

BIOM9021

A UghYfg Dfc YWhifk U`ZH]a YŁ

HYfa "H\fYY" ## "&\$&\$

7ci fgY^{*}Cj Yfj]Yk

GHJZZ:7cbHJWh:8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWUhjcb	D\cbY
A]WXUY``GhYjYbg	h\Yg]g"V]ca YXYb[4 i bgk "YXi "Ui			
: UhYa Y\'? Uf]a]	h\Yg]g"V]ca YXYb[4 i bgk "YXi "Ui			

GWXcc`7cbHJWh ≠bZcfa Uh]cb

Gh XYbhGYfj]WYg'WUb'VY'WcbHUWYX'j]U'<u>i bgk "hc#k YV7cfa g</u>

7ci fgY 8YW] g

7 fYX]hDc]bhg * *

Gi a a UfmcZh\Y 7ci fgY

 $6 + A - \$\&\%]g'h Y'gYWcbX' U'ZcZh Y'\%' I C7'f YgYUf W.' dfc YWf'' 6 + A - \$\&\$']g'h Y'Z]fgh 'U'Z'9bfc `a Ybh]bh YgY'Wcifg Yg'U'`ck g'U'ghi XYbhhc'i bXYfh U_Y'h Y'Yei]j U'Ybh cZ6 + A - - %('A Ugh Yfg'Dfc YWhcj Yf'h k cg Ygg]cbg'' F Ygi 'hg'Uf Y' [fUXYX'''$

 $H Y V C a YX W Y Y b [] b Y Y f] b [`A Ugh Y fg `Dfc Y W i U ``ck g `Wci fg Y k cf_ `A Ugh Y fg `gh X Y b hg `hc `Y | d Y f] Y b W `f Y g Y U f W f Y g Y U f W f Y g Y U f W f Y g Y U f Y f K] h \ Y `G W cc ``cf k] h `Wc ``U V cf U h b [`] b g h h h Y `G W c g d] h U g `U b X `7 G \ C \ " D f c Y W g U f Y g Y `Y W Y X 'V m h Y `gh X Y b h] b `Wc b g i `h U h j cb `k] h `U g i d Y f] g c f `Wc b X i W h b [`f Y g Y U f W `] b `U b `U f Y U `c Z] b h Y f Y g h h Y f Y g h k Y `gh X Y b h a i g h U f f U b `U f Y U h Y g h X Y b h a i g h U f f U b [Y Z c f U b `] b h Y f b U ` h c `h Y `G W cc ` \# b] y Y g] m z h Y `gh X Y b h a i g h U f f U b [Y Z c f U b `] b h Y f b U ` ; G 6 a 9 `Wc! g i d Y f j] g c f " U h Y D f c Y W g U f Y U g Y g g Y X `cb `h Y `V U g] g `c Z U `d f c Y W f Y d c f h] b `h Y `Z c f a U h c Z Y] h Y f `U `h Y g] g `c f `U `f Y g Y U f W X `d U d Y f `f Y U X m Z c f g i V a] g g] c b `h C `U `f Y Z Y f Y X `c i f b U `" D Y f Z c f a U b W `] b `h] g `Wc i f g Y `] g `[f U X Y X "$

 $H\ [g'Wc i fgY'Wc bh]bi Yg'h\ Y'k cf_'dfcdcgYX']b''6 \\ \ \ A-\$\&\$\check{z}'k]h\ 'h\ Y'c i hWc a Y'VY]b['U') \$\$\$'gW]Ybh]Z]W fYgYUfW.'dUdYf''$

7 ci fgY 5]a g

H\Y'6]ca YX]WU``9b[]bYYf]b['A UghYfg`Dfc YWf]g'cdYb'hc'Xi U``fZcfa Yf`miWcbWiffYbhz'XY[fYY'ghi XYbhg`k \c\Uj Y'gi WW'ggZi ``miWca d`YhYX'H\Yg]g'5ž'6'UbX'7ž'cf'dcgh[fUXi UhY'ghi XYbhg'Ybfc``YX']b'h\Y'A UghYfg'cZ 6]ca YX]WU``9b[]bYYf]b['Vm7ci fgYk cf_'fDfc[fUa 'WcXY', **\$L''

7ci fgY @YUfb]b[Ci hWca Yg

%" 9 j U`i UhY`UbX`Wf]hjWU``mfYj]Yk 'h\Y`gWjYbhjZjW`]hYfUhi fY &" K f]hY`U`gWjYbhjZjWfYdcfhUbX`Wca a i b]\WUhY`gWjYbhjZjWZjbX]b[g`hc`Ub`YXi WUhYX`Ui X]YbWY ' " 8 Yg][bž`WUffmci hž`UbU`mgY`UbX`fYdcfhcb`fYgYUfW\`hUg_g

HYUWX]b['GlfUhY[]Yg'

<u>@YUfb]b['UbX'hYUWX]b['UWfi]hYa</u>

H\Y`ghi XYbhik]```fY`mcb`XYj Y`cd]b[`Ub`]bXYdYbXYbhiUbX`Wc``UVcfUhjj Y``YUfb]b[`UddfcUWX"`F YgYUfWX ei Ygh]cbg`UfY`cZhYb`cdYb!YbXYX`UbX`\][\`mgdYW]U`]gYXž`gc`h\Y`ghi XYbhik]````YUfb`a cghiVmcbY!hc!cbY a Ybhcf]b[`dfcj]XYX`Vmh\Y`gi dYfj]gcf`UbX`h\Y]f`fYgYUfWX`hYUa "

<u>'91 dYWUhcbg'cZghi XYbha</u>

& a hamite hyfigi `athyrji Qlangafy ggya[YbhUfiycbih]a Y

X]h]cbU`7cifgY bZcfaUh]cg

 $\label{thm:continuous} $$H\YfY^{g'}g'bc'cZ_WU'''Wugg'ha Y'Zcf'h\]g'WcifgY'''Wci'a ighgh)``YbgifY'mcif'Ybfc`a Ybh'UbX'fY[]ghfUh]cb']g id'hc'XUhY']b'mcif'Ybfc`a Ybh''Mcif'ZUWY'hc!ZUWY'ha Y'bYYXg'hc'VY'cf[Ub]gYX'k]h\'mcif'gidYfj]gcfz'Ug'mciUfY'YIdYWYX'hc'a YYhh\'Ya 'Uh'YUghcbWY'dYf'k YY_"$

5ggYgga Ybh

 $H\Y'Z_bU''[fUXY'Z_cf'6 \\le A - $&\% \\le$

5ggYgga Ybh'HUg_g

5ggYgga Ybh'hUg_	K Y][\h	8i Y [.] 8UhY	Gh XYbh@YUfb]b[Ci hWca Yg 5ggYggYX
GWYbhZWA Ubi gWf]dh	, \$1	A cbXUmK YY_'%%	%ž [.] &ž [.] '

5ggYgga Ybh8YHJ]`g

5ggYgga Ybh% GWJYbhJZJWA Ubi gWf]dh

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\.') \$\$\$ k cfXg

8 YHJ]`g.

H\Y`cVYWIJ Y`cZh\]g`UggYgga Ybh]g`hc`WfYUHY`U`fYgYUfW\`a Ubi gWf]dhh\UhiWci `X`Zcfa `h\Y`VUg]g`cZU``ci fbU` Uff]WY"`D`YUgY`fYj]Yk `h\Y`XcW a Ybhg`cb`A ccX`Y#HYUa g`Zcf`Z fh\Yf`]bghfi Wl]cbg"`BchY`h\Uhih\YfY`]g`U`ghf]Wh k cfX``]a]hcZ) \$\$\$`k cfXg"

%" @|hYfUhi fY`fYj]Yk #VUW_[fci bX`UbX`di h]b['h\Y`fYgi `hg`]b`WcbhYl hif&\$\ \text{\Lambda} \text{\Lamb

Hi fb]hjb gYhjb[. H\]g]g bchU Hi fb]hjb Ugg][ba Ybh

FYgci fW/g

DfYgWf]VYX F Ygci fWYg

F Ygci fWgk]``VYa UXYUj U]`UVYhc`\Y`d'gh XYbhg'[i]XYh\Ya']b'h\Y]f'ci fbYmZcf'H\Yg]g'5"

91 hybg]cbg

 $\label{thm:condition} $$Mci 'WUb'Udd`m'Zcf'gdYWJU``Wcbg]XYfUhJcb'k \Yb']``bYgg'cf'ch\Yf'WJfW a ghUbW'g']bhYfZYfY'k]h\'mci f UggYgga Ybh'dYfZcfa UbW'''$

Ch\Yf'Udd`]\Wh]cbg`Zcf`YI hYbg]cb`cZgi Va]gg]cb`cZh\Yg]g`fYdcfhg`fY"["`Yei]da YbhVfYU_Xck bžYhWL

%" 8]gW gg 'h\Y 'dcgg]V]`]hmcZUb 'YI hYbg]cb 'k]h\ 'mci f 'gi dYfj]gcf 'Z[fgh'

'"FYeiYghaighVY`cX[YXVm**KYY_***cZhYfa"

("DUbY``XYW]q]cb'k]``'VY'a UXY'VmYbX'cZkYY_'+"

-) " H\Y`XYV][g]cb`k]``VY`a UXY`VmU`dUbY``—`Wcbg]gh]b[`cZh\Y`<cG`fcf`h\Y]f`bca]bYYŁž'H\Yg]g 7 ccfX]bUhcfž'UbX`%ch\Yf`dYfgcb"
- *" Ghi XYbhgʻg\ci `X'VY'U`YfhYX'hc'h\Y'ZJ\Whih\Uhih\]gʻ]gʻbch[i UfUbhYYXž'UbX'h\i gʻg\ci `X'bchfY`mcb [Yhh]b['Ub'YI hYbg]cb"
- +" Hmd]\W\D``m\overline{Y\] HYbg]cbg`UfY`[fUbhYX`ID`HC`'`kYY_g"`H\Y``Yb[h\`cZh\Y`YIhYbg]cb`bYYXg`hc`VYfYeiYghYX`UbX`^gh]\ZYX`Vmh\Y`gidYfj]gcf"`DUbY``k]```XYV\]XY`h\Y``Yb[h\`cZh]aY`[fUbhYX"

DfcWYXi fY]Z mci ZU]`

Ghi XYbhg`\Uj Y`h\fYY`cdh]cbg"`

%" fY!Ybfc`Zcf'6 € A - \$&\$# \$&%*bYk 'dfc YWhUbX'gi dYfj]gcf

- &" fY!Ybfc``Zcf'6€A-\$&%'U[U]b'k]h\`h\Y'gUaY'dfcYWh!'bYYXg'WcbgYbhcZUb'Uddfcdf]UhY'gidYfj]gcf/gh XYbh
- ' " Gh XYbhXcYgʻZ fh\Yfʻk cf_žʻfY!gi Va]hgʻh\Yg]gʻUZhYfʻUʻa UlʻcZ*ʻk YY_g"ʻ5agæWa Uf_ʻWUddYXʻUh)\$ı "'⊋gh]``bchgUh]gZUWcfmžʻh\YbʻbYYXgʻhcʻfY!Ybfc`"

 $H\g``Ughcdh]cb']g'cb`mUj\ U]`UV`Y']Zh\Y'cf][\]bU``a\ Uf_'k\ Ug'\ (\ \$\check{z}'C\ F']Zh\Y'ghi\ XYbh']g']b'h\Y]f'``UghgYa\ YghYf\ VYZcfY'[\ fUXi\ Uh]cb'ffY[\ UfX`Ygg'cZh\Y'cf][\]bU``a\ Uf_Ł''$

±DXi glfmVUgYX dfc YWbg

K Y'YbWci fU[Y'ghi XYbhg'hc'gYY_'dUffbYfg\]dg'k]h\`]bXi ghfmž'gc'ghi XYbhg'WJb'\Uj Y'U'Wc!gi dYfj]gcf'Zfca]bXi ghfm''< ck Yj Yfž']ZWcbZJXYbhJU`]mm]g'fYei]fYXž'U'WcbZJXYbhJU`X]gWcgi fY'U[fYYa Ybhff7 8 5 Ł']g'cV'][Uhcfm' H\Y'U[fYYa Ybhk]``dfchYWh\Y']bhY``YWh U`'dfcdYfmf][\hg'cZh\Y']bXi ghfmdUffbYfž'I BGK 'UbX'h\Y'ghi XYbh' Ghi XYbhg'cf'UWJXYa]Wg'UfY'bchUi h\cf]gYX'hc'g][b'WcbZJXYbhJU``X]gWcgi fY'U[fYYa Ybhg'cb'VY\U'ZcZ I BGK 'UbX'UfY'UXj]gYX'hc'hU`_hc'h\Y'Wci fgY'WccfX]bUhcf'UbX'I BGK '`Y[U`'cZZJWY'hc'UffUb[Y'Zcf'XfUZh]b[UbX'g][b]b['cZh\Y'WcbZJXYbhJU``X]gWcgi fY'cf'fYgYUfW\'U[fYYa Ybh'

<u>@UhY 'dfc WY Xi fY</u>

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

@UVcfUlrcfmfYdcfhg UbX a U/cf Ugg][ba Ybhg k]``fYei]fY U Bcb D`U[]Uf]ga '8 YWUfUh]cb '7 cj Yf 'G\YYh'

@UhY`gi Va]gg]cbg`k]```VY`dYbU`]gYX`%\$ı `cZh\Y`a Uf_`Zcf`YUW\`WU`YbXUf`XUm``UhY"'=Zmci `ZcfYgYY`U`dfcV`Ya]b`a YYh]b[`h\Y`bca]bUhYX`gi Va]gg]cb`XUhY`d`YUgY`WcbhUWh\Y`7 ci fgY`7 cbj Ybcf`hc`a U_Y`Ub`Uddc]bha Ybh hc`X]gW gg`mci f`g]hi Uh]cb`Ug`gccb`Ug`dcgg]V`Y"

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D@5; =5F €A

6Yk UfY"5b"Ugg][ba Ybhh\Uh']bWi XYg'd'U[]Uf]gYX'a UhYf]U``k]```fYWY]j Y'U'\$ı ': U]`ž'UbX'ghi XYbhg'k \c

5 WUXYa]W = 2cfa Uhlcb

7CI FG9'9J5@I 5H€B'5B8'89J9@CDA 9BH

Gh XYbhZYXVUW_`\Ug`\Y`dYX'hc`g\UdY`UbX`XYj Y`cd`h\]g`Wci fgYž]bWl X]b['ZYYXVUW_`cVhJ]bYX`Zfca 'cb! `]bY`Yj U`i Uh]cbg`Ug`dUfhcZl BGK 'g`Ug`dUfhcZl BGK 'g`a m9l dYf]YbWl`dfcWlgg"'Mci 'UfY`\][\`m YbWci fU[YX`hc`Wca d`YhY`gi W.`Ub`cb!`]bY`Yj U`i Uh]cb`hck UfX`h\Y`YbX`cZHYfa "': YYXVUW_`UbX`gi [[Ygh]cbg dfcj]XYX`k]```VY`]a dcfhJbh`]b`]a dfcj]b['h\Y`Wci fgY`Zcf`Z h fY`gh XYbhg"

.

85H9G'HC'BCH9

FYZYfihciA ml BGK iZcfi a dcfhUbhi8UhYgžiUj UjiUViYiUh \hdg.##a mii bgk "YXi "Ui #ghi XYbh#Ygci fWYg#! Ym8UhYg"\ha_i

.

57589A = 7.58J = 7.9

: cf]bZcfa Uh]cb UVci h

- "BchYg'cb'UggYgga Ybhg'UbX'd'U[]Uf]ga ž
- "GdYWW"7 cbg]XYfUhcbgž
- "GWkcc"Gh XYbh9h\]Wa'CZZWYfž'UbX
- ... 69GG

.

Gi dd'Ya YbhUfm'91 Ua]bUh]cbg.

Gi dd`Ya YbhUfm91 Ua]bUh]cbg`Zcf`HYfa '' '&\$&\$`k]``VY`\Y`X`cb`A cbXUmi%h\`>Ubi Ufm—': f]XUm'%) h\>Ubi Ufmf]bWi g]j YŁ'g\ci `X'mci 'VY`fYei]fYX`hc`g]hcbY"

= 2 U[Y'7fYX]h

GmbYf[]Yg]bGcibX&\$%*

7F = 7CG

7F = 7CG Dfc| XYf 7cXY. \$\$\$-,;

5W bck `YX[Ya YbhcZ7ci bhfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb : `W : ghcX]Ubg : cZh, Y ``UbXg : cb : k \]WX : I BGK ? Ybg]b[hcb : WUa di g :]g ``cWUhYX"$