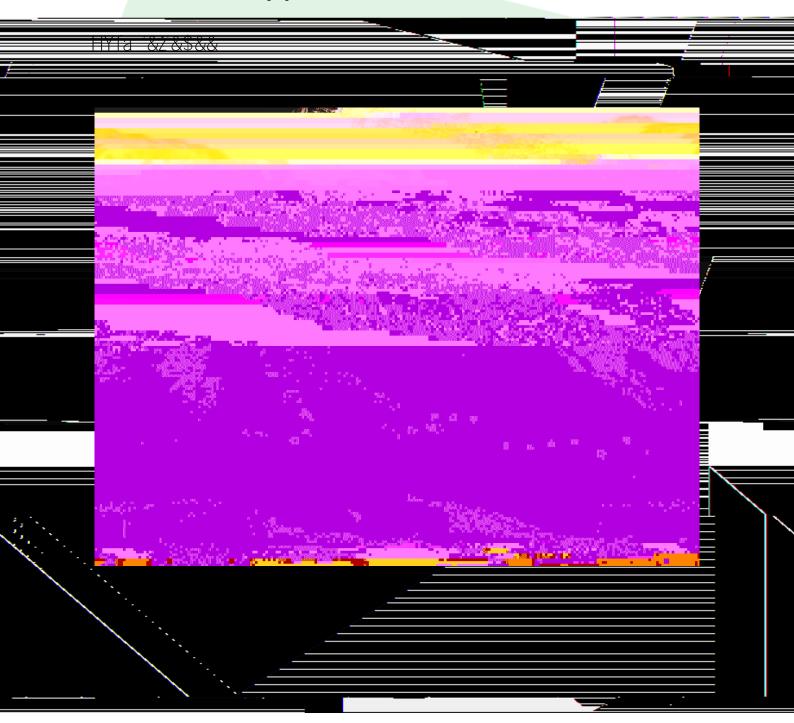


ARTS2486

H\Y': fYbW\'GdYU_]b['K cfX



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GHJZ7cbHJWh8YHJ]`g

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@c\\U||cb. G\\cc`C\\Z|\\\žA cfj\Yb'6fck\b'6i]\X]b[\\ž@Yj\Y``&\\z\&),

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9a U]`. \<u>U`4 i bgk "YXi "Ui</u>

5W_bck `YX[Ya YbhcZ7ci bhfm

I BGK '5frgž8Yg][b'UbX'5fW,]hYWi fY'? Ybg]b[hcb'UbX'DUXX]b[hcb'Wa di gYg'UfY'Vi]'hcb'5Vcf][]bU`@UbXg"'K Y'dUmci f'fYgdYWg'hc'h,Y'6]X'][U''UbX'; UX][U''dYcd'Yg'k \c'UfY'h,Y'7 i ghcX]Ubg'cZh,YgY'`UbXg" K Y'UW_bck `YX[Y'h,Y'5Vcf][]bU`'UbX'HcffYg'GhfU]h=g`UbXYf'dYcd'Ygž'h,Y':]fghi5i ghfU`]Ubgžk \cgY'`UbXgž k]bXg'UbX'k UhYfg'k Y'U``'bck 'g\UfYž'UbX'dUmfYgdYWhc'h,Y]f'i b]ei Y'j U'i Ygž'UbX'h,Y]f'Wbh]bi]b['UbX YbXi f]b['W' h fYg'k \]W. XYYYdYb'UbX'Ybf]W. h,Y'`]ZY'cZci f'bUh]cb'UbX'Wca a i b]h]Yg"''

 $\label{eq:continuity} $$ = U[Y'Wc'ifhYgmicZh\Y'CZh\Y'Dfc'J]WY!7 \setminus White $$ (Y'bc'ig'] BGK $$ fig' + X][Ybc'ig'ghfUhY[m'] $$ (Y'bc'ifhYgmicZh\Y'CZh\Y'Dfc'J) $$ (Y'bc'ifhYgmicZh\Y'Dfc'J) $$ (Y'bc'ifhYgmicZh\Y'CZh\Y'Dfc'J) $$ (Y'bc'ifhYgmicZh\Y'Dfc'J) $$ (Y'bc'ifhY$

7ci fgY 8YHJ] g

$I b h c Z 7 f Y X h^*$

Gi a a UfmcZh\Y 7ci fgY

♣ 'h\]g 'Wci fgYzghi XYbhg'k]```\Uj Y'h\Y'cddcfhi b]hmhc'X]gWcj Yf'h\Y'W'bhfU`]hmcZh\Y': fYbW\ ``Ub[i U[Y']b ZfUa]b[': fYbW\]XYbh]hmz'UbX'hc'Yl d`cfY'h\Y'W ffYbhghUh g'cZh\Y': fYbW\ ``Ub[i U[Y']b gcW]Yh]Yg'UbX]bgh]hi h]cbg'Ufci bX'h\Y'k cfX"'H\]g 'Wci fgY'k]``'dfcj]XY'ghi XYbhg'k]h\ 'Ub'cj Yfj]Yk 'cZh\Y'\]ghcfmcZh\Y : fYbW\ ``Ub[i U[Y'Zfca ']hg'cf][]b'hc'h\Y'WcbhYa dcfUfmdYf]cX'flYZfcfhg'hc'WcX]Zmh\Y'`Ub[i U[Y'k]``'fYWl']j Y dUff]W `Uf'UhHYbh]cbtZ'UbX'k]h\ 'Ub'cj Yfj]Yk 'cZh\Y'UWhi U'`X]j Yfg]mcZ: fYbW\ ']b': fUbW''UbX'UbX'UbX'\h\Y k cfX'f]b'h\Y'5a Yf]WUgz']b'5Zf]WU'UbX']b'9i fcdYtz']bWi X]b['h\Y'DUW]ZJWUbX'+bX]Ub'C WYUb'fY[]cbg'fcZ]W]U`dc`]W]Yg'hc'UggYfhh\Y'ghUh' g'cZ: fYbW\ ']b'h\Y'k cfX'k]``fYWl']j Y'dUffl]W `Uf'UhHYbh]cbt''5j Uf]YhmcZk f]hHYb UbX'Ui X]c!j]gi U``a UhYf]U'g'k]```VY'i gYX'hc']``i ghfUhY'h\Y'`YWhi fYg"

7 ci fgY @YUfb]b[Ci hWca Yg

%" 8 YgWf]VY h\Y a U]b ghU[Yg cZh\Y \\]ghcf]WU``Yj c`i h]cb cZ: fYbWX
&" &" F YWc[b]nY h\Y j Uf]ci g Zcfa g cZ: fYbWX h\ Uh'UfY W ffYbhmgdc_Yb j]b h\Y k cfX
' " ' " I gY 'U'gYhcZWcbWhdhg gdYWJZ]Whc h\Y X]gWJd`]bY gi W\ 'Ug 'GhUbXUfX': fYbWX žWfYc`Y 'UbX'X][`cgg]U
(" (" 8]gW gg 'UbX fYZYWhcb \ck h\Y Yj c`i h]cb 'UbX'h\Y 'W ffYbhghUh g cZ: fYbWX ``Ub[i U[Y fY`UhYg hc gcW]cdc`]h]WJ``]ggi Yg
) ") " 7 ca dUfY h\YgY'd\Ybca YbU'k]h\ 'h\Y g]hi UhJcb cZmci f'ck b ``Ub[i U[Y

HYUWX]b[GhfUhY[]Yg

H\Y`Wci fgY`]g`XYg][bYX`fc`ZUW]]hUfY`f\Y`XYj Y`cda YbficZU`gW\c`Uf`mUbX`Wf]hJWU``i bXYfgfUbX]b[`cZf\Y Yj c`i f]cbžYl dUbg]cb`UbX`W ffYbfigfUfi g`cZ: fYbW\`]b`f\Y`k cf`X"`H\Y`WcbfYbfi]g`f]W\`]b`]bZcfa Uf]cb`UVci h f\Y``Ub[i U[Y`UbX`]h'UXXfYggYg`WcbfYa dcfUfmgcW]YhU``]ggi Yg`cZfY`Yj UbW'`Zcf`: fYbW\`gfi XYbfg`]b dfcZYgg]cbU``UbX`X]gW[d`]bUfmZ]Y`Xg"

±0Wi g]j Y`hYUW\]b['ghfUhY[]Ygž'Ui X]c!j]gi U``gi ddcfhUbX`dYYf`Wc``UVcfUh]cb'U]a 'UhYb[U[]b['ghi XYbhg`]b YUfb]b['h\YgY`WcbhYbhg''5 'fUb[Y`cZUggYgga YbhhUg_g'UfY 'gYhhc'gi ddcfhh\Y`UW\]Yj Ya YbhcZ_Ym

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&"`C fU``X]gW gg]cb	&\$I	8]gW gg]cb Xi f]b['hi hcf]U'g. VYhk YYb k YY_'&'UbX') ž 7 f]h]WJ`'fYZYWf]cb Xi Y'Vm) da 'cb'h\Y'XUmcZh\Y'hi hcf]U' X]gW gg]cb"	' Ž'(
' "; fci d'dfYgYbHJh]cb	&\$I	F YWcfXYX j]XYc dfYgYbhUh]cb Xi Y Vm) da lk c XUmg fcb K YXbYgXUmcVYZcfY h\Y h hcf]U`X]gW gg]cb cZh\Y j]XYc dfYgYbhUh]cb Xi f]b[h hcf]U`g k YY_g', hc %\$"	&ž (
("::]bU``YggUm	(\$1	%) #\$, #&\$&&`\$) .\$\$`DA	(ž)

5ggYgga Ybh'% 'HYgh

5ggYgga Ybh`Yb[h\.`WU"'() 'a]bi hYg 8i Y`XUhY.`&\$#\$*#&\$&&fK YY_'(Ł

CbY']b!WUgg'ei]n'WejYf]b['h\Y'WebhYbhcZh\Y'WeifgY'k]``'hU_Y'd`UWY'Xif]b['h\Y''YWffYgž'WU''() a]bihYg"

: YYXVUW_j jUjb!WUggX]gW gg]cbUbXWcffYWgcbcZhYgh"

H\]g]g bchU Hi fb]hb Ugg][ba Ybh

5XX]h]cbU`XYhJ]`g

 $\label{thm:condition} $$HY'HYghVUgYX'cb'hYbhcZhY'a UhYf]U``Wcj YfYX'k]``VY'XcbY'cb`]bY'j]U'U'h]a YX'A ccX`Y'E i]n Xi f]b['h\Y']fgh\ci f`cZh\Y'`YWfi fY''$

5ggYgga Ybh& CfU`X]gW gg]cb

5ggYgga Ybh`Yb[h\. *\$\$ k cfXg

8i Y`XUhY. '8]gW gg]cb`Xi f]b['hi hcf]U`g. 'VYhk YYb`k YY_'&'UbX`) ž'7 f]h]WU``fYZYWf]cb`Xi Y`Vm) 'da 'cb`h\Y`XUm cZh\Y`hi hcf]U``X]gW gg]cb"

Ghi XYbhg`dfYgYbhU`Wf]hJWU``UbU`mg]g`cZcbY`UfhJWY#cd]WždfYdUfY`ei YghJcbg`hc``YUX`U`hi hcf]U``X]gW gg]cbžUbX`k f]hY`U`Wf]hJWU``fYZYWfJcb`fWU"`*\$\$`k cfXgŁ"

: YYXVUW_'j]U']b!WUgg'X]gW gg]cbž'Ug'k Y```Ug'k f]ffYb'ZYYXVUW_'cb'a Uf_g\YYff'

.

H\]g`Ugg][ba Ybh]g`gi Va]hhYX`h\fci [\'Hi fb]h]b`UbX`ghi XYbhg`Xc`bchgYY`Hi fb]h]b`g]a]`Uf]hmfYdcfhg"

5XX]h]cbU`XYhU]`g

H\Y`hi hcf]U```YUXYfg\]d`X]gW gg]cbg`k]```H_Y`d`UW'`Xi f]b['h\Y`hi hcf]U``fWYhk YYb`k YY__'&`UbX`) Ł"`H\Y [fci d]b[g`k]```VY`Wcbghhi hYX`Xi f]b['k YY__'%''H\Y`Ufh]WYg`k]```VY`Uj U]`UV`Y`j]U`A ccX`Y''

5ggYgga Ybh'; fci d dfYgYbhUh]cb

5 ggYgga Ybh`Yb[h.; fci d'dfYgYbhUh]cb.') 'a]bi hYg'dYf'ghi XYbh
Gi Va]gg]cb'bchYg. 'Gi Va]gg]cb'cZj]XYc'j]U'A ccX'Y
8 i Y'XUhY. 'F YWcfXYX'j]XYc'dfYgYbhUh]cb'Xi Y'Vm) 'da 'hk c'XUmg'fbb'K YXbYgXUmŁ'VYZcfY'h\Y'hi hcf]U`X]gW gg]cb'cZh\Y'j]XYc'dfYgYbhUh]cb'Xi f]b['hi hcf]U`g. 'k YY_g', 'hc'%\$"

Gh XYbhg k]``YUW Webhf]Vi hY he 'U'%) a]b [fci d'dfYgYbhUh]cb eb 'U'hed]WfY Yj Ubhhe 'h Y Wei fgYžgi [[YghYX Vmh\Y Webj Ybef"

 $: YYXVUW\underline{\quad \ \ } \]U^*]b!WUgg^*X]gW^*gg]cb\check{z}^*fi\ Vf]Wg^*UbX^*]bX]j\]Xi\ U^*k\ f]MYb^*Wca\ a\ Ybhg^*cb^*U^*a\ Uf\underline{\quad } g\backslash YYh^*$

H\]g]g bchU Hi fb]hb Ugg][ba Ybh

5XX]h]cbU`XYhU]`g

H\Y'%) 'a]b"'[fci d`cfU`dfYgYbhUh]cb`fUVci h') 'a]b"'dYf`gh XYbhŁ'k]```VY`gi Va]hhYX`j]U`J c]\W`H\fYUX`]b`h\Y \Zcfa `cZU`j]XYc`dfYgYbhUh]cb`fl gi U``m`]b`h\Y`\Zcfa `cZU`bUffUhYX`dck Yfdc]bhŁ`h\Y`fY\\f\]b[`f]\b`a d(`cf Yei]j U`YbhŁ'hc`VY`gi Va]hhYX`Vm) da `hk c`XUmg`VY\ZcfY`h\Y`h\ rh hcf]U``XUmf]"Y"\Z`gi Va]gg]cb`cb`K YXbYgXUm\Z`) da \L/U```gh XYbhg`g\ci `X`k Uh\X`h\Y`j]XYc`dfYgYbhUh]cbg`UbX`dfYdUfY`ei Ygh]cbg`\Zcf`h\Y`X]g\W gg]cb`U\Vci h\\Y`dfYgYbhUh]cb`Xi f]\b[`h\Y`h\pcb`Xi f]\b[`h\pcb`Xi f]\b[`h

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5ggYgga Ybh``Yb[h\.`&\\$\$\$`k cfXg 8i Y`XUhY.`%) #\$, #&\$&&`\$) .\$\$`DA

:]bU``YggUmcZWU"'&ž\$\$\$'k cfXgž'k]h\`Uddfcdf]UhY'fYZYfYbVJb[ž'gi Va]hhYX'cb'Hi fb]hJb"

: YYXVUW_j]UFiVf]Wg UbX k f]MYb Wca a Ybhg cb Hi fb]h]b"

H\]g`Ugg][ba Ybh]g`gi Va]h\YX`h\fci [\`Hi fb]h]b`UbX`ghi XYbhg`Xc`bchgYY`Hi fb]h]b`g]a]`Uf]hmfYdcfhg"

5XX]h]cbU`XYhJ]`g

H\Y`YggUm]g`Xi Y`cb`9I Ua `k YY_"`A cfY`]bZc`cb`A ccX`Y"

	5ggYgga Ybh	CF5@DF9G9BH5H€B'f&\$i Ł'!'K 99? -'; FCIDG 8]gWgg]cb'Xif]b['hihcf]U`g
		3 jg v
K YY_'%\$.'%'5i [i gh!') 5i [i gh	@YWn fY	7 i ffYbh`]ggi Yg`UbX`W\U``Yb[Yg.': fYbW\']b`h\Y [`cVU``U[Y
		7cbWi g]cb
	FYUX]b[5XUa gcbžF "'f&\$\$+Ł"'@Ub[i U[Y'UbX']XYbh]mm" ±b. H\Y'XYZYbWY'cZ: fYbWX.'U'`Ub[i U[Y']b'Wf]g]g3'fd'" %)'!%*\$Łž7`YjYXcb.'A i `h]`]b[i U``A UhYfg"'
	5ggYgga Ybh	CF5@DF9G9BH5H€B'f&\$i Ł'!'K 99?'%\$; FCIDG
		8]gWgg]cb'Xif]b['hihcf]U'g

F Ygci fWYg DfYgWf]VYX F Ygci fWYg

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwci bhYf'U'dfcV'Ya k \Yb'UhYa dhJb['hc'gi Va]hmci f'Ugg][ba Ybht\fci [\'Hi fb]hJbž'd'YUgY

HY'Yd\cbY'9| hYfbU'`Gi ddcfhcb'-',) '' ' ' %cf'Ya U]`'h\Ya 'cb'Y! hYfbU'hY'hgi ddcfh4 i bgk "YXi "Ui '"'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUfŁ"'=Imci
UfY'i bUV'Y'hc'gi Va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\'Hi fb]hJb'mci 'a UmUdd'mZcf'Ub'Y! hYbg]cbž'Vi hmci
a i ghfYhJ]b'mci f'hJW_Yhbi a VYf'Zfca '9! hYfbU'`Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY'Yj UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj]XYbW'hc'gi ddcfhmci f'Y! hYbg]cb'Udd']WUhJcb"'=Imci 'Ya U]''9! hYfbU'`Gi ddcfhmci 'k]'`
Ui hca UhJWJ'`mfYWY]j Y'U'hJW_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k]'``bYYX'hc'gdYWJZJWJ'`mUg_'Zcf'cbY''
Hi fb]hJb'U'gc'dfcj]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hYf"

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

: cf']b \mathbb{Z} cfa Uh]cb'cb'\ck 'hc'gi Va]h'Ugg][ba Ybhg'cb`]bY'j]U'A ccX`Y. `\hhdg.##gh XYbh'i bgk "YXi "Ui \mathbb{A} ck! qi Va]h'Ugq][ba Ybha ccX`Y

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i=iWUbihU_Yia Ubm Zcfa gžZfca iXYi]VYfUhYiWXYUh]b[ihciUWW]XYbhU`mWcdm]b[iZfca iUigci fWYik]h\ci hiUW_bck iYX[Ya Ybh'i