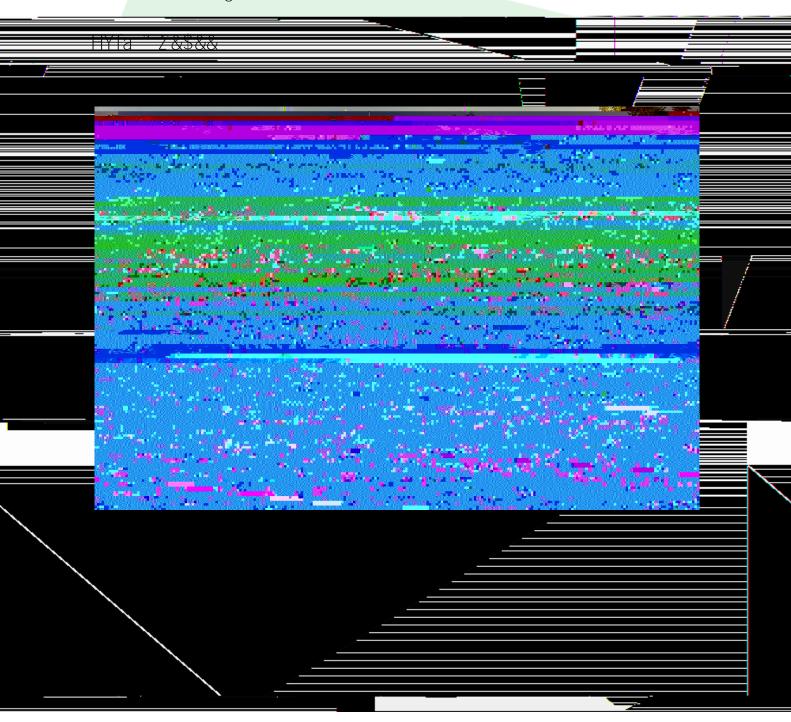


CVEN3202

Gc]~A YWXUb]Vg



7ci fgY Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g

7cbj Ybcfg

BUa Y	9a U]`	5j U]`UV]`]lm	@cWUh]cb	D\cbY
5fa Ub ? < C G < ; < 5@6	Ufa Ub" \cg\[\U`V4 i bgk "YXi " Ui	: f]XUmgʻZfca " 'da hc'(.'\$'da	79)\$'	

GW.cc`7cbHJWh =bZcfa Uhlcb

<u>9b[]bYYf]b['Gh'XYbhGiddcfhGYfj]WYg'-</u>'H\Y'BiWYig'!'Ybfc`a Ybhž'dfc[fYgg]cb'W\YW_gž'WUg\'fYei Yghgž WtifgY']ggi Yg'cf'dfc[fUa!fY`UhYX'ei Yf]Yg'

<u>9b[]bYYf]b['±bXi glf]U`'HfU]b]b[</u>'--'±bXi glf]U`'lfU]b]b['ei Ygl]cbg'

<u>I_BGK_'Gh_Xm5VfcUX</u>'--gh_XmUVfcUX'gh_XYbhYbei_]f]Yg^fZcf']bVci_bX'gh_XYbhgŁ'

I BGK '91 WXUb[Y'-ghi XYbhYl WXUb[Y'Ybei]f]Yg'flcf']bVci bX'ghi XYbhgŁ'

LBGK : i h fy Gh XYbh - dch bh U gh XYbh Ybei]f]Yg Y"["UXa]gg]cbgž ZYYgž dfc[fUa gž WfYX]h lf UbgZYf

D\cbY.

fŽ*%&Ł-',),)\$\$ - Bi WYi g Gh XYbh<i V

fŽ*%%&L'-',) '+**%'-'9b[]bYYf]b['=bXi ghf]U`'HfU]b]b['

fŽ*%"&&-',)" %+-'-1 BGK "Ghi Xm5VfcUX"UbX"1 BGK "91 WXUb[Y"fZcf"]bVci bX"ghi XYbhg&

7ci fgY 8YHJ] g

$I b hg c Z 7 f Y X h^*$

Gi a a UfmcZh\Y 7ci fgY

5b`]bhfcXi WhcfmWci fgY`hc`Z bXUa YbhU`g`cZgc]`a YWXUb]Wg"`Hcd]Wg`]bWi XY.`XYgWf]dh]cb`cZgc]`ž`VUg]Wd\UgY`fY`Uh]cbg\]dgž`WUma]bYfU`c[mž`WcbZ]bYX`UbX`i bWcbZ]bYX`gYYdU[Yždf]bW]d`Y`cZYZZYWfj Y`ghfYggž Wcbgc`]XUh]cb`h\Ycfmž`Wca dUWf]cbžghfYgg`X]ghf]Vi h]cb`UbX`gYhhYa YbhžA c\f`W]fWYž`ZU]`i fY`Wf]hYf]cbž ghfYb[h\`cZgc]`gžgc]``hYgh]b[žghfYgg!ghfU]b`VY\Uj]ci f`cZgc]`g`UbX`g`cdY`ghUV]`]hm'

7ci fgY⁻5]a g

 $\label{thm:linear} $$HY'cV'W''_jY'cZhY'W''_i fgY''_]g'hc'i bXYfgHUbX'hY'VUg]Wdf]bW''_d'Yg'cZgc]''a YW''Ub]Wg''UbX'hc'ghi Xm'hY'VVY\Uj]ci f'cZgc]''Ug'UbY'b[]bYYf]b['a UhYf]U'ž'Vch\'hYcfYh]WU''mfh\fci [\'YW'i fYgŁ'UbX'dfUW']WU''mfh\fci [\'UVcfUhcfmWUggYgŁ''']$

7 ci fgY @YUfb]b['Ci hWca Yg

5ZYYf'gi WWYggZi ``mWta d`Yh]b['h\]g'Wti fgYž'mci 'g\ci `X'VY'UV`Y'hc.

@YUfb]b['Ci HWca Y	95 GHJ[Y %7 ca dYHYbW]Yg	

5ggYgga Ybh

5ggYgga Ybh'tUg_		

<i fX`Y`fYei]fYa Ybh

I	I	l

		eVWbSYVfi
K YY_'*.'%+'CWvcVYf'! &%CWvcVYf	FYUX]b[Bc'@YWh fY'fl Yl]V]`]hmk YY_Ł
8/0 C WEVII		Bc'K cf_g\cd
K YY_'+.'&('CWcVYf'! &,'CWcVYf	@YWhifY	FUHY'cZWcbgc`]XUH]cbž'G\YUf'gHfYb[H\'cZgc]`g
a, c wevii		Ei]n'&fkYY_g'&'fc'('aUhYf]U`gŁ
		@UVcfUlrcfm' 'a cXi `Y'k]``'VY'fY`YUgYX"
		K cf_g\cd')
		DWWSeWaXWSd [`Y_aVgW'/DSfWaX Ua`ea{VSf[a`fi
K YY_', ." %C WcVYf!'(@YWhifY	G\YUf`ghfYb[h\`]b`gc]`g`fWcbh'lz`8]fYWng\YUf`hYgh
Bcj Ya VYf		K cf_g\cd [*]
		DWWSeWaXWSd[Y_aVgW(/?aZdZ5ag?a_T XS['gdWUdfWd[a`fi
K YY_''+'Bcj Ya VYf'!	@YWhifY	Hf]Ul]U``hYghž`GhfYgg`dUh\`hYW\b]eiY
₩Bcj Ya VYf		'@UVcfUhcfmi('a cXi 'Y'k]``'VY'fY`YUgYX"
		'K cf_g\cd'+
		DWWSeWaXWSd [Y _ aVg/W) /Fd[Sj [S^fWeffi
K YY_'%\$.'%('Bcj Ya VYf	@YWhi fY	G`cdY`ghUV]`]hm
!'%, 'Bcj Ya VYf		Ei]n" fk YY_g") hc", 'a UhYf]U`gŁ
		K_cf_g\cdg', 'UbX'-
		DWMSeWaXMSd [Y_aVgW*/E abWefST[{fkfi

FYgci fWyg

DfYgWf]VYX F Ygci fWYg

 $\label{thm:linear_continuous_problem} H\Y''HYI''HYCC_'Zcf''h\Y'Wci'' fgYž'cb''k \]WX''a cghicZh\Y'Wci' fgY''Dck YfDc]bhig`]XYg''UfY''VUgYX''UbX''WcbHJ]bg h\cfci [\'YI d'UbUh]cbg''UbX'XcnYbg''cZk cf_YX'YI Ua d'Ygž']g''gc'X'']b''h\Y'I BGK 'Vcc_g\cd.$

 $<c`mžF"8"ž?cjUWgžK"8"`UbX`G\YU\Ubž'H"7"`f&$\%\\\2"5b`\=bffcXiWf]cb`hc`;YchYW\b]WU``9b[]bYYf]b["žGYWcbX`9X]h]cb"\=bhYfbUh]cbU``9X]h]cb"\DYUfgcb"$

 $\label{thm:condition} $$HY'Zc``ck \]b[\ `fYZYfYbWY'Vcc_g'a\ UmiU`gc`VY'i\ gYZ\ ``Zcf`UXX]h]cbU``fYUX]b[\ \check{z}a\ UbmcZh\Ya\ `WUb`VY`Zci\ bX`]b h\Y'I\ BGK\ ``]VfUfm$

- ±DXfUfUlbUž'< Y]hcfž'UbX'J]bcXž''; YchYW\b]WU`DfcV`Ya g'UbX'Gc`i h]cbg'! 5 DfUW]WU`DYfgdYWhj Y"ž 7 F 7 'dfYqqž'&\$&\$
- 7 fU][ž'F ": "'"Gc] A YW Ub] Wq"ž 7 F 7 'df Y gqž & \$\%
- 8 Ugž 6 " A "ž "Df]bWd Yg cZ; YchYW\b]WU 9b[]bYYf]b["ž DK G di V]g\]b[ž % -,!&\$\$*
- @Ua VY`UbX`K \]ha Ubž'"Gc]``A YVXUb]Wq"ž'K]`Ymž'% +)
- 6UfbYgž'; "ž'"Gc]`A YWXUb]WgžDf]bWdYg"UbX'dfUWfWY"žDU`[fUjY'A UWA]``Ub/'fX'9Xž'&\$%%
- 6i X\i ž'A "ž"Gc] A YWXUb]Wq"UbX: ci bXUhcbq"žK]Ym/ Gcbqž&\$\$+
- Ga lh\ž=ž"Ga lh\'q"9"Ya YbhcZGc]"A YW\Ub|\Vq"\ž6`U\V_k Y\"\ž\&\$\$*

5`gczgh XYbhg'a Umzbx'h\Y'Gc]`A YW\Ub]Wg'6cc_VmDfcZJYffi]作]b'D8: Zfca.

\hd.#[Yc"] Yffi]^h"bYh#qcZhk UfY#Gc]`A YWX6cc_&\$%&"dXZ

7 ci fqY '9 j U`i Uh|cb 'UbX '8 Y j Y`cda Ybh

: YYXVUW_cb'h\Y'Wci fgY']g'[Uh\YfYX'dYf]cX]WJ``mi g]b['j Uf]ci g'a YUbgž']bWi X]b['h\Y'I BGK a m9I dYf]YbW''dfcW'ggž'UbX']bZcfa U``X]gW gg]cbg'UbX'ZYYXVUW_'h\fci [\ci h\Y'I\fa "'Mci f'ZYYXVUW_']g HU_Yb'gYf]ci g`mž'UbX'Wcbh]bi U``]a dfcj Ya Ybhg'UfY'a UXY'hc'h\Y'Wci fgY'VUgYXž']b'dUfhž'cb'gi W\'ZYYXVUW_"

@UVcfUhcfmK cf g\cd \(\pi\)Zcfa Uhlcb

Bc']b!dYfgcb``UVcfUhcfmWUggYg'h\]g'HYfa 'Xi Y'hc'h\Y``UVcfUhcfmfYZ fV]g\a Ybh'

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

D`YUgY`fYZYf`hc`h\Y`A ccX`Y`dU[Y`cZh\Y`Wci fgY`Zcf`Z fh\Yf`[i]XUbW\`cb`UggYgga Ybhigi Va]gg]cb"

I BGK `\Ug`U`ghUbXUfX``UhY`gi Va]gg]cb`dYbU`hmcZ

•)ı 'dYf'XUmž'Zcf'U``'UggYgga Ybhg'k \YfY'U'dYbU'hm'Udd`]Ygž'WUddYX'Uh'Zjj Y'XUmg'f1%&\$`\ci fg\z'UZhYf k\]WX'U'ghi XYbh\WUbbchgi Va]h'Ub'UggYgga Ybhž'UbX'bc'dYfa]hhYX'j Uf]Uh]cb"

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

6Yk UfY "5b" Ugg][ba Ybhh\Uh]bWi XYg"d`U[]Uf]gYX"a UhYf]U``k]```fYWY]j Y"U"\$ı ': U]`žUbX`ghi XYbhg`k \cd"\U[]Uf]gY\"a UmZU]``h\Y'Wci fgY"'Ghi XYbhg`k \cd"\U[]Uf]gY\"UfY\"U`gc"`]UV`Y'hc"X]gW]d`]bUfm'UWf]cbž]bWi X]b[YI Wi g]cb'Zfca 'Ybfc`a Ybh'

 $D`U[]Uf]ga ~]g'hY'i gY'cZUbch\Yf'dYfgcb'g'k cf_'cf']XYUg'Ug']Zh\Ymk YfY'mci f'ck b'''K ~Yb']h]g'bYWYggUfmcf XYg]fUV'Y'hc'i gY'ch\Yf'dYcd'Y'g'a UhYf]U`'mci 'g\ci `X'UXYei UhY`mUW_bck `YX[Y'k \cgY'k cfXg'cf']XYUg'h\Ym$

5 WUXYa]W = DZcfa Uhjcb

:]bU`'9l Ua]bUh]cbg.

:]bU`YI Ua g`]b`H' `&\$&&`k]```VY`\Y`X`cb`]bY`VYlk YYb`&) h\`Bcj Ya VYf`!`, h\`8YWYa VYf`&\$&&`]bWi g]j Yž`UbX gi dd`Ya YbhJfmYl Ua g`VYlk YYb`- h\`!`% h\`>Ubi Ufm&\$&' `]bWi g]j Y"'Mci `UfY`fYei]fYX`hc`VY`Uj U]`UV`Y`cb h\YgY`XUhYg"`D`YUgY`Xc`bchhc`a U_Y`UbmdYfgcbU``cf`lfUj Y``UffUb[Ya Ybhg`Xi f]b[`h\]g`dYf]cX"'

57589A = 7.58J = 7.9

- ? YmiGtUZztc '7 cbtUWiZcf '5 WUXYa]W5 Xj]WY flc[']b 'k]th 'mci f 'n=8 'UbX dUggk cfXt '\text{htdg.#|btfUbYtiW| Yb["i bgk "YXi "Ui # YmlgtUZItc!WcbtUWiXi f]b[!mci f!gti X]Yg!Utli bgk
- <u>? Ymil_BGK_'8 UhYg'</u>! 'Y["'7 Ybgi g'8 UhYžYI Ua 'XUhYgž``UghiXUmhc 'Xfcd'U'Wci fgY'k]h\ci h UWUXYa]\#Z|bUbW]U```]UV]`]miYhW''
- 7 J 9B 'Ghi XYbhi=bhfUbYhrflc[']b 'k]h\ 'mci f'n=8 'UbX dUggk cfXŁ '\hadg.#|bhfUbYh'W| Yb["i bgk "YXi "Ui #ahi XYbh]bhfUbYh'
- Gh XYbh@ZY 'Uh7 J 9Bž]bWi X]b['Gh XYbh GcW]Yh]Yg. \(\frac{1}{2} \) Htdg. #k k k "i bgk "YXi "Ui #Yb[]bYYf]b[#M] \(\frac{1}{2} \)! UbX!Ybj]fcba YbHU\!Yb[]bYYf]b[#gh XYbH\]ZY \(\frac{1}{2} \)
- GdYV)JU``7 cbg]XYfUhjcb. \https://https://www.https://https://https://https://https://www.https://ht

5ddYbX]l. '9b[]bYYfg'5i glfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWm GHJbXUfX

Dfc[fUa '±bHYbXYX'@YUfb]b['Ci HWca Yg	
?bck `YX[Y`UbX`g_]```VUgY	
D9%"%7ca dfY\Ybg]j YžfNYcfmVUgYX'i bXYfgHJbX]b['cZfNY'i bXYfd]bb]b['bUhi fU`'UbX d\mg]WJ`'gWJYbWYg'UbX'h\Y'Yb[]bYYf]b['Z bXUa YbHJ`g'Udd`]WJV`Y'hc'h\Y'Yb[]bYYf]b['X]gWJd`]bY	
D9%"&"7cbWYdh U``i bXYfgHJbX]b['cZh\Y'a Uh\Ya Uh]Wgžbi a Yf]WJ``UbU`mg]gžgHJh]gh]WgžUbX Wca di hYf`UbX`]bZcfa Uh]cb'gW]YbWYg'k\]W\'i bXYfd]b'h\Y'Yb[]bYYf]b['X]gW]d`]bY	
D9%" '=b!XYdh\'i bXYfgHJbX]b['cZgdYW]U`]ghVcX]Yg'cZ_bck `YX[Y'k]h\]b'h\Y'Yb[]bYYf]b[X]gW]d`]bY	
D9%"('8]gWfba YbhcZ_bck `YX[Y`XYj Y`cda YbhUbX`fYgYUfW\`X]fYWf]cbg`k]h\]b`h\Y Yb[]bYYf]b['X]gW]d`]bY	
D9%") '? bck `YX[Y`cZYb[]bYYf]b['XYg][b`dfUWf]WY`UbX`WcbhYl hi U``ZUWhcfg`]a dUWf]b['h\Y Yb[]bYYf]b['X]gW]d`]bY	
D9%"* I bXYfgHJbX]b['cZh\Y'gWcdYž'df]bW]d`Ygž'bcfa gž'UWVci bHJV]`]h]Yg`UbX`Vci bXg`cZ gi gHJ]bUV`Y`Yb[]bYYf]b['dfUW]WY`]b`h\Y`gdYW]Z]WX]gW]d`]bY	
9b[]bYYf]b['Udd`]WUh]cb'UV]`]hm	
D9&"%5dd`]WUh]cb`cZYghUV`]g\YX`Yb[]bYYf]b[`a Yh\cXg`hc`Wca d`Yl `Yb[]bYYf]b[`dfcV`Ya gc`j]b[
D9&"&": `i YbhiUdd`]\WJh]cb'cZYb[]bYYf]b['hYVXb]ei Ygž'hcc`g'UbX'fYgci f\Wg	
D9&" '5dd`]WUh]cb`cZgmghYa Uh]WYb[]bYYf]b['gmbh\Yg]g'UbX'XYg][b'dfcWYggYg	
D9&"('5dd`]WUh]cb'cZgmghYa Uh]WUddfcUVXYg'hc'h\Y'WcbXi WhUbX'a UbU[Ya YbhcZYb[]bYYf]b[dfcYWng	
DfcZYgg]cbU`'UbX'dYfgcbU`'UHff]Vi HYg	
D9' "%'9h\]WU`'WcbXi WiUbX'dfcZYgg]cbU`'UWWci bHJV]`]hm	
D9' "&'9ZYWNjjY'cfU`'UbX'k f]hhYb'Wcaaib]WUhjcb']b'dfcZYgg]cbU`'UbX'`Um'XcaU]bg	