XYj Y`cd'mci f']bhYfYgh]b'U'hcd]\Wymdi fgi]b[]bXYdYbXYbhfYgYUfW\'UbX'h\Y']b!WUgg'hYghdfcj]XYg'Ub'cddcfhi b]hmZcf'mci 'hc'fYZYWhicb'h\Y g][b]Z\WbW'cZh\Y'hcd]\Wg'Ug'h\YmfY`UhY'hc'YUW\'ch\Yf"'H\Y'Wti fgY'g'a U'cffUh]cbU'Y']g'hc'gh]a i `UhY'mci f']bhYfYgh]b'5i qhfU`]Ufa'dUghUg'U'k UmcZi bXYfghUbX]b['WtbhYa dcfUfm5i qhfU`]U"

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GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\.'&) \$\$ k cfXg

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 $Gh XYbhg k] ``k f]hY Ub YggUmf&z) $$ k cfXgEVUgYX cb]bXYdYbXYbhfYgYUfWk": YYXVUW_j JU]bX]j JXi U`Wa a Ybh'H\]g Jg h Y ZbU`UggYgga YbhZcf'UhYbXUbW'di fdcgYg"$

 $\label{thm:continuous} \begin{tabular}{ll} Hi & fb & fb & gYM &$

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DfYgWf]VYX`F Ygci fWYg`

 $9\,ggYbh]U``fYUX]b[\,g^.k\,]```VY^.Uj\,\,U]`UV`Y^.hc^.ghi\,\,XYbhg^.cb^.A\,\,ccX`Y$

FYWca a YbXYX FYgci fWYg

 $\label{thm:linear_condition} $$HY'Zc``ck\]b['dfcj']XY'[ccX'[YbYfU``cj'Yfj']Yk\ gžcf']bffcXi\ Wf]cbgž'hc'h\Y'h\Ya\ Yg'XYU`hik\]h\']b'h\Y'Wci\ fgY$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb['hc'gi va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]h]bž'd'YUgY

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\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
UfY'i bUV'Y'hc'gi va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a Um'Udd'mZcf'Ub'Y! hy'bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' 'hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va]hUgg][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

- i bXYfgHUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'ghi XYbh'Uhi BGK VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hž'I BGK 'Ghi XYbh'7cXY'cZ7cbXi Wh'UbX'5VWWdhUV`Y'I gY'cZ IBGK =7 H°F Ygci fW/g°Dc`]Wm

5 WUXYa] W + D Zcfa Uh]cb

: cf`YggYbhJU``gh XYbh`]bZcfa UhJcb`fY`UhJb['hc.

- fYei Yghg Zcf Yl hYbg]cb/`UhY gi Va]gg]cbg [i]XY`]bYg/
- fYj]Yk cZa Uf_g/