

ARTS2362

5`]YbUhjcb'UbX'GcWjU`'7f]hjeiY

HYfa 'Hk c''##'&\$&%

7ci fgY^{*}Cj Yfj]Yk

GHJZZ:7cbHJWh:8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWUh]cb	D\cbY
< Y]]		7 cbHJWfiVmiYa U]`Zcf Wcbgi `HJH]cb	A cfj Yb [·] 6fck b ' &%	

GWXcc`7cbHJWh ≠bZcfa Uh]cb

GWkcc``cZ<iaUb]hJYg`UbX`@Ub[iU[Yg

@c\WJh]cb. G\W\cc``C\Z]\\Y\ž\A\cfj\Yb'6fck\b'6i\]\X]b[\ž'@Yj\Y``&\ž\&),

7ci fgY 8YHJ] g

7 fYX]hDc]bhg**

Gi a a UfmcZh\Y 7ci fgY

H\]g`Wci fgY`Ug_g`\ck `U`gcW]YhmWUb``Y[]h]a UhY`mWf]h]W]gY`]hgY`Z'=hYl Ua]bYg`k \m]h]g`h\Uhbch]cbg`gi W\`Ug ZYYXca žgY`Z\XYhYfa]bUh]cb`UbX`\]ghcf]WU``dfc[fYgg`\Uj Y`Wca Y`hc`Uggi a Y`U`WYbhfU``d`UWY`]b`a cXYfb`]ZY" 5fY`h\YfY`d`Ui g]V`Y`k Umg`hc`^\X[Y`gca Y`dUfh]W``Uf`XYj Y`cda Ybhg`cZgcW]U```]ZY`Ug`dfc[fYgg]j Y`cf fY[fYgg]j Y3`5fY`gca Y`Zcfa g`cZgcW]U```]ZY`'dUh\c`c[]WU`'3`=g`h\Y`df]WY`cZa cXYfb`ZfYYXca `U`]YbUh]cb`Zfca ci fgY`j Yg`UbX`h\Y`bUh fU``k cf`X3`H\Y`h\Ya Yg`X]gW ggYX`]b`h\]g`Wci fgY`a Um]bWi XY.`U`]YbUh]cb`Z]XYc`c[m² a cXYfb]hm²hchU`]hUf]Ub]ga ž'dgm\%cUbU`mg]g`UbX`dck Yf"`H\]b_Yfg`k \c`a Um`VY`Yl Ua]bYX`]bWi XY. F ci ggYUi ž'? Ubh²c\Yf\Yi YfVUW\ZB]Yhmg\%YZA Ufl Z`@`_!\Mg\Z'K YVYfZ': fYi Xz'<Y]XY[[YfZ'5Xcfbcz'<cf_\Y]a YfZ'5fYbXhz': ci WUi `hUbX`ch\Yf`]bZi YbhJU``Z[[i fYg`]b`Wf]hJWU``gc\JU``d\]`cgcd\m'

7 ci fgY @YUfb]b[Ci hMca Yg

- %" 9j U`i UHY'h\Y'a Yf]rg'UbX``]a]hUh]cbg'cZ_Ym'UddfcUW\Yg'rc'h\Y'd\]`cgcd\]WU`'dfcV`Ya 'cZa cXYfb]hm UbX'gcW]U`'d\]`cgcd\m
- &" 5ggYgg`X]gh]bWidcg]h]cbg`k]h\`fY[UfX`hc`U`]YbUh]cbžZfYYXca `UbX`gcW]U``Wf]h]ei Y`]b`_Ymk cf_g`]b K YghYfb`d\]`cgcd\m
- ' " 7 f]h]WU``mUddfU]gY`h\Y`fY`Yj UbWY`cZ_YmUddfcUW\Yg`hc`U`]YbUh]cbž'ZfYYXca `UbX`gcWJU``Wf]h]ei Y`]b a cXYfb`d\]cgcd\mhc`WcbhYa dcfUfmgcWJYhm'
- ("8YjY`cd`UbX`Yb\UbW'`g_]``g`UggcW]UhYX`k]h\`d\]`cgcd\]WU``]bei]fmžgi W\`Ug.`Wf]h]WU``UbU`mg]gž hYI hi U``]bhYfdfYhUh]cbžUf[i a Ybh'UbX`k f]hhYb'YI dfYgg]cb"

HYUWX]b['GhfUhY[]Yq'

H\Y'Wti fgY'k]``bcfa U``m'VY'HJi [\hk]h\'U'Hkc!\ci f'kYY_`m'YWti fYz'UbX'U'cbY!\ci f'X]gWi gg]cb!VUgYX hi hcf]U'"'@YWti fYg'k]```VY']bhYfUWtji Yz'UbX'ghi XYbhdUftjWjdUhjcb']g'YbWti fU[YX"'@YWti fYg'k]```Wtj Yf'_YmhXa Yg'UbX'gdYWjZjWhYl hg']b'a cXYfb'd\]cgcd\mž'Ug'k Y```Ug'VUW_[fci bX'\]ghcf]WU`]ggi Yg"'H\fci [\'U gY'YWtjcb'cZfYUX]b[gžYl YfWjgYgž'UbX'ga U```[fci d'X]gWi gg]cbgž'h\Y'Wti fgY'k]``XYj Y`cd'ghi XYbhgfiUV]`]hmlrcfYUXz'UbU`mgYz'Wf]hJWjgYz'X]gWi ggz'UbX']bhYfdfYhid\]`cgcd\]WU``HYl hg"'H\Y'fYgYUfW\'dcfhZc`]cz'k\]W\']g XYg][bYX'hc'YbWti fU[Y'ghi XYbhg'hc'Yb[U[Y'h\cfci [\`mk]h\'h\Y'dfYgWf]VYX'kYY_`mfYUX]b[g'TW&dWWUgg UbX'hc'dfYdUfY'ei Ygh]cbg'Zcf'h\Y'hi hcf]U'z']g'U'WtfY'YYa YbhcZh\Y'hYUW\]b['gffUhY[mcZh\Y'Wti fgY"'K YYl dYWfighi XYbhg'hc'dUffjWjdUhY']b'h\]g'Wti fgY'VmUhYbX]b['"YWfi fYgz'Yb[U[]b['k]h\'ch\Yfg']b'hi hcf]U'g'UbX cb']bY'X]gWi gg]cbg'fk\YfY'Udd']WUV'YŁ'UbX'hc'Wta d'YhY'h\Y'fYei]fYX'fYUX]b[']b'dfYdUfUhjcb'Zcf'hi hcf]U`g UbX''YWfi fYg"'Hi hcf]U'g'k]"'U'gc'X]gWi gg'fYgYUfW\'g_]``g'UbX'k f]hjb['g_]``g"

5ggYgga Ybh

5ggYgga YbhHUg_g

5ggYgga Ybh'hUg_		

 $\label{thm:limit} \begin{tabular}{ll} Hi & fb \end{tabular} $$ Hi & fb \end{tabular} $$ h' \end{tabular} $$ I' Hi & fb \end{tabular} $$ h' \end{tabular}$

5ggYgga Ybh' . 9ggUm

8YHJ]`g.

 $\label{lem:local-condition} $$H^[g]_g^hY'Z_bU^*UggYgga\ Ybhilug_^Zcf'UlhYbXUbW'di\ fdcgYg'': YYXVUW_']g'k\ f]hhYb'Wca\ a\ Ybhg'UbX'cf'U a\ Uf_]b['g\YYh]$

A U'cf'YggUmcb'U'_Ym'][ifY'cf'h\YaY']b'h\Y'WcifgY"

&&\$\$'k cfXg

5XX]h]cbU`XYhU]`g.

9ggUmh\Ya Yg'k]``VY'X]gW ggYX']b'h\Y'hi hcf]U'g'UbX']bghfi Whobg'k]``UddYUf'cb'A ccX'Y"

Hi fb]h]b'gYh]b[.'H\]g'Ugg][ba Ybh]g'gi Va]hhYX'h\fci [\'Hi fb]h]b'UbX'gh XYbhg'Xc'bchgYY'Hi fb]h]b g]a]'Uf]hmfYdcfhg"

		5fY'h\YfY'k Umg'hc'fYg]ghB'J]Yk g'Vm'@ci]g'5`h\i ggYfž
		>i X]h\ '6i hYfžUbX'ch\Yfg"
	Hi hcf]U`	@YWi fY h\Ya Yg'UbX'5 h\i ggYffg'hYl h'
	FYUX]b[@ci]g:5`h\iggYf.''⇒XYc`c[mUbX'⇒XYc`c[]WU`GHUHY 5ddUfUhigYgfi
	Cb`]bY'5WMjj]hm	K UHWX 'h\Y 'Z]`a 'H\Y '7 % dcfUH % bž'UbX'dUff]WjdUHY %]b 'Ub'cb`]bY 'X]gW' gg]cb'UVci h`]H' '8 YHJ]`g'hc'VY]ggi YX'cb'A ccX`Y"
K_YY_"+."%&">i `m!"%*">i `m	@Y\\\h fY	DgnWX.cUbU`mg]g`UbX`gcW]U```]ZY

Fygci fWyg

DfYgWf]VYX F Ygci fWYg

 $\label{eq:hammer_hammer} H\Y'k\YY_`mfYUX]b[\ g'k\]```VY'UWWgg]V`Y'fh`fci\ [\ \ `A\ ccX`Y''$

FYWca a YbXYX FYgci fWYg

 $5\,\widehat{\ \ }]ghcZ\overline{\ \ }fh\ YffYUX]b[\ \ k\]\widehat{\ \ }VY\,Uj\ U]UVY\,cb\,A\ ccXY''$

7 ci fgY '9j U'i Uh]cb 'UbX '8 Yj Y`cda Ybh

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

☐ Interpretation of the property of the p

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=hWJbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

• i bXYfgHJbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbh'Uhil BGK

5 WUXYa]W±bZcfa Uh]cb

: cf'YggYbhJU`'gh XYbh']bZcfa UhJcb'fY`UhJb['hc.

- fYei Yghg 'Zcf'Yl hYbg]cb/
- `UhY`gi Va]gg]cbg`[i]XY`]bYg/
- fYi]Yk 'cZa Uf_g/
- I BGK '< YU'h\ 'UbX'GUZYhm'dc`]\\\Yg/
- YI Ua]bUh]cb dfcWYXi fYg/
- gdYWJU`Wcbg]XYfUHjcb`]b`H\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybh fY/
- gh XYbhYei]miUbX'X]qUV]`]m/
- UbX'ch\Yf'YggYbhJU`'UWUXYa]W]bZcfa UhJcbz'gYY

\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa]W]bZcfa Uh]cb#dfchcWc`g![i]XY`]bYg#

.

⇒a U[Y'7fYX]h

5 fcmU`hmiZfYY`d]Wfi fY`Zfca kkk"d]l UVUm'Wca

7F = 7CG

7F = 7CG Dfc|]XYf 7cXY. \$\$\$-,;

5W_bck `YX[Ya YbhcZ7ci bhfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb : `W ghc X]Ubg : c Z : h, Y ``UbXg : cb : k \]WX : I B G K ? Ybg]b[hcb : WUa di g :]g ``c WUhY X''$