

IEST5003

5XXfYgg]b['9bj]fcba YbHJ``≢ggi Yg. 'DUh\k Umg'hc'7\Ub[Y! A U_]b[

HYfa 'Hk c''#'&\$&%

7ci fgY⁻Cj Yfj]Yk

GHJZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWJhjcb	D\cbY
@Ui fU'A W@Ui WX`Ub	`Ui fU"a WUi W\`Ub4 i bgk "YXi "Ui	O	A cfj Yb 6fck b &* -	d`YUgY'i gY Ya U]`

GWXcc``7cbHJWhi±bZcfa Uh]cb

GWkcc`cZ<iaUb]hJYg'UbX'@Ub[iU[Yg

@c\\U||cb. G\\cc``C\\Z|\\\žA\cfj\Yb'6fck\b'6i]\X]b[\z'@\j\Y``&z'&),

CdYb]b['<ci fg. 'A cbXUm'! : f]XUmž - Ua '! ') da

D\cbY.'Ž*%'&'-',)'%*,%

: UI . 'Ž * %'&'-' ,) ', +\$)

9a U]`. '<u>\U`4 i bgk "YXi "Ui</u>

7ci fgY 8YW] g

7 fYX]hDc]bhg**

Gi a a UfmcZh\Y 7ci fgY

#b 'th]g 'Wti fgYz'mci 'k]```cc_'Uh\ck 'mci 'WUb'Udd`mth\Y'ZTUa Yk cf_g'UbX']bg][\hg'mci '\Uj Y'[U]bYX']b 'mci f dcgh[fUXi UhY'Ybj]fcba YbhUbX'gcW]Yhmghi X]Yg'hc'h\Y'Ybj]fcba YbhU`]ggi Yg'mci 'WUfY'UVci ha cgh''H\Y Wti fgY'i gYg'Ub']bhYfX]gW]d`]bUfmUddfcUW\']b'k\]W\'mci 'UfY'YbWti fU[YX'hc'UhYbX'hc'h\Y'Wta d`Yl]hmcZ Ybj]fcba YbhU`]ggi Yg'UbX'hc'XYj Y`cd'YZZYWfj Y'dfcdcgU`g'Zcf'UWfjcb'''K\]Y'h\Y'Wti fgY'hci W\Yg'cb'U'k]XY

5ggYgga Ybh

5ggYgga YbhHUg_g

5ggYgga Ybh'tUg_	K Y][\h	8iY'8UHY	Gh XYbh@YUfb]b[Ci hWca Yg 5ggYggYX
K YY_`mF YZYW¶cbg'	' \$1	Bch5dd`]WUV`Y	%ž'&ž''
7 UgY Ghi XmDfYgYbhUhjcb	&\$I	Bch5dd`]WUV`Y	' Ž'(
:]bU``F Ydcfhi) \$1	%&#\$, #&\$&%`\$*.\$\$`DA</td><td>%ž'&ž' ž')</td></tr></tbody></table>	

5ggYgga Ybh8YHJ]`g

5ggYgga Ybh% K YY_`mF YZYWh]cbg

GhUfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g.

 $K YY_`mg\cfhk f] h b gi a a Uf] Yg`Zcf`X] ghUbWh`UbX`cb! WUa di g`ghi XYbhg`z'k] h b g`cfhcb`] b Y`ZYYXVUW_`[] j Yb z Zcf'- 'k YY_g'r &) $'k cfXg'dYf'k YY_''$

5XX]h]cbU`XYhJ]`g.

H\fci [\ci hih\Y`Wci fgYz`mci `k]```dfcXi WY`g\cfhfYZYWf]cbg`U]a YX`hc`XYYdYb`mci f`Yb[U[Ya Ybhik]h\`k \Uh mci `\Uj Y``YUfbYX`]b`h\Y`A 9A `UbX`hc`YbWci fU[Y`mci `hc`XYj Y`cd`mci f`WfYUh]j]hmUbX`g_]```]b`Udd`m]b[`mci f`YUfb]b[g`hc`fYU`!`]ZY`g]hi Uh]cbg"`Mci `k]```dcghimci f`fYZYWf]cbg`cb`A ccX`Y`YUW\`k YY_'h\Y`XUm`VYZcfY`WUgg"

Hi fb]hjb gYhjb[. H\]g]g bchU Hi fb]hjb Ugg][ba Ybh

5ggYgga Ybh& 7UgY Ghi XmDfYgYbhUh]cb

GhUfhXUhY. Bch5dd`]WUV`Y

8YW]`q.

'\$ a]bg`WUgg`dfYgYbfUf]cb`cf`Zcf`X]gfUbWf`cbY`k YY_``YUX]b[`Ub`cb`]bY`Zcfi a "`K f]ffYb`[fci d`ZYYXVUW_`k]`` VY`[]j Yb"

5XX]h]cbU`'XYhU]`q.

H\]g`Ugg][ba Ybhk]``YbWti fU[Y`mci 'hc`i gY`h\Y`a cghfY`Yj Ubhih\Ycf]Yg`Zfca 'h\Y`Wti fgY`fYUX]b[g`hc UbU`mgY`UbX`YI d`U]b`Ub`Ybj]fcba YbhU``]ggi Y`mci 'UfY`dUgg]cbUhY`UVci h'`9UW\`[fci d`ftf`]bX]j]Xi U`ž XYdYbX]b['cb'bi a VYfgŁ'k]```VY`[]j Yb'h\Y`fYUX]b[g`Zfca 'U'dUfh]W``Uf`k YY_`UbXž`]b`h\Uhk YY_ž'k]```YUX`U ZcW gYX`X]gW gg]cb'Udd`m]b['cbY`cf'hk c'WtbW'dhg`Zfca 'h\Y`fYUX]b[g`hc`U`WUgY`ghi XmcZh\Y]f`W\c]WY"`\db mci f`dfYgYbhUh]cbžmci 'k]```hYUW\`i g`h\Y`_YmY`Ya Ybhg`cZmci f`h\Ycfm\ZfUa Yk cf_`UbX`YbWti fU[Y`h\Y`WUgg

hc fYZYWicb k \Uh]h\Y`dg h\Ya hc gYY`]b h\Y WUgY gh Xm'

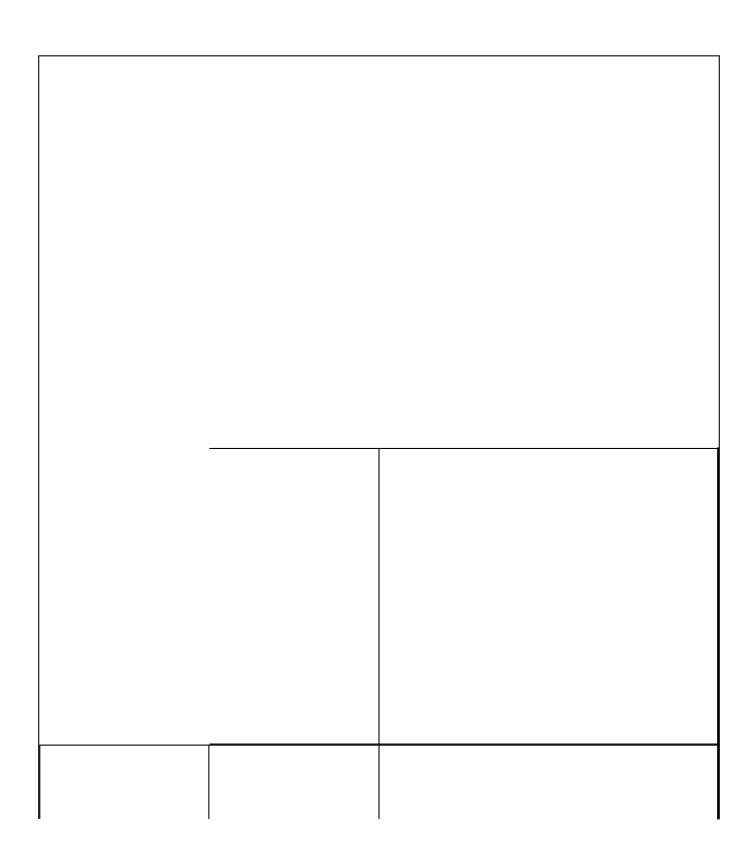
 $\label{eq:higher_problem} \mbox{Hi fb]h]b gYhh]b[. H\]g]g]bchUHi fb]h]b Ugg][ba Ybh$

5ggYgga Ybh' . :]bU`F Ydcfh

8YHJ]`g.

Ghi XYbhgʻk]``VYʻfYei]fYXʻhcʻgi Va]hiUʻ&\$\$\$`k cfXʻZ|bU`ʻfYdcfhVUgYXʻcbʻ]bj Ygh][Uh]cb#JbU`mg]gʻcZUb Ybj]fcba YbhU`]ggi YʻcZh\Y]f`VXc]WY"

 $\label{eq:Karlowskin} \text{K f]} \text{hh} \text{Yb} \text{`Z} \text{Y} \text{X} \text{VU} \text{W} \text{`k} \text{]```} \text{V} \text{Y} \text{`[]} \text{j} \text{Yb} \text{"}$



	#Dih\]gigYa]bUfžkYik]````cc_'Uhih\Y'Ufh'UbX'gW]YbWYcZW\Ub[Y'aU_]b["' <ck 'xc'ky'gi="" fgy`j="" fiz]bu`fydcffgžky'k]``gdyw]z\wj`m`cc_'uhw\ub[y!au_]b['ubx'ug_]b['\ckuwjxya]\wgh="" ghj]bici="" th="" u_]b["'<ck="" x]yg'ubx'fygyufw\!]bzcfayx'kcf_'wub<="" ygk\]\ubx'k\m3'k\uh]giu'h\ycfmczw\ub[y'ubx'k\mxcyg]hauhfyf3'k\]h\'ub'ymy'hc'mci="" ygk\]ya=""></ck>
K YY_', .'%-'>i `m!'&' '>i `m	

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb['hc'gi va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]h]bž'd'YUgY

Hy'Yd\cby'9| hy'fbu''Gi ddcfhcb'-',) '' ' ' %cf'Ya U]''h\Ya 'cb'Y! hy'fbu'hy'hgi ddcfh4 i bgk "YXi "Ui "''Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
UfY'i bUV'Y'hc'gi va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a Um'Udd'mZcf'Ub'Y! hy'bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbU''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' 'hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbU''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfZ'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va]hUgg][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=iWUbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i

- i bXYfglUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbhUhi BGK
- VY 'Uk UfY 'cZd`U[]Uf]ga ž Wcdmf][\hzi BGK 'Ghi XYbhi 7 cXY 'cZ 7 cbXi WhUbX '5 WW dhUV 'Y 'I gY 'cZ I BGK '=7 H'F Ygci fW g'Dc`]Wh
- VY'Uk UfY'cZh\Y'ghUbXUfXg'cZVY\Uj]cif'YldYWhYX'cZYjYfmcbY']b'h\Y'l BGK 'Wcaaib]hm

.

5 WUXYa]W±bZcfa Uhjcb