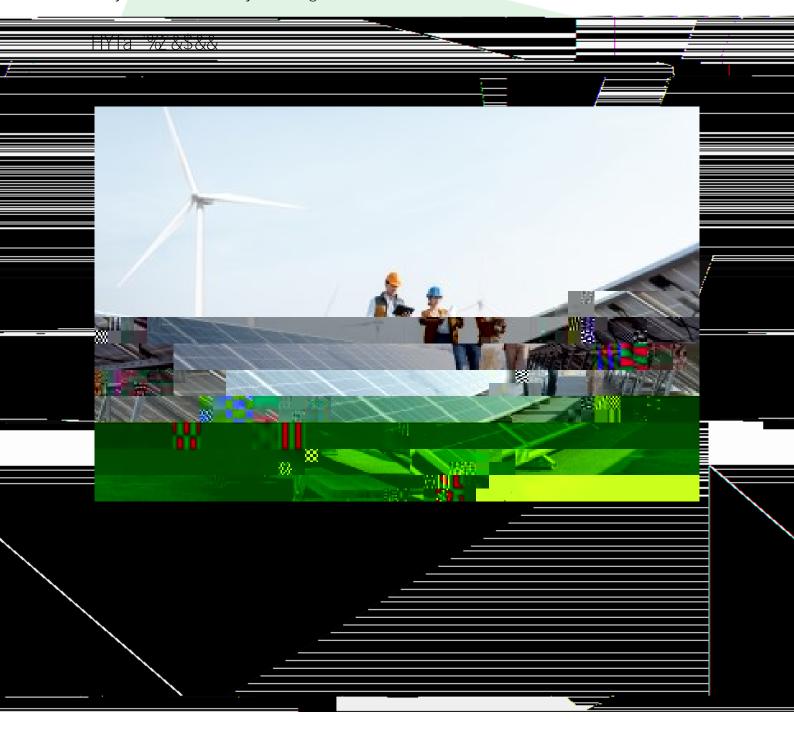


# **SOLA9101**

5Xj UbWYX D\chcj c`HJ]Wg



# 7ci fgY<sup>·</sup>Cj Yfj ]Yk

# GHJZZ:7cbHJWh:8YHJ]`g

# 7 cbj Ybc**7**g bj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]hm	@cWUh]cb	D\cbY
5g\fUZI XX]b	<u>U"i XX]b4 i bgk "YXi "Ui</u>	H\i fgXUm &da!(da fK YY_`m 7 cbgi `HUh]cbgŁ		

### 7ci fgY 8YHJ] g

 $I b]hg cZ7 fYX]h^*$ 

Gi a a UfmcZh\Y 7ci fgY

7 ci fgY 5 la

#### HYUWX]b[ 'GhfUhY[]Yg'

H\Y'HYUW\]b['gHfUHY[mZcf'H\]g'Wci fgY'Wca df]gYg'U'gYf]Yg'cZ`YWi fYg'UbX'k cf\_g\cdgž'dfcV'Ya g'UbX WUggYg"'H\Y''YWi fY'gYf]Yg'k]``dfYgYbhh\YcfmfY`UHYX'hc'gYa]WcbXi Whcfa UHYf]U'g'UbX'XYj]Wyg'UbX'i d!hc! XUHY']bZcfa UHJcb'UVci hUj U]`UV'Y'Yei]da Ybhž'WcgH]b[ž'UbX'eiU']hmWcblfc``fYgci fWyg"'8i f]b['k cf\_g\cdgž ghi XYbhg'WUb'U`gc'Ug\_'XYa cbglfUhcfg'Ubmei YgH]cbg'h\Yma Um\Uj Y'UVci hh\Y'a UHYf]U`'HUi [\h]b'`YWi fYg"

@YWMi fYg. H\YfY 'UfY '%\$ 'k YY\_g cZCb`]bY @YWMi fYg fA G 'HYUa gŁ]b 'HYfa 'H% &\$&&" '9UW 'k YY\_'\Ug 'hk c 'YWMi fYg']b cbY! 'UbX 'hk c!\ci fg g`chg" 'H\Y "YWMi fY 'h]a Y 'UbX 'd`UWYg 'UfY 'Ug. 'K YXbYgXUm'%. \$\$ ! '% .\$\$ z fA G HYUa gŁ'UbX cb 'H\i fgXUm'%) .\$\$ - '%+.\$\$ 'fA G 'HYUa gŁ' '5 ````YWMi fY 'bchYg 'k ]```VY 'dfcj ]XYX 'VY zcfY 'h\Y 'YWMi fY zY]h\Yf'j ]U'I BGK 'g 'A ccXY 'g]hY 'cf'Ug 'd\chcWcd]YX \UbXci hg"

.

K cf\_g\cdg. '±o'h\Y'k cf\_g\cd'gYgg]cbžghi XYbhg'k]``k cf\_']b'ga U``[ fci dg"'H\Y'k cf\_g\cd'dfcV'Ya g'k]` VY'dfcj ]XYX'VYZcfY'YUW\'k cf\_g\cdžY]h\Yf'j ]U'A ccX'Y'cf'Ug'U'd\chc\\cd]YX'\UbXci h''H\Y'gc'i h]cbg'k]``VY dfcj ]XYX'Xi f]b[ 'cf'UZhYf'YUW\'k cf\_g\cd"'H\Y'k cf\_g\cd'g\\YXi 'Yg'Zcf'HYfa 'H\ž'&\$&\&']g'Ug. 'K YXbYgXUm\\((.\$\$'-\%'.\$\$'fC\b')\bYž'A G'HYUa g\z\z'H\i fgXUm'\&.\$\$'-\%'.\$\$'f@Uk 'Vi]'X]b[ '%' &\z\z\z\U\Y\z''''

.

5gg][ ba Ybhg. `H\YfY`UfY`hk c`Ugg][ ba Ybhg`]b`h\]g`Wti fgY"`5gg][ ba Ybhg`k]```VY`dfcj]XYX`j]U`I\_BGK 'g A ccX`Y`g]hY"`H\Y`hk c`hU\_Y!\ca Y`Ugg][ ba Ybhg`k]```VY`\UbXYX`ci h]b`k YY\_g`%UbX`+"`H\Y]f`Xi Y`XUhYg`k]`` VY`g\ck b`cb`h\Y`dUdYfg"`H\Y`gc`i h]cbg`a UmVY`dfYgYbhYX`]b`h\Y`K cf\_g\cd`fVi hk]``bchVY`X]ghf]Vi hYXŁ"

Ghi XYbhgʻUfYʻUʻgcʻghfcb[`miYbWci fU[YXʻhcʻi gYʻh\YʻX]gW gg]cbʻ[fci dʻcbʻA ccX`YʻhcʻUgg]ghh\Y]fʻ`YUfb]b["8Ya cbghfUhcfg`k]``a cb]hcfʻh\Y`X]gW gg]cbgʻUbX`\Y`dʻUbgk YfʻdcghYX'ei Ygh]cbg"

.

: ]bU``9I Ua .`: ]bU``YI Ua `]b`th`]g`Wti fgY`]g`U`gtUbXUfX`&`\ci f`cb`]bY`k f]thYb`YI Ua ]bUt]cb"`I b]j Yfg]tm Uddfcj YX`WJ`W``Uhcfg`UfY`U``ck YX"`H\Y`YI Ua ]bUt]cb`thYghg`UbU`mt]\WJ``UbX`Wf]t]WJ``th`]b\_]b[`UbX`[YbYfU` i bXYfgtUbX]b[`cZth\Y`Wti fgY`a UthYf]U``]b`U`Wtblfc``YX`ZJg\]cb"`E i Ygt]cbg`a UmVY`XfUk b`Zfca `UbmUgdYWicZth\Y`Wti fgYži b`Ygg`gdYWJZJWJ``m]bX]\WJthX`cth\Yfk ]gY`Vmth\Y``YWfi fYf"`A Uf\_g`k ]```VY`Ugg][ bYX`UVWtfX]b[`tch\Y`WtffYWfbYgg`cZth\Y`fYgdcbgYg"

.

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#### 5XX]h]cbU`7ci fgY \=bZcfa Uh]cb

5```Wci fgY`a UhYf]U`g`UbX`Ubbci bWYa Ybhg`k]```VY`dcghYX`cb`A ccX`Y"`D`YUgY`bchY`h\Uhimci `k]```VY`XYYa YX hc`\Uj Y`fYWY]j YX`h\]g`]bZcfa Uh]cbžgc`mci `g\ci `X`hU\_Y`WUfYZ\``bchY`cZU```Ubbci bWYa Ybhg"H\]g`]g`U`\* I c7 Wci fgY`UbX`h\Y`YI dYWhYX`k cf\_`cUX`]g`%&—%(`\ci fg`dYf`k YY\_'h\fci [\ci hih\Y`%\$!k YY\_'hYfa "'GC @5 - %\$%]g U``Yj Y``) `Wci fgY"'=h]g`cZZYfYX`hc'' fX`UbX`(h\`mYUf`I; `ghi XYbhg`UbX`; fUXi UhY`8]d`ca U`UbX`A UghYf'g Dcgh[fUXi UhY`dfc[fUa g`ghi XYbhg`]b`h\Y`GW\cc``cZD\chcj c`hU]WUbX`F YbYk UV`Y`9bYf[m 9b[]bYYf]b[ 'GW\cc`''=h]g`U`dfcZYgg]cbU``Y`YWhj Y`Wci fgY`Zcf`h\Y`D\chcj c`hU]WUbX`Gc`Uf`9bYf[mDfc[fUa "'=h]g`U`WcfY#Y`YWhj Y`Wci fgY`Zcf`ghi XYbhg`Zc``ck]b[`U`69`fA UhYf]U`g`GW]YbWY`cf`9`YWhf]WU``9b[]bYYf]b[ Ł dfc[fUa `UbX`ch\Yf`Wca V]bYX`XY[fYY`dfc[fUa gž`UbX`Ub`Y`YWhj Y`Zcf`d\mg]Wg`ghi XYbhg'"

#i]g Uggi a YX h\ Uhghi XYbhg Ybfc``YX ]b h\ ]g Wci fgY UfY ZUa ]`]Uf k ]h\ gYa ]WcbXi Wrcf a UhYf]U`g UbX XYj ]WYg gi W. Ug d\chcj c`hU]WXYj ]WYg UbX X]cXYg"

7 cbgi `Huhjcbg.': cf'U```Ybei ]f]Yg'UVci hih.Y'Wci fgYž'd`YUgY'WcbHUWhih.Y'Wci fgY'Wcbj YbYf"5 fY[i `Ufk YY\_`mWcbgi `Huhjcb'hja Y']g'cb'H\i fgXUm&!'( 'da 'cb`]bY'fA G'HYUa gŁ'cf']bH9H6'fcca '%&\*"'': cf'U`` ch\Yf'ei Yghjcbg'cf'Ybei ]f]Ygž'mci 'UfY'YbWci fU[YX'hc'Ug\_'h\Y'`YWi fYf'UZhYf'WUgg'cf'dcghimci f'ei Yghjcbg'cb h\Y'8]qW qq]cb'6cUfX'cb'A ccX`Y"

\htdg.##a ccX\Y"hY\h'i bak "YXi "Ui #c[]b#bXYI "d\d

SOLA9101 // Term 1, 2022 // published at 10-02-2022 © UNSW Sydney, 2022

### 5ggYgga Ybh

#### 5ggYgga Ybhg

HU_Y! <ca &<="" ba="" th="" y`5gg][="" ybh%=""><th>`&amp;\$I</th></ca>	`&\$I
A ]X!HYfa '9I Ua '	·%) I
GY`ZI@YUfb]b[ '9  Ua 'fHYfa '9bX'HYghz''	·%) I
: ]bU`9I Ua `f&`\ci fgŁ``	···) \$ı

- $\bullet \ 5 @@a \ UhYf]U``dfYgYbhYX`Xi f]b[ \ 'h\Y`gYgg]cbg`k ]```VY`YI Ua \ ]bUV`Y`]b'`h\Y`Z]bU``YI Ua 'i b`Ygg`ch\Yfk ]gYbchYX''`$
- 5```UggYggUV`Y`k cf\_`flYl WYdhih\Y`: ]bU``9l Ua Ła i ghVY`gi Va ]lhYX`k ]h\`U`Wca d`YhYX`fUbX`g][ bYXŁ Wcj Yf`g\YYh`Wb`VY`Xck b`cUXYX`Zfca 'h\Y`7 ci fgY`A ccX`Y`g]hY"
- @UhY`Ugg][ ba Ybhg`k ]```VY`dYbU`]nYX`)ı ž'd`i g`)ı 'dYf`XUmih\Uhih\Y`k cf\_`]g``UhY`fa Ul ]a i a 'dYbU`hm ]g`%\$\$ı Ł"`C bWY`h\Y`gc`i h]cbg`UfY`dfYgYbhYXž'h\Y`a Ul ]a i a 'dYbU`hmk ]```Udd`m'

K Y][\h 5ggYgga Ybh'hUg\_ 8i Y'8UHY 7 ci fgY @YUfb]b[ Cihwca Yg 5ggYggYX %\$#\$' #&\$&&`%&.\$\$`5A %" `A ]X!HYfa '91 Ua %) I %ž'&ž'' &"'5gg][ ba Ybh!'% **%\$**1 % #\$' #&\$&&`%&.\$\$`5A %ž'&ž'' ' "5gg][ ba Ybh! & **%\$**1 &&#\$(#&\$&&`%&.\$\$`5A ( ( ("'HYfa!9bX'HYgh %) I &%#\$(#&\$&&`%&.\$\$`5A ": ]bU`'91 Ua Hc 'VY 'WcbZfa YX %ž'&ž'' ž'( ) \$1

### 5qqYqqa Ybh% A ]X!HYfa '9l Ua

GhUfh:XUhY. "%\$#\$" #&\$&&" \\ . \\$ \\$ \\$ A

Gi Va ]gg]cb bch/g. >i ghUZh/fh\Y h/ghzfygi `hg k ]``VY Ui hca UhJWJ`mgi Va ]hh/X cb A ccXY

8i Y'XUhY. '%\$#\$' #&\$&&'\\&.\$\$\'5A

A ]X!HYfa 'YI Ua 'k ]``'Wcj Yf'U``'gc`Uf'WY``'XYj ]WYg']b'H\Y'Wci fgY"'≢ik ]``'VY'UddfcI ]a UHY`m(\$'a ]bi HYg'UbX'k ]`` VY'Ub'cb`]bY'YI Ua "

#### 5ggYgga Ybh'Wf]hYf]U

D`YUgY`gYY`GC @5 - %\$%`A ccX`Y`g]hY`Zcf`5ggYgga Ybh7f]hYf]U"

#### 5ggYgga Ybh& 5gg][ ba Ybh! %

GhUfhiXUhY. '% #\$&#&\$&& '%&.\$\$ '5A

Gi Va ]gg]cb bchYg. 'D`YUgY'gi Va ]hmci f`Ugg][ ba Ybh']b h\Y'gi Va ]gg]cb Vcl ']b A ccX`Y"

8i Y'XUhY.'% #\$' #&\$&&'%&.\$\$'5A

**8YUX`]bY**'Zcf'UVgc`i hY'ZU]`. ``@UhY'Ugg][ba Ybhg'k]```VY'dYbU`]nYX')ı ž'd`ig')ı 'dYf'XUmh\Uh'h\Y'k cf\_']g `UhY'fa Ul]a ia 'dYbU`hm]g'%\$\$ı E"'C bWY'h\Y'gc`i h|cbg'UfY'dfYgYbhYXž'h\Y'a Ul]a ia 'dYbU`hmk]``'Udd`m'

5gg][ ba Ybh%k ]``VY`dfcj ]XYX`]b`k YY\_`%@YWi fY`]b`A ccX`Y"`Gh XYbhg`bYYX`hc`gc`j Y`h\Y`Ugg][ ba Ybh%dfcV`Ya g`UbX`gi Va ]h'h\Y`k YY\_`) `@YWi fY"

Ghi XYbhg'k]``\Uj Y'('k YY\_g'h]a Y'hc'gc'j Y'h\Y'dfcV'Ya g"

#### 5ggYgga YbhWf]hYf]U

 $\label{eq:continuous} \mbox{D'YUgY'gYY'GC @5-\%\%A ccX'Y'g]} \mbox{M'Zcf'5ggYgga Ybh'7f]} \mbox{U''} \mbox{The properties of the continuous of the continuou$ 

#### 5ggYgga Ybh' . 5gg][ ba Ybh! &

GhUfh'XUhY. '&) #\$' #&\$&&' \\ . \$ 5 A

Gi Va ]gg]cb'bchYg. 'D`YUgY'gi Va ]hh\Y'5gg][ ba Ybh&'gc`i h]cb']b'h\Y'gi Va ]gg]cb'Vcl']b'A ccX`Y"

8i Y'XUhY.'&&#\$(#&\$&&'%&.\$\$'5A

5gg][ ba Ybh&ik ]``VY`]b`A ccX`Y`]b`k YY\_`\*`@YWfi fY`UbX`ghi XYbhg`bYYX`hc`gi Va ]hh\Y`gc`i h]cb`cZ Ugg][ ba Ybh&i]b`k YY '%\$`@YWfi fY"

Gh XYbhg'k]``[Yh'('kYY\_g'ha Y'hc'gc'jY'h\Y'Ugg][ba Ybh'dfcV'Ya g"

#### 5ggYgga YbhWf]hYf]U

D`YUgY`gYY`GC @5 - %\$%`A ccX`Y`g]hY`Zcf`5ggYgga Ybh7f]hYf]U"

.

#### 5ggYgga Ybh( HYfa !9bX HYgh

GhUfhiXUhY. 84 (#8 & & 16 & 15 A

Gi Va ]gg]cb bchYg. 'D'YUgY gi Va ]hmci f'hYghfYgi 'hg 'î ghUZhYf'h\Y'hYgh'

8i Y'XUhY.'&%#\$(#&\$&&'%&.\$\$'5A

 $H\Y'HYfa !9bX'HYghk ]``Wcj Yf'U``h\Y'dfcWrgg]b[ hcd]Wg'' \\ +ik ]``VY'Uddfcl ]a UhY`m'( $`a ]bi hYg'UbX'k ]``VY'Ub cb`]bY'Yl Ua "$ 

#### 5ggYgga Ybh'Wf]hYf]U

D`YUgY`gYY`GC @5 - %\$%`A ccX`Y`g]\Y`Zcf`5ggYgga Ybh7f]\Yf]U"

5ggYgga Ybh) : ]bU`9l Ua

GHUfhXUhY. 'Hc 'VY 'WcbZ]fa YX
5 ggYgga Ybh``Yb[ h\. '&'\ci fg
Gi Va ]gg]cb'bchYg. '>i gh'UZhYf'h\Y'Yl Ua 'd`YUgY'gi Va ]hmci f'Ubgk Yf'dUdYf'k ]h\]b'' \$'a ]bi hYg"
8i Y'XUhY. 'Hc 'VY 'WcbZ]fa YX
8 YUX`]bY'Zcf'UVgc`i hY'ZU]`. ''@UhY'gi Va ]gg]cb'k ]``'bch'VY 'UWWdhYX"

H\Y': ]bU`'9| Ua 'k ]```Wcj Yf'U```rh\Y'Wci fgY'a UhYf]U`g'gi W\`Ug'`YWn fY'bchYgžk cf\_g\cdg'UbX'Ugg][ ba Ybhg"'\dank ]```VY'U'&\ci f'cb`]bY'Y| Ua ']b'A ccX`Y"'>i gh'UZhYf'h\Y'Y| Ua žghi XYbhg'bYYX'hc'gi Va ]h'h\Y]f'Ubgk Yf'dUdYfg ]b'h\Y'gi Va ]gg]cb'Vcl']b'A ccX`Y"

.

#### 5ggYgga YbhWf]hYf]U

D`YUgY`gYY`GC @5 - %\$%`A ccX`Y`g]\Y`Zcf`5ggYgga Ybh7f]\Yf]U"

# 5 hhyb XUb WY F Yei ]fYa Ybhg

 $\hbox{Ghi XYbhg'UfY'ghfcb[`m'YbWc'i fU[YX'hc'UhhYbX'U```WUggYg'UbX'fYj]Yk'``YWhi fY'fYWc'fX]b[g''' } \\$ 

# 7ci fgY'GWXYXi `Y

# 7cbHJWhi<cifg

GYgg]cbg	8 Um	H]a Y	@c₩Uh]cb
@YWhifY	K YXbYgXUm	% \$\$ <b>-</b> % . \$\$	Cb`]bY'fA G'HYUagŁ
@YWhifY	H∖i fgXUm	%) . \$\$ "—"%+. \$\$	Cb`]bY'fA G'HYUagŁ
K cf_g\cd	K YXbYgXUm	%( .\$\$ '- '%* .\$\$	Cb`]bY'fA G'HYUagŁ
K cf_g\cd	H∖i fgXUm	%.\$\$ <del>-</del> %( .\$\$	"@Uk "6`X""%*&"fl UWY!hc!
			: UVYŁ

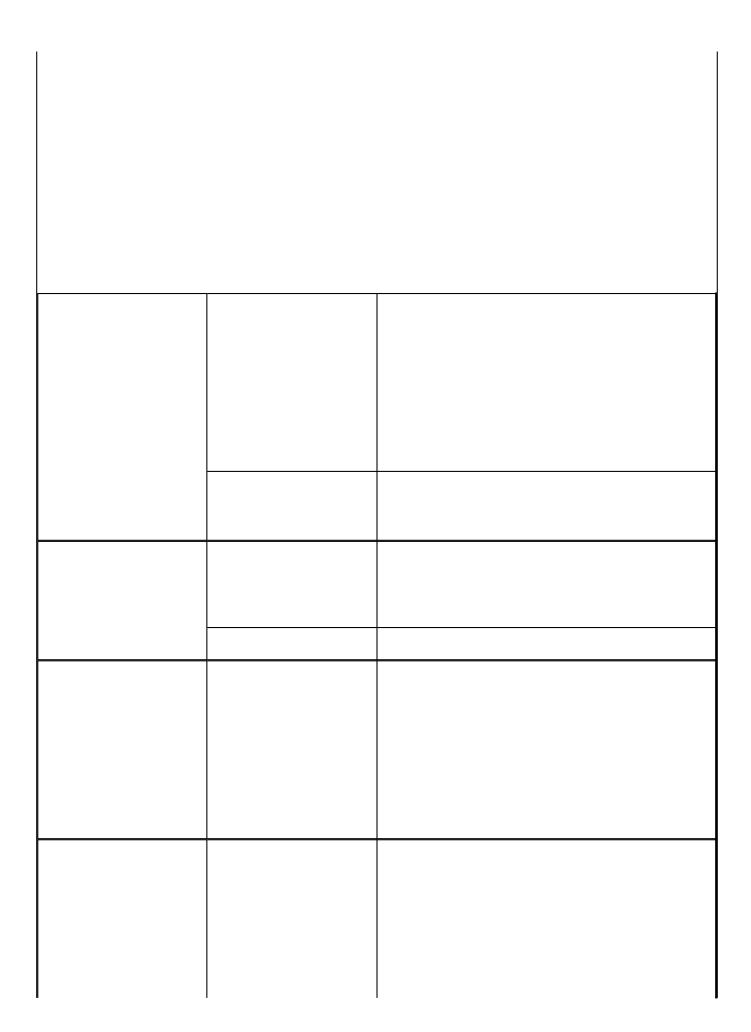
.

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# <u>J]Yk 'WUgg'hja YHUV'Y</u>

# H]a YtUV`Y

8 UhY	Hmd Y	7 cbhYbh	
K YY_'% '%( ': YVfi Ufm!	@YWhifY	@YWhifY`Hcd]Wg.	
% : YVfi Ufm		7 ci fgY ci h]bYg UbX ±bHcXi Wh]cb f@%5Łž	
		9bYf[miVUbXg`UbX`WUff]Yf`WcbW'f@%6Ł	
		7 Uff]Yf'lfUbgdcfhiD\Ybc2,YbU'f@%7 Ł"	
		BK CEGYDINY 19	
	5ggYgga Ybh	5 g][ by fY YU YX	
K YY_'&.'&%: YVfi Ufm! &) ': YVfi Ufm	@YWhifY	@YWity Hcd]Wg.	
α) . Ιντι οιπι		D!B'1\bW1jcb'X]cXYg'f@&5tž	
		G]`]Wcb'gc`Uf'WY``g'f@&6Ł	
		G]`]Wcb`gc`Uf'WY``g`fl@&7 Ł	
		/ 'K cf_g\cd'%	



### FYgci fWyg

### DfYgWf]VYX F Ygci fWYg

### 7ci fgY F Ygci fWYg

#### HYI hUbX F YZYfYbW Vcc\_g.

- %" G"A "'GnYž'E W\_ [Ua` VgUfad6 Wh[UWe /bZke[Ue S` V FWUZ` a 'aYkfž' fX`UbX`&bX`YX"'fK ]`Ymž'&\$\%.'UbX &\$\$&L"
- &" G"A "'GnYž"BZke[Ue aXE W\_ [Ua` VgUfad6Wh[UWe"ž' fX'9X]h]cb'fK ]`Ymž&\$\$+\t/ch\Yf'`YWh fY'a UhYf]U`g k ]``VY'XfUk b'Zfca 'j Uf]ci g'hYl h\cc\_g'UbX'ci fbU``dUdYfg"
- ' " A "5"; fYYbžEa′Sd5W°e\*fl BGK '6cc\_g\cdž'%, &Ł"
- ("5fj]bX'G\U\ž'"H\]b!Z\`a 'G]`]Wcb'gc`Uf'WY``q''ž'&\$%\$ž'7F7'dfYgg"
- )">"'8"'D'ia a Yfž'A "'8"'8YU`'UbX'D"6"; f|ZZ|bž'G|`|Wcb'J @G=HYWkbc`c[mž'&\$\$\$Z'DfYbh|WY'<U``"
- \*"  $'M''7 \setminus Ub["UbX'G"A""GnYž'I @G=HYWXbc`c[nž'% *ž'AW fUk'<]``$
- +" `G"'? "'; \UbX\]ž""J@G=: UVf]WUh]cb Df]bW]d`Ygž'% ( ž'>c\b'K ]`Ym"
- , "JUf]ci g K YVdU[Yg

#### Cb!`]bY'F Ygci fWfg

- K YVg]hY. I BGK 'g'A ccX`Y":5g'U'dUfhcZh\Y'hYUW\]b['Wca dcbYbhz'A ccX`Y'k]``VY'i gYX'hc X]ggYa]bUhY'hYUW\]b['a UhYf]U'gz`\cghZcfi a g'UbX'cVWUg]cbU``mei]nnYg":5ggYgga Ybha Uf\_g'k]`` U`gc'VY'a UXY'Uj U]`UV`Y'j]U'A ccX`Y. \hdg.##a ccX`Y'hY`h'i bgk "YXi "Ui #c[]b#bXYI "d\d
- @YWhifY'BchYq.'@YWhifY'bchYq'k]``VY'dfcj]XYX'VYZcfY'YUWX'`YWhifY'j]U'IBGK'q'Accx`Y'q]hY"
- K cf\_g\cdg. K cf\_g\cd'dfcV'Ya g'k]``VY'dfcj]XYX'VYZcfY'YUW\k cf\_g\cd'j]U'a ccX'Y"'H\Y gc'i f|cbg'k]``VY'dfcj]XYX'UZYf'YUW\k cf\_g\cd']b'I BGK 'a ccX'Y'g]f\"
- 5gg][ ba Ybhg flubX ch\Yf Wci fgY a UhYf]u`gŁ k ]``VY dfcj ]XYX j ]u i BGK 'g A ccX`Y g]hY"
- D7 %8 'gc`Uf`WY```g]a i `Uhcf. '=g']bghU``YX`cb`h\Y`D7g']b'H9H6": cf'U'dYfgcbU``WcdmzgYY`
   k k k "dj "i bgk "YXi "Ui #]b\_g#dfcXi Wmg#dW%X"Ugd"

.

### Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

 $K_cf_gi_Va_h^2X^uh'_k_h^2x^uh'_k_h^2X^uh'$ 

 $\label{thm:condition} $$HY^`UhY`dYbU`hmi]g`Udd`]YX`dYf`WU`YbXUf`XUmif]bWi X]b[`k YY_YbXg`UbX`di V`]W`\c`]XUmg&h\Uhih\Y UggYgga Ybhi]g`cj YfXi Y''`H\YfY`]g`bc`dfc!fUhU`cZh\Y``UhY`dYbU`hmiZcf`gi Va ]gg]cbg`a UXY`dUfhk Umih\fci [\'UXUm'$ 

K cf\_'gi Va ]hhYX'UZhYf'h\Y''XYUX`]bY'Zcf'UVgc`i hY'ZU]''']g'bchUWWdhYX'UbX'U'a Uf\_'cZnYfc'k]``'VY'Uk UfXYX Zcf'h\Uh'UggYgga Ybh']hYa "

cf'gca Y'UggYgga Ybh']hYa gž'U'``UhY'dYbU`hma Umbch'VY'Uddfcdf]UhY"'H\YgY'UfY'WYUf'm']bX]\WUhYX']b'h\Y Wci fgY'ci h']bYz'UbX'gi W\'UggYgga Ybhg'fYWY]j Y'U'a Uf\_'cZnYfc']Zbch'Wca d`YhYX'Vmh\Y'gdY\\JZ]YX'XUhY" 91 Ua d'Yg']bWi XY.

U"''K YY\_`mcb`]bY`hYghg`cf``UVcfUhcfmk cf\_`k cfh\`U`ga U```dfcdcfh]cb`cZh\Y`gi VYWha Uf\_žcf

V"''C b`]bY ei ]nnYg k \YfY Ubgk Yfg UfY fY`YUgYX hc gh XYbhg cb Wca d`Yhlcbžcf

····cf

X""DUgg# U]"UggYgga YbhHJg\_g"

### 5 WUXYa ]W<cbYghmUbX D`U[]Uf]ga

 $\label{thm:continuous} IBGK ``Ug`Ub`cb[c]b[`Wcaa]haYbhhc`ZcghYf]b[``U`W``hifY`cZ`YUfb]b[`]bZcfaYX`VmUWUXYa]W]bHY[f]hm'`5``IBGK ``ghiXYbhg``UjY`U`fYgdcbg]V]`]hmhc`UX\YfY`hc`h\]g`df]bW]d`Y`cZUWUXYa]W]bHY[f]hm'`D`U[]Uf]gaibXYfa]bYg`UWUXYa]W]bHY[f]hmUbX`]g`bchhc`YfUhYX`UhIBGK "`B'SY[Sde_SfG@EI[eVWY] WW Sege[YfZWiadVead[VWSeaXafZWdeS`VbSee[YfZW_aXXSekagdai`ž$ 

D`U[]Uf]ga i]g`U`hmdY`cZ]bhY``YWi U``h\YZh'`±iWUb`hU\_Y`a UbmZcfa gžZfca `XY`]VYfUhY`W\YUh]b[`hc`UWV]XYbhU``m Wcdm]b[`Zfca `U`gci fWYk]h\ci hUW\_bck `YX[Ya Ybh'`I BGK `\Ug`dfcXi WYX`U`k YVg]hY`k]h\`U`k YU`h\`cZ fYgci fWYg`hc`gi ddcfhighi XYbhg`hc`i bXYfghUbX`UbX`Uj c]X`d`U[]Uf]ga žij ]g]h`ghi XYbh'i bgk "YXi "Ui #d`U[]Uf]ga "H\Y`@YUfb]b[`7 YbhY`Ugg]ghg`ghi XYbhg`k]h\`i bXYfghUbX]b[`UWUXYa]W]bhY[f]hmUbX`\ck 'bchhc'd`U[]Uf]gY" H\YmU`gc`\c`X`k cf\_g\cdg`UbX`WUb`\Y`d`ghi XYbhg`cbY!cb!cbY"

Mci 'UfY'U'gc'fYa ]bXYX'h\Uh'WUfYZ\ ``h]a Y'a UbU[Ya Ybh']g'Ub']a dcfhUbhdUfhcZgh XmUbX'cbY'cZh\Y ]XYbh]Z]YX'WUi gYg'cZd'U[]Uf]ga ']g'dccf'h]a Y'a UbU[Ya Ybh'Gh XYbhg'g\ci `X'U``ck 'gi ZZ]W]Ybh'h]a Y'Zcf

# 5 WUXYa] W + D Zcfa Uh]cb

7 ci fgY'9j U'i Uh]cb'UbX'8Yj Y`cda Ybh'

# 5ddYbX]l. '9b[]bYYfg'5i glfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWm GHJbXUfX

Dfc[fUa '±bhYbXYX'@YUfb]b['CihWca Yg	
?bck `YX[Y'UbX'g_]```VUgY	
D9%"%7cadfY\Ybg]j Yž'h\YcfmVUgYX'i bXYfgHJbX]b[ 'cZh\Y'i bXYfd]bb]b[ 'bUhi fU`'UbXd\mg]\WJ`'g\\Yb\W'g'UbX'h\Y'Yb[ ]bYYf]b[ 'Z bXUaYbHJ`g'Udd`]\WJV`Y'hc'h\Y'Yb[ ]bYYf]b[ 'X]g\\]d`]bY	
D9%"&`7cbWYdhiU``ibXYfghUbX]b['cZh\Y'aUh\YaUh]WgžbiaYf]WU``UbU`mg]gžghUh]gh]WgžUbX WcadihYf'UbX']bZcfaUh]cb'gW]YbWYg'k\]W\`ibXYfd]b'h\Y'Yb[]bYYf]b['X]gW]d`]bY	
D9%" '±0!XYdh\'i bXYfghUbX]b[ 'cZgdYW]U`]ghVcX]Yg`cZ_bck `YX[ Y`k ]h\]b`h\Y`Yb[ ]bYYf]b[ X]gW]d`]bY	
D9%"( '8]gVWfba YbhcZ_bck 'YX[ Y'XYj Y`cda YbhUbX'fYgYUfVX 'X]fYWf]cbg'k ]h\]b'h\Y Yb[]bYYf]b[ 'X]gWJd`]bY	
D9%") '? bck `YX[Y`cZYb[]bYYf]b[ `XYg][b`dfUWf]WY`UbX`WcbHYl hi U``ZUWcfg`]a dUWf]b[ 'h\Y Yb[]bYYf]b[ `X]gW]d`]bY	
D9%"* 'I bXYfgHJbX]b[ 'cZh\Y'gWcdYz'df]bWjd`Ygz'bcfa gz'UWVci bHJV]`]hjYg'UbX'Vci bXg'cZ gi gHJ]bUV`Y'Yb[ ]bYYf]b[ 'dfUWfJWY']b'h\Y'gdYWjZJWX]gWjd`]bY	
9b[]bYYf]b[:Udd`]WUh]cb:UV]`]hm	